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# Compilation Principle 编译原理

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## 第14讲：语义分析(2)

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# Review Questions

- Why context analysis is not performed in parsing stage?  
Parsing relies on CFG, which is context free.
- Give some examples of semantic analysis.  
Def-before-use, no redefinition, same type, scoping ...
- What is Syntax Directed Translation?  
The parsing process and parse trees are to direct semantic analysis and the translation of the program (a.k.a., CFG-driven translation)
- How to augment grammar for semantic analysis?  
Semantic attributes for symbols, rules/actions for productions
- What are SDD and SDT?  
SDD = Syntax Directed Definitions, SDT = SD Translation Schemes
- What is an synthesized attribute?  
Defined by attribute values of node  $N$ 's children and  $N$  itself

# Example: Synthesized Attribute (cont.)

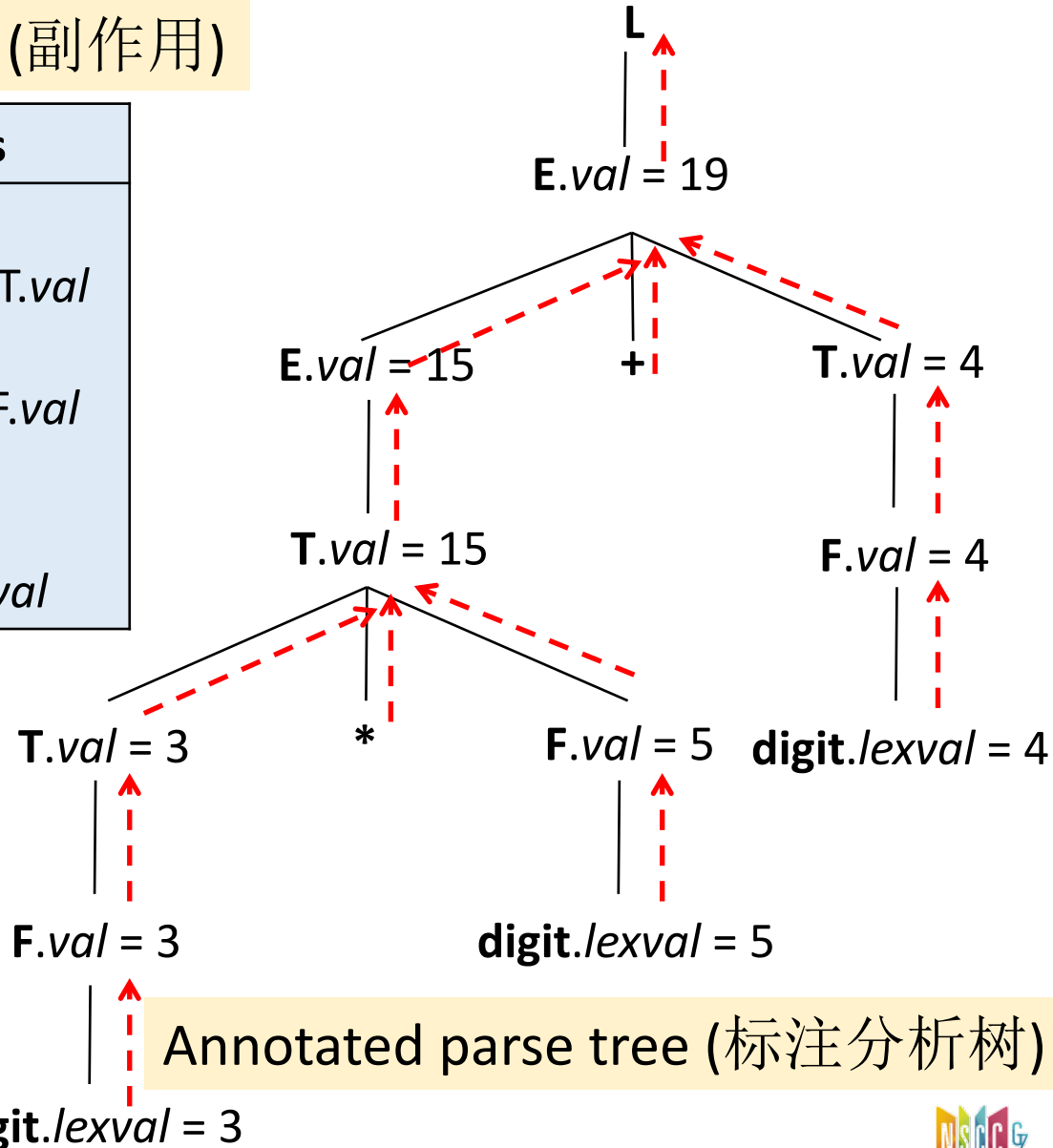
SDD:

Side effect (副作用)

Production Rules	Semantic Rules
(1) $L \rightarrow E$	<code>print(E.val)</code>
(2) $E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
(3) $E \rightarrow T$	$E.val = T.val$
(4) $T \rightarrow T_1 * F$	$T.val = T_1.val \times F.val$
(5) $T \rightarrow F$	$T.val = F.val$
(6) $F \rightarrow (E)$	$F.val = E.val$
(7) $F \rightarrow \text{digit}$	$F.val = \text{digit.lexval}$

Input:

3 \* 5 + 4



# Example: Inherited Attribute[继承]

SDD:

Production Rules	Semantic Rules
(1) $D \rightarrow T L$	$L.inh = T.type$
(2) $T \rightarrow int$	$T.type = int$
(3) $T \rightarrow float$	$T.type = float$
(4) $L \rightarrow L_1, id$	$L_1.inh = L.inh$ $addtype(id.entry, L.inh)$
(5) $L \rightarrow id$	$addtype(id.entry, L.inh)$

$T$  has synthesized attribute *type*  
 $L$  has inherited attribute *inh*

Pointing to a symbol-table[符号表] object

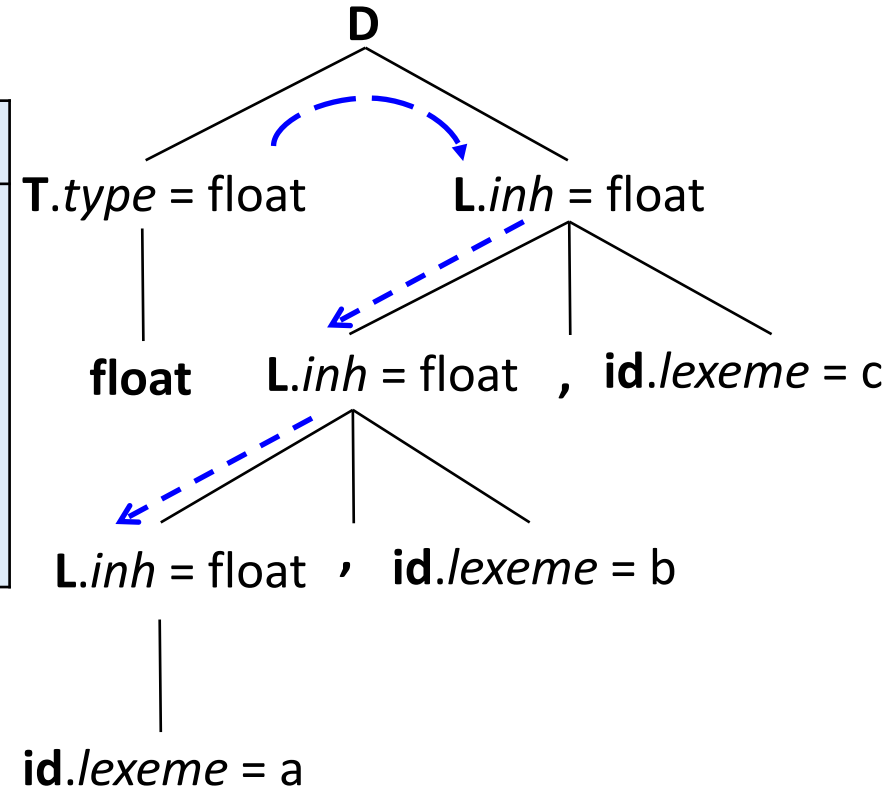
Variable declaration of type int/float followed by a list of IDs:

- (1) Declaration: a type  $T$  followed by a list of  $L$  identifiers
- (2) Evaluate the synthesized attribute  $T.type$  (int)
- (3) Evaluate the synthesized attribute  $T.type$  (float)
- (4) Pass down type, and add type to symbol table entry for the identifier
- (5) Add type to symbol table

# Example: Inherited Attribute (cont.)

SDD:

Production Rules	Semantic Rules
(1) $D \rightarrow T L$	$L.inh = T.type$
(2) $T \rightarrow int$	$T.type = int$
(3) $T \rightarrow float$	$T.type = float$
(4) $L \rightarrow L_1, id$	$L_1.inh = L.inh$ $addtype(id.entry, L.inh)$
(5) $L \rightarrow id$	$addtype(id.entry, L.inh)$



Input:

float a, b, c

*type* depends on **child**  
*inh* depends on **sibling or parent**

# The Concepts

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- **Side effect**[副作用]
  - 一般属性值计算（基于属性值或常量进行的）之外的功能
  - 例如: code generation, print results, modify symbol table ...
- **Attribute grammar**[属性文法]
  - 一个没有副作用的SDD
  - The rules define the value of an attribute purely in terms of the value of other attributes and constants[属性文法的规则仅仅通过其他属性值和常量来定义一个属性值]
- **Annotated parse-tree**[标注分析树]
  - 每个节点都带有属性值的分析树
    - A parse tree showing the value(s) of its attribute(s)
  - a.k.a., attribute parse tree[属性分析树]
  - Can also have actions being annotated[也可标注语义动作]

# Dependence Graph[依赖图]

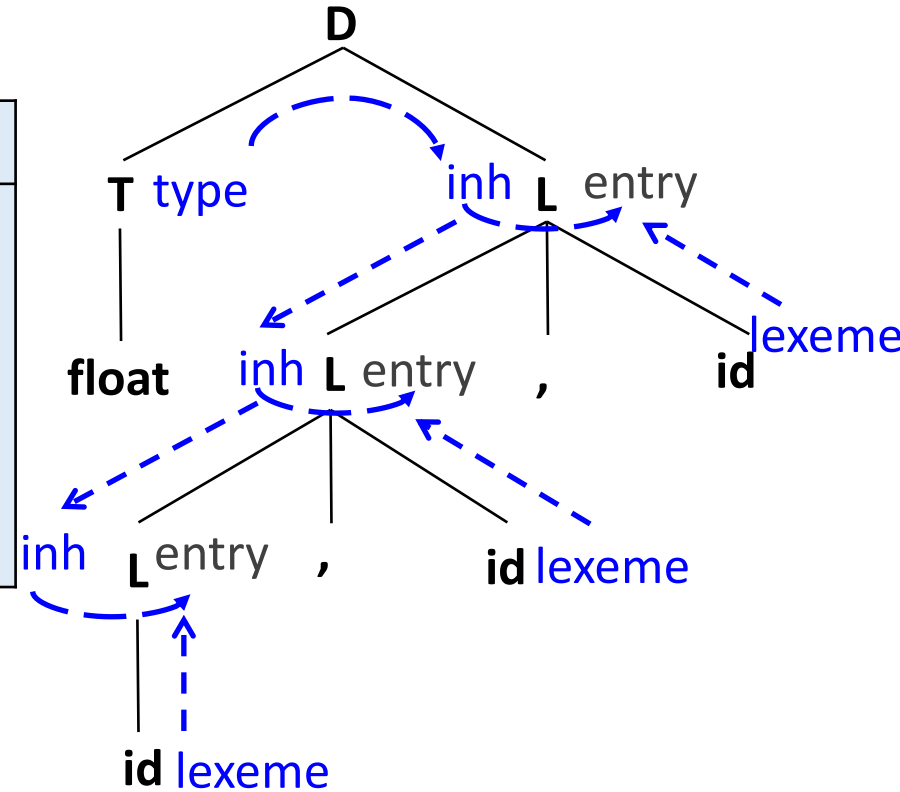
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- Dependence relationship[依赖关系]
  - Before evaluating an attribute at a node of a parse tree, we must evaluate all attributes it depends on[按照依赖顺序计算]
- **Dependency graph**[依赖图]
  - While the annotated parse tree shows the values of attributes, a dependency graph helps determine how those values can be computed[依赖图决定属性值的计算]
  - Depicts the flow of info among the attribute instances in a particular parse tree[描绘了分析树的属性信息流]
    - **Directed graph** where edges are dependence relationships between attributes
    - For each parse-tree node  $X$ , there's a graph node for each attr of  $X$
    - If attr  $X.a$  depends on attr  $Y.b$ , then there's one directed edge from  $Y.b$  to  $X.a$

# Example: Dependency Graph

SDD:

Production Rules	Semantic Rules
(1) $D \rightarrow T L$	$L.inh = T.type$
(2) $T \rightarrow int$	$T.type = int$
(3) $T \rightarrow float$	$T.type = float$
(4) $L \rightarrow L_1, id$	$L_1.inh = L.inh$ $addtype(id.entry, L.inh)$
(5) $L \rightarrow id$	$addtype(id.entry, L.inh)$



Input:

float a, b, c

'entry' is dummy attribute for the *addtype()*



# Evaluation Order[属性值计算顺序]

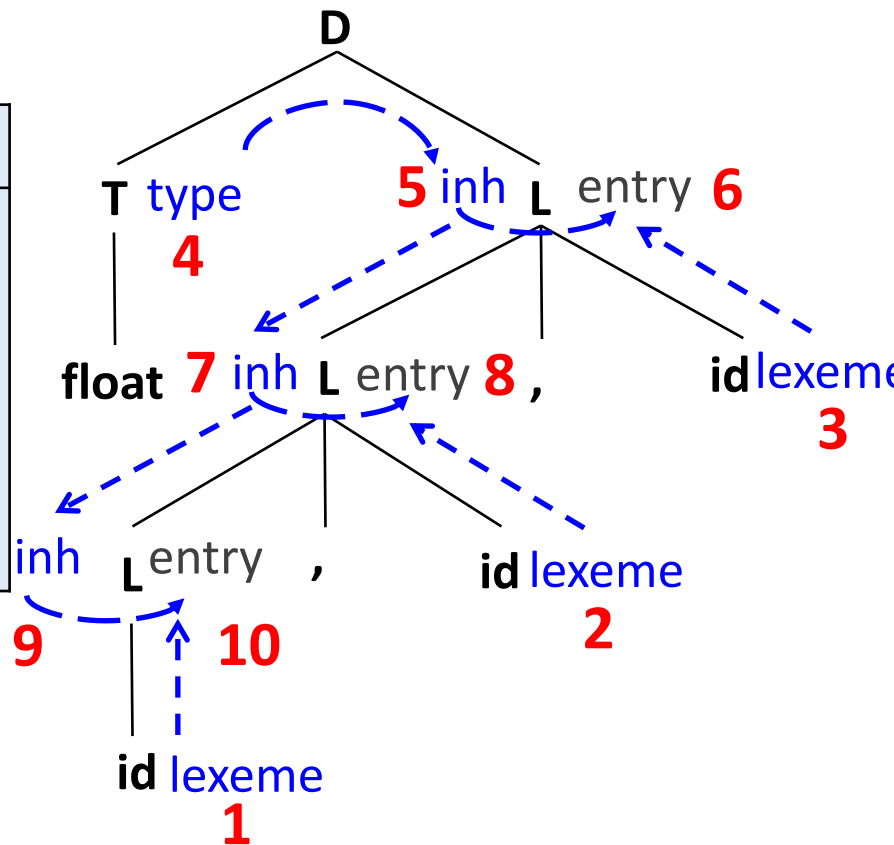
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- Ordering the evaluation of attributes[计算顺序]
  - Dependency graph characterizes possible orders in which we can evaluate the attributes at the various nodes of a parse-tree
- If the graph has an edge from node  $M$  to node  $N$ , then the attribute associated with  $M$  must be evaluated before  $N$ [用图的边来确定计算顺序]
  - Thus, the only allowable orders of evaluation are those sequences of nodes  $N_1, N_2, \dots, N_k$  such that if there is an edge of the graph from  $N_i$  to  $N_j$ , then  $i < j$
  - Such an ordering embeds a directed graph into a linear order, and is called a **topological sort**[拓扑排序] of the graph
    - If there's any cycle in the graph, then there are no topological sorts, i.e., no way to evaluate the SDD on this parse tree
    - If there are no cycles, then there is always at least one topological sort

# Example: Evaluation Order

SDD:

Production Rules	Semantic Rules
(1) $D \rightarrow T L$	$L.inh = T.type$
(2) $T \rightarrow int$	$T.type = int$
(3) $T \rightarrow float$	$T.type = float$
(4) $L \rightarrow L_1, id$	$L_1.inh = L.inh$ $addtype(id.lexeme, L.inh)$
(5) $L \rightarrow id$	$addtype(id.lexeme, L.inh)$



Input:

float a, b, c

Topological sort:

1, 2, 3, 4, 5, 6, 7, 8, 9, 10

# Evaluation Order (cont.)

- Before evaluating an attribute at a node of a parse tree, we must evaluate all attributes it depends on[依赖关系]
  - Synthesized: evaluate children first, then the node itself
    - Any bottom-up order is fine
  - For SDD's with both inherited and synthesized attributes, there's no guarantee that there is even one evaluation order
- Difficult to determine whether exist any circularities[非常难确定是否有循环依赖]
  - But, there are useful subclasses of SDD's that are sufficient to guarantee that an evaluation order exists
    - Such classes do not permit graphs with cycles

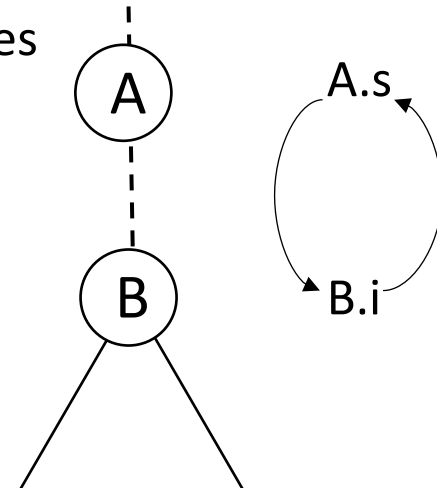
Production

$A \rightarrow B$

Semantic Rules

$A.s = B.i;$

$B.i = A.s + 1;$



# S-Attributed Definitions[s-属性定义]

- An SDD is **S-attributed** if every attribute is synthesized[只具有综合属性]
- If an SDD is S-attributed (S-SDD)
  - We can evaluate its attributes in any bottom-up order of the nodes of the parse-tree[任何自底向上的顺序计算属性值]
  - Can be implemented during bottom-up parsing[LR分析中实现]

Production Rules	Semantic Rules
(1) $L \rightarrow E$	$\text{print}(E.val)$
(2) $E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
(3) $E \rightarrow T$	$E.val = T.val$
(4) $T \rightarrow T_1 * F$	$T.val = T_1.val \times F.val$
(5) $T \rightarrow F$	$T.val = F.val$
(6) $F \rightarrow (E)$	$F.val = E.val$
(7) $F \rightarrow \text{digit}$	$F.val = \text{digit}.lexval$

# L-Attributed Definitions [L-属性定义]

- An SDD is **L-attributed** (L-SDD) if
  - Between the attributes associated with a production body, dependency-graph edges can go from left to right, but not from right to left [依赖图的边只能从左到右]
  - More precisely: each attribute must be either **synthesized**, or **inherited** but with the rules limited as follows: suppose  $A \rightarrow X_1 X_2 \dots X_n$ , the inherited attribute  $X_i.a$  only depends on
    - **Inherited** attributes associated with A **Why not synthesized?**  
**Cycle:  $X_i$  depends on A, A.s depends on  $X_i$**
    - Either *syn* or *inh* attributes of  $X_1, X_2, \dots, X_{i-1}$  located to the **left** of  $X_i$
    - Either *syn* or *inh* attributes of  $X_i$  itself, but **no cycles** formed by the attributes of this  $X_i$
- Can be implemented during top-down parsing [LL分析中]

Production Rules	Semantic Rules
$A \rightarrow B C$	$A.s = B.b$ $B.i = f(C.c, A.s)$

S-SDD or L-SDD?

Not S-SDD:  $B.i$  is inh

Not L-SDD:  $A.s$  is syn attr

Not L-SDD: C is right to B

# Syntax Directed Trans. Impl.[实现]

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- Learnt how to specify translation: SDD and SDT[定义]
  - SDT is an executable specification of the SDD
    - CFG with semantic actions embedded in production bodies
- SDT can be implemented in two ways[具体实现]
  - Using a parse tree or AST[基于预先构建的分析树]
    - First build a parse tree, and then apply rules or actions at each node while traversing the tree
    - All SDDs (without cycles) and SDTs can be implemented
      - Since the tree can be traversed freely, implements any ordering
  - During parsing, without building a parse tree[语法分析过程中]
    - Apply rules or actions at each production while parsing
    - **Only a subset** of SDDs and SDTs can be implemented
      - Evaluation ordering restricted to parser derivation order

# Syntax Directed Trans. Impl. (cont.)

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- Typically, SDD (i.e., semantic analysis) is implemented during parsing[更为高效]
  - Allows compiler to skip parse tree generation
  - Saves time and memory
- Two important classes of SDD's[两个关键子类]
  - SDD is S-attributed, the underlying grammar is LR-parsable
  - SDD is L-attributed, the underlying grammar is LL-parsable
  - For both classes, semantic rules in an SDD can be converted into an SDT with actions that are executed at the right time[允许SDD到SDT的转换]
    - During parsing, an action in a production body is executed as soon as all the grammar symbols to the left of the action have been matched

# == Implement S-SDD ==

- Convert S-attributed SDD to SDT by[SDD->SDT的转换]
  - Placing each action at the end of the production[将每个语义动作都放在产生式的最后]
  - SDTs with all actions at the right ends of the production bodies are called **postfix SDT's**[后缀/尾部SDT]

S-SDD

Production Rules	Semantic Rules
(1) $L \rightarrow E$	$\text{print}(E.val)$
(2) $E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$
(3) $E \rightarrow T$	$E.val = T.val$
(4) $T \rightarrow T_1 * F$	$T.val = T_1.val \times F.val$
(5) $T \rightarrow F$	$T.val = F.val$
(6) $F \rightarrow (E)$	$F.val = E.val$
(7) $F \rightarrow \text{digit}$	$F.val = \text{digit.lexval}$

SDT

CFG with actions
(1) $L \rightarrow E \{ \text{print}(E.val) \}$
(2) $E \rightarrow E_1 + T \{ E.val = E_1.val + T.val \}$
(3) $E \rightarrow T \{ E.val = T.val \}$
(4) $T \rightarrow T_1 * F \{ T.val = T_1.val \times F.val \}$
(5) $T \rightarrow F \{ T.val = F.val \}$
(6) $F \rightarrow (E) \{ F.val = E.val \}$
(7) $F \rightarrow \text{digit} \{ F.val = \text{digit.lexval} \}$



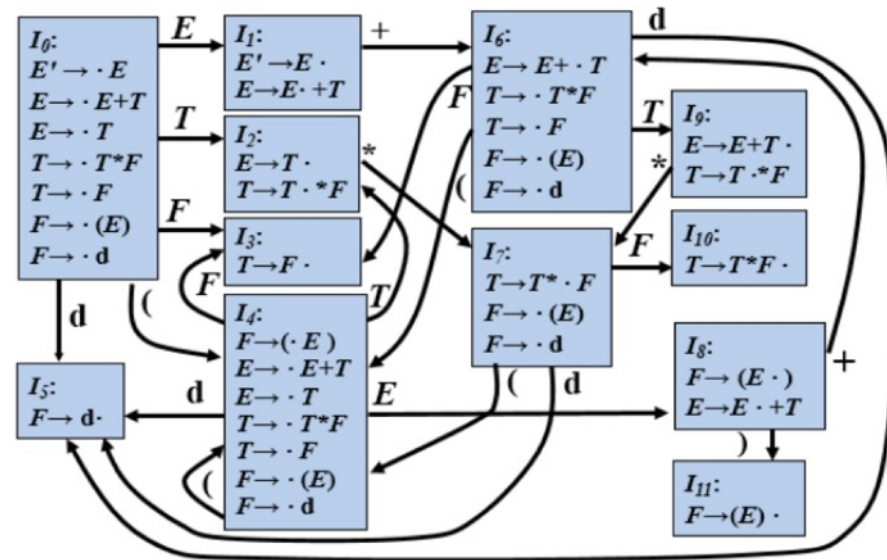
# Implement S-SDD (cont.)

- If the underlying grammar of S-SDD is LR parsable
  - Then the SDT can be implemented during LR parsing
- Implement the converted SDT by [借助归约实现]
  - Executing the action along with the reduction of  $head \leftarrow body$

## SDT

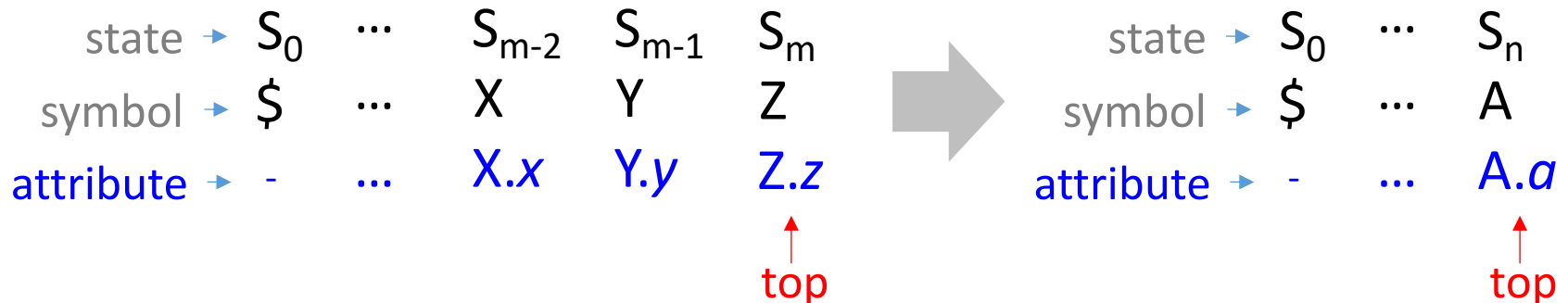
CFG with actions
(1) $L \rightarrow E$ { print (E.val) }
(2) $E \rightarrow E_1 + T$ { $E.val = E_1.val + T.val$ }
(3) $E \rightarrow T$ { $E.val = T.val$ }
(4) $T \rightarrow T_1 * F$ { $T.val = T_1.val \times F.val$ }
(5) $T \rightarrow F$ { $T.val = F.val$ }
(6) $F \rightarrow (E)$ { $F.val = E.val$ }
(7) $F \rightarrow \text{digit}$ { $F.val = \text{digit.lexval}$ }

## SLR Automaton



# Extend LR Parse Stack[扩展分析栈]

- Save synthesized attributes into the stack[栈中额外存放综合属性值]
  - Place the attributes along with the grammar symbols (or LR states that associated with these symbols) in records on stack
  - If there are multiple attributes
    - Make the records large enough or by putting pointers to records on the stack[栈记录足够大, 或栈记录中存放指针]
- Example:  $A \rightarrow XYZ$  {action}
  - $x, y, z$  are attributes of  $X, Y, Z$  respectively
  - After the action,  $A$  and its attributes are at the top (i.e.,  $m-2$ )

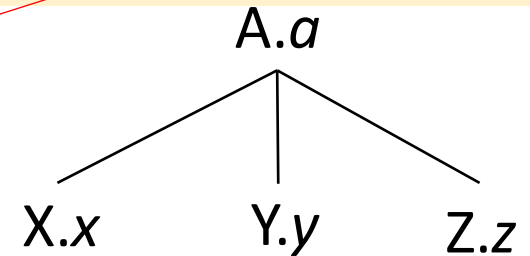


# Stack Manipulation[栈操作]

- Rewrite the actions to manipulate the parser stack[语义动作]
  - The manipulation can be done automatically by the parser

$stack[top-2].symbol = A$   
 $stack[top-2].val = f( stack[top-2].val, stack[top-1].val, stack[top].val )$   
 $top = top - 2$

$A \rightarrow XYZ \{ A.a = f(X.x, Y.y, Z.z) \}$



state	→	$S_0$	...	$S_{m-2}$	$S_{m-1}$	$S_m$
symbol	→	$\$$	...	X	Y	Z
attribute	→	-	...	X.x	Y.y	Z.z
						↑ top

state	→	$S_0$	...	$S_n$
symbol	→	$\$$	...	A
attribute	→	-	...	A.a
				↑ top

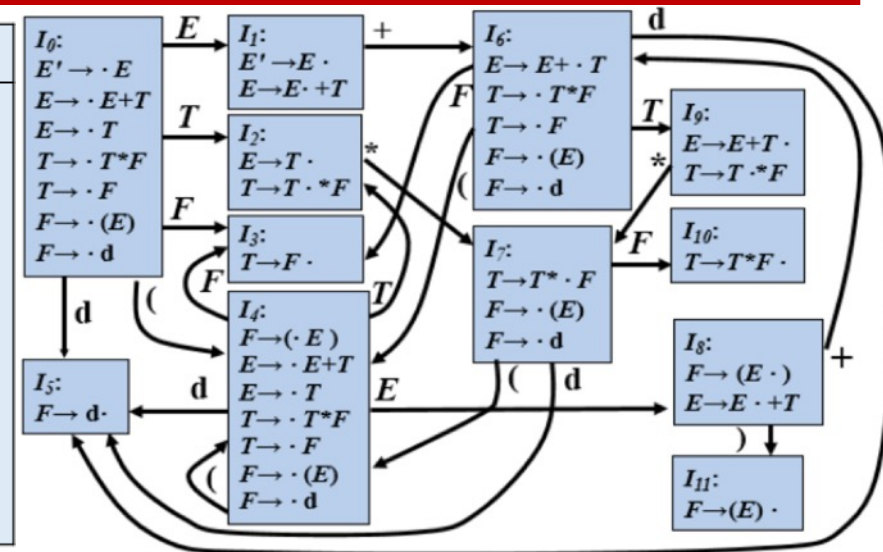
# Example

- Rewrite the actions to manipulate the parser stack
  - The manipulation can be done automatically by the parser

Productions	Semantic Rules	Semantic Actions
(1) $L \rightarrow E$	$\text{print}(E.val)$	{ $\text{print}(\text{stack}[\text{top}].val)$ ; }
(2) $E \rightarrow E_1 + T$	$E.val = E_1.val + T.val$	{ $\text{stack}[\text{top}-2].val = \text{stack}[\text{top}-2].val + \text{stack}[\text{top}].val$ ; $\text{top} = \text{top} - 2$ ; }
(3) $E \rightarrow T$	$E.val = T.val$	
(4) $T \rightarrow T_1 * F$	$T.val = T_1.val * F.val$	{ $\text{stack}[\text{top}-2].val = \text{stack}[\text{top}-2].val * \text{stack}[\text{top}].val$ ; $\text{top} = \text{top} - 2$ ; }
(5) $T \rightarrow F$	$T.val = F.val$	
(6) $F \rightarrow (E)$	$F.val = E.val$	{ $\text{stack}[\text{top}-2].val = \text{stack}[\text{top}-1].val$ ; $\text{top} = \text{top} - 2$ ; }
(7) $F \rightarrow \text{digit}$	$F.val = \text{digit}.lexval$	

# Example

Productions	Semantic Actions
(1) $L \rightarrow E$	{ print(stack[top].val); }
(2) $E \rightarrow E_1 + T$	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top - 2; }
(3) $E \rightarrow T$	
(4) $T \rightarrow T_1 * F$	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top - 2; }
(5) $T \rightarrow F$	
(6) $F \rightarrow (E)$	{ stack[top-2].val = stack[top-1].val; top = top - 2; }
(7) $F \rightarrow \text{digit}$	

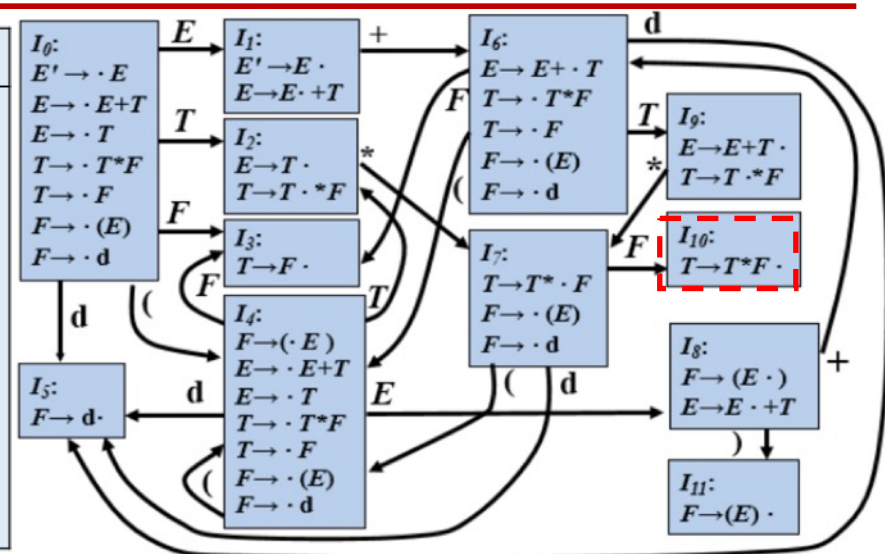


Input: 3 \* 5 + 4  
 ↑ ↑ ↑

state →  $S_0$     $S_5$     $S_7$     $S_{10}$   
 symbol → \$   #   \*   #  
 attribute → -   3   -   5

# Example (cont.)

Productions	Semantic Actions
(1) $L \rightarrow E$	{ print(stack[top].val); }
(2) $E \rightarrow E_1 + T$	{ stack[top-2].val = stack[top-2].val + stack[top].val; top = top - 2; }
(3) $E \rightarrow T$	
(4) $T \rightarrow T_1 * F$	{ stack[top-2].val = stack[top-2].val x stack[top].val; top = top - 2; }
(5) $T \rightarrow F$	
(6) $F \rightarrow (E)$	{ stack[top-2].val = stack[top-1].val; top = top - 2; }
(7) $F \rightarrow \text{digit}$	



Input: 3 \* 5 + 4



state  $\rightarrow$  S<sub>0</sub> S<sub>2</sub> S<sub>7</sub> S<sub>10</sub>  
 symbol  $\rightarrow$  \$ T \* F  
 attribute  $\rightarrow$  - 3 - 5  
↑  
top



state  $\rightarrow$  S<sub>0</sub> S<sub>2</sub>  
 symbol  $\rightarrow$  \$ T  
 attribute  $\rightarrow$  - 15  
↑  
top