



# Compilation Principle 编译原理

---

## 第14讲：语法分析(11)

张献伟

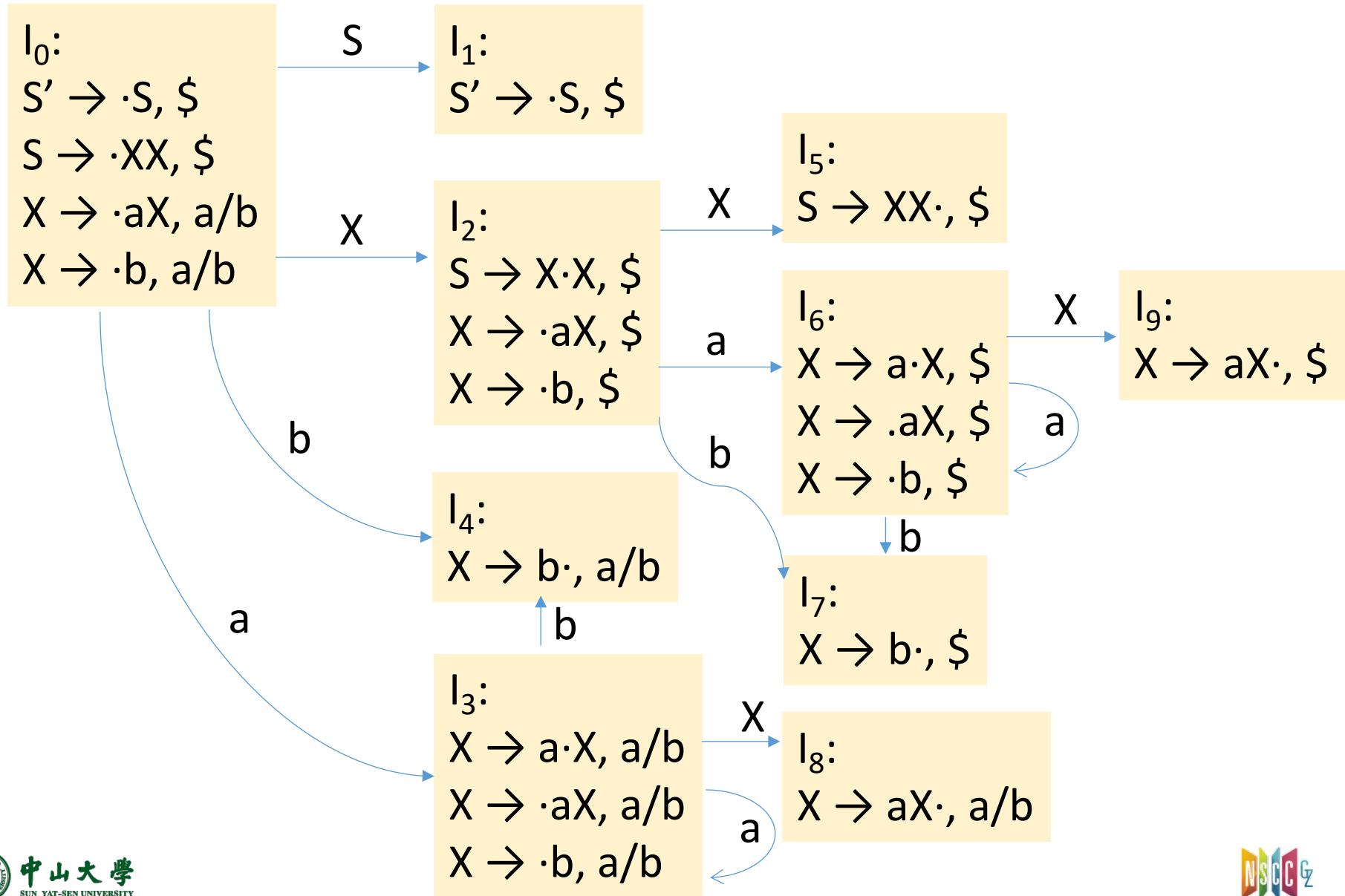
[xianweiz.github.io](https://xianweiz.github.io)

DCS290, 4/11/2023

# Review Questions

- Why LR(0) is of limited usage?  
No lookahead, easy to have shift-reduce and reduce-reduce conflicts
- How does SLR(1) improve LR(0)?  
Lookahead using the FOLLOW set when reduce happens
- At high level, how does LR(1) improve SLR(1)?  
Splitting FOLLOW set (i.e., splitting states) to enforce reduce to consider not only the stack top
- How does LR(1) split the states?  
Add lookahead to each item, i.e., LR(1) item=LR(0) item+lookahead
- How to understand the item  $[A \rightarrow u\bullet, a/b/c]$   
Reduce using  $A \rightarrow u$ , ONLY when the next input symbol is  $a/b/c$

# Example



# LR(1) Parse Table[解析表]

---

- Shift[移进]
  - Same as LR(0) and SLR(1)
  - Don't care the lookahead symbols
- Reduce[归约]
  - Don't use FOLLOW set (too coarse-grain[太粗粒度])
  - Reduce only if input matches lookahead for item
- ACTION and GOTO[表格]
  - If  $[A \rightarrow \alpha \cdot a\beta, b] \in S_i$  and  $\text{goto}(S_i, a) = S_j$ ,  $\text{Action}[i, a] = s_j$ 
    - Shift  $a$  and goto state  $j$
    - Same as SLR(1)/LR(0)
  - If  $[A \rightarrow \alpha \cdot, a] \in S_i$ ,  $\text{Action}[i, a] = r[R]$ 
    - Reduce R:  $A \rightarrow \alpha$  if input matches  $a$
    - For SLR, reduced if put input matches  $FOLLOW(A)$

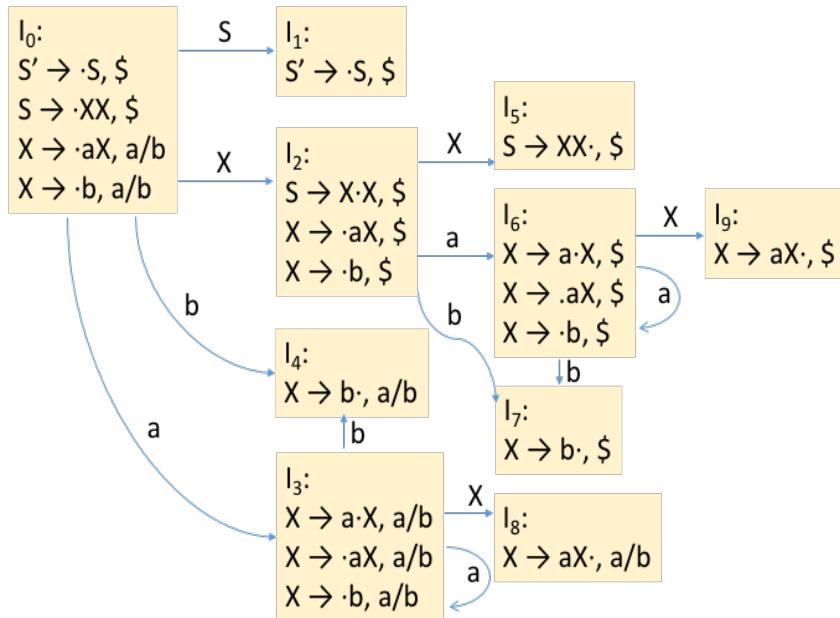
# Example

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$



State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5				r1	
6	s6	s7			9
7				r3	
8	r2	r2			
9				r2	

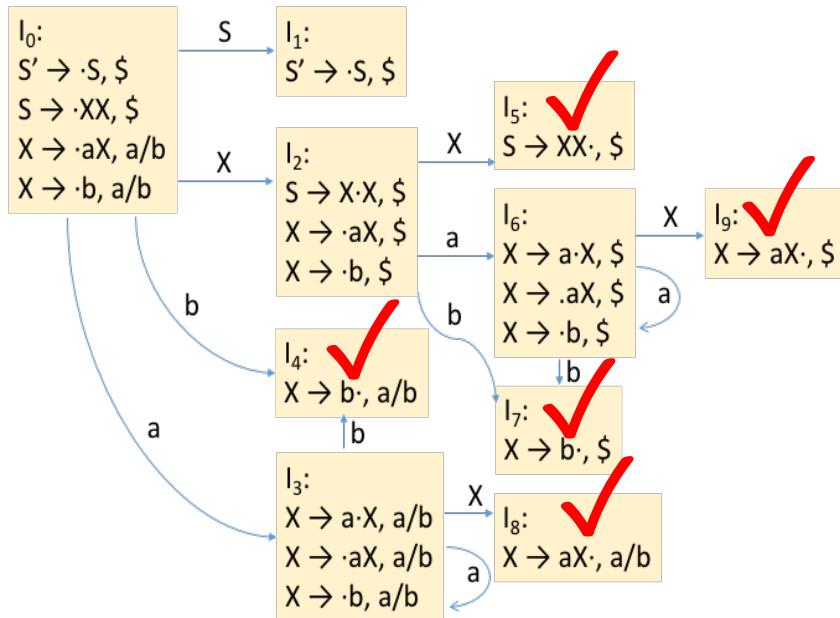
# Example

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$



State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

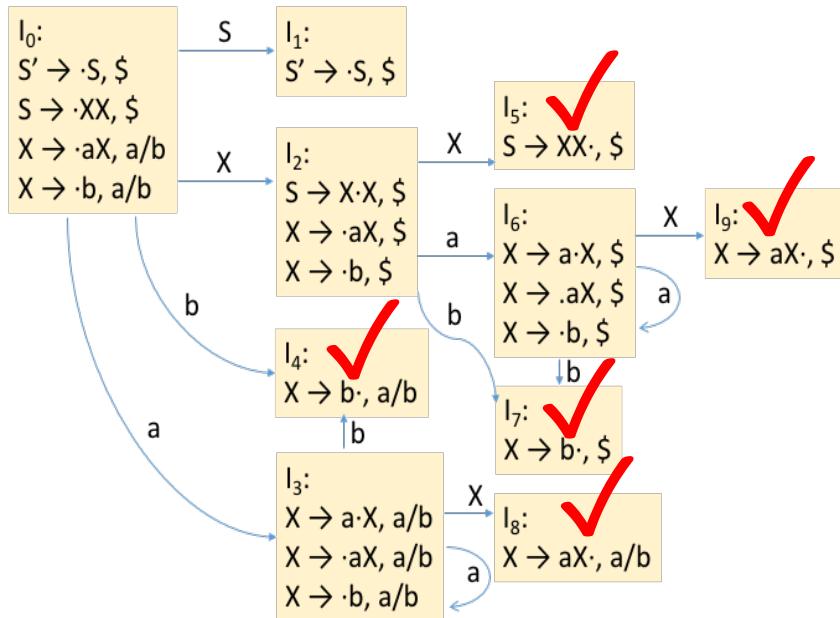
# Example

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$



State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

# LR(1) Grammars

---

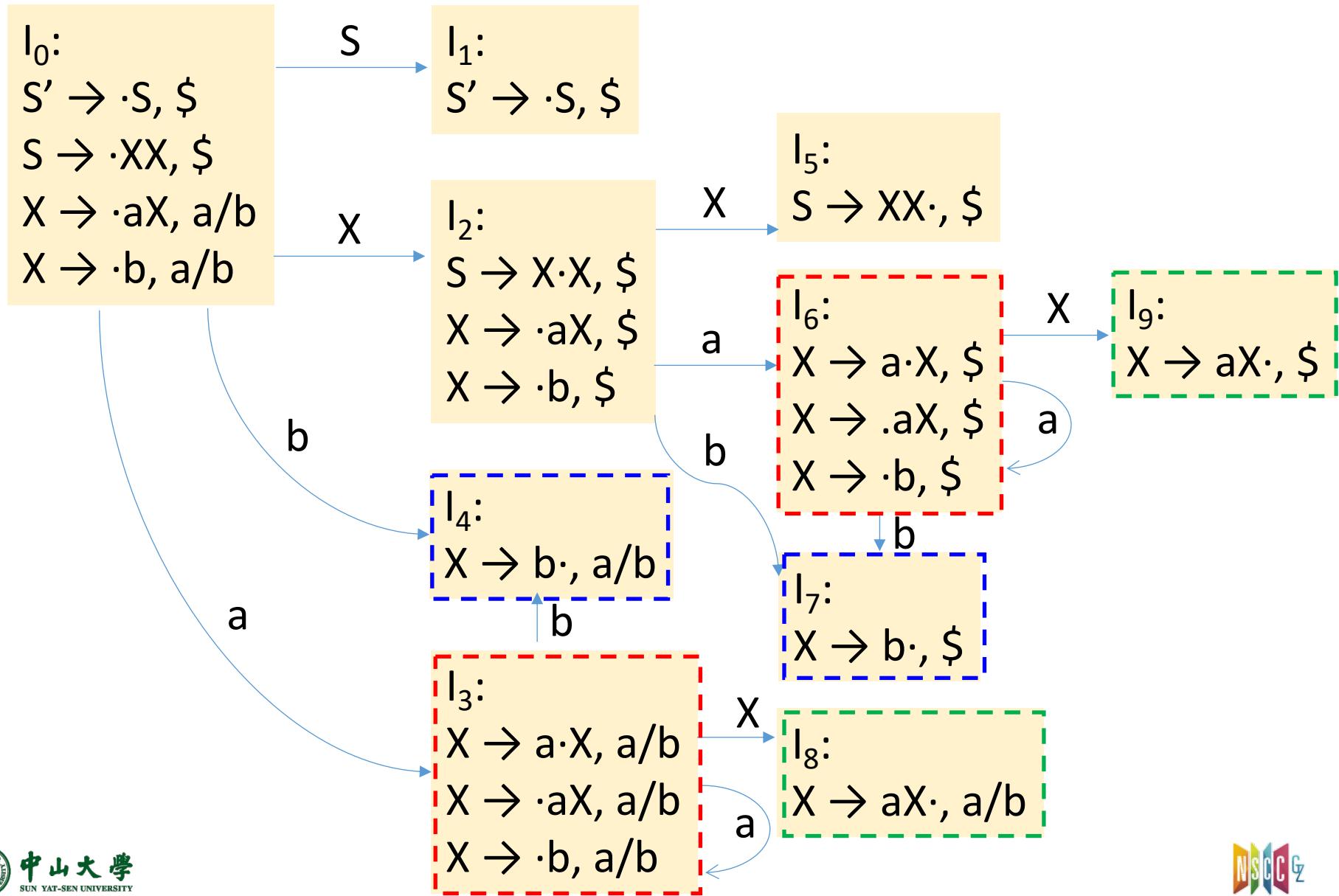
- Every SLR(1) grammar is LR(1), but the LR(1) parser may have **more states** than SLR(1) parser[SLR一定是LR, LR状态更多]
  - LR(1) parser splits states based on differing lookaheads, thus it may avoid conflicts that would otherwise result if using the full FOLLOW set
- A grammar is LR(1) if the following two conditions hold for each configuring set[是LR需要满足两个条件]
  - (1) For any item  $[A \rightarrow u \cdot xv, a]$  in the set, with terminal  $x$ , there is no item in the set of form  $[B \rightarrow v \cdot, x]$ 
    - In the table, this translates no shift-reduce conflict on any state
  - (2) The lookaheads for all complete items within the set must be disjoint, e.g. set cannot have both  $[A \rightarrow u \cdot, a]$  and  $[B \rightarrow v \cdot, a]$ 
    - This translates to no reduce-reduce conflict on any state

# LALR(1) Parser

---

- LR(1) drawbacks[缺点]
  - With state splitting, the LR(1) parser can have many more states than SLR(1) or LR(0) parser
    - One LR(0) item may split up to many LR(1) items
    - As many as all possible lookaheads
    - In theory can lead to an exponential increase in #states
- **LALR** (lookahead LR) – compromise LR(1) and SLR(1)[折衷]
  - Reduce the number of states in LR(1) parser by merging similar states[状态合并]
    - Reduces the #states to the same as SLR(1), but still retains the power of LR(1) lookaheads[LR状态可能过度细分，合并回去，但还是比FOLLOW精细]
  - **Similar states:** have same number of items, the core of each item is identical, and they differ only in their lookahead sets[相似：核心相同，展望不同]

# The Example



# State Merging[状态合并]

- Merge states with the same core
  - Core: LR(1) items minus the lookahead (i.e., LR(0) items)
  - All items are identical except lookahead

$I_3:$   
 $X \rightarrow a \cdot X, a/b$   
 $X \rightarrow .aX, a/b$   
 $X \rightarrow \cdot b, a/b$

$I_6:$   
 $X \rightarrow a \cdot X, \$$   
 $X \rightarrow .aX, \$$   
 $X \rightarrow \cdot b, \$$



$I_{36}:$   
 $X \rightarrow a \cdot X, a/b/\$$   
 $X \rightarrow .aX, a/b/\$$   
 $X \rightarrow \cdot b, a/b/\$$

$I_4:$   
 $X \rightarrow b \cdot, a/b$

$I_7:$   
 $X \rightarrow b \cdot, \$$



$I_{47}:$   
 $X \rightarrow b \cdot, a/b/\$$

$I_8:$   
 $X \rightarrow aX \cdot, a/b$

$I_9:$   
 $X \rightarrow aX \cdot, \$$



$I_{89}:$   
 $X \rightarrow aX \cdot, a/b/\$$

# State Merging (cont.)

State	ACTION			GOTO	
	a	b	\$	S	X
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

LR(1)

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

LALR(1)  
Grammar:

- (0)  $S' \rightarrow S$
- (1)  $S \rightarrow XX$
- (2)  $X \rightarrow aX$
- (3)  $X \rightarrow b$

# State Merging (cont.)

State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	s3	s4			5
3	s3	s4			6
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		



LR(0)/SLR(1)

State	ACTION			GOTO	
	a	b	\$	S	X
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

LR(1)

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

LALR(1)

Grammar:

- (0)  $S' \rightarrow S$
- (1)  $S \rightarrow XX$
- (2)  $X \rightarrow aX$
- (3)  $X \rightarrow b$

# Merge Effects[合并效果]

---

- Merging states can introduce **conflicts**[引入归约-归约冲突]
  - **Cannot** introduce shift-reduce (*s-r*) conflicts
    - i.e., a *s-r* conflict cannot exist in a merged set unless the conflict was already present in one of the original LR(1) sets
  - **Can** introduce reduce-reduce (*r-r*) conflicts
    - LR was introduced to split the FOLLOW set on reduce action
    - Merging reverts the splitting
- **Detection of errors** may be delayed[推迟错误识别]
  - On error, LALR parsers will not perform shifts beyond an LR parser, but may perform more reductions before finding error
  - We'll see an example

# Merge Conflict: Shift-Reduce

---

- Shift-reduce conflicts are **not** introduced by merging
- Suppose

$S_{ij}$  contains:  $[A \rightarrow \alpha \cdot, a]$  reduce on input  $a$   
 $[B \rightarrow \beta \cdot a \gamma, b]$  shift on input  $a$

Formed by merging  $S_i$  and  $S_j$  [注:  $S_{ij}$ 并不一定只有这两个item]

- Because
  - Cores must be the same for  $S_i$  and  $S_j$ , and thus one of them must contain  $[A \rightarrow \alpha \cdot, a]$
  - and it must have an item  $[B \rightarrow \beta \cdot a \gamma, c]$  for some  $c$  [否则怎么同core?]
    - This state has the same shift/reduce conflict on  $a$ , i.e., the grammar was not LR(1)
  - Shift-reduce conflicts were already present in either  $S_i$  and  $S_j$  (or both) and not newly introduced by merging

# Merge Conflict: Reduce-Reduce

- Reduce-reduce conflicts can be introduced by merging

$$S' \rightarrow S$$

$$S \rightarrow aBc \mid bCc \mid aCd \mid bBd$$

$$B \rightarrow e$$

$$C \rightarrow e$$

$$\begin{aligned}I_0: \quad & S' \rightarrow \bullet S, \$ \\& S \rightarrow \bullet aBc, \$ \\& S \rightarrow \bullet bCc, \$ \\& S \rightarrow \bullet aCd, \$ \\& S \rightarrow \bullet bBd, \$\end{aligned}$$

$$I_1: \quad S' \rightarrow S \bullet, \$$$

$$\begin{aligned}I_2: \quad & S \rightarrow a \bullet Bc, \$ \\& S \rightarrow a \bullet Cd, \$ \\& B \rightarrow \bullet e, c \\& C \rightarrow \bullet e, d\end{aligned}$$

I<sub>69</sub>:

$$\begin{aligned}C \rightarrow e \cdot, c/d \\B \rightarrow e \cdot, d/c\end{aligned}$$

next token is c or d,  
reduce to B or C???

$$\begin{aligned}I_3: \quad & S \rightarrow b \bullet Cc, \$ \\& S \rightarrow b \bullet Bd, \$ \\& C \rightarrow \bullet e, c \\& B \rightarrow \bullet e, d\end{aligned}$$

$$I_4: \quad S \rightarrow aB \bullet c, \$$$

$$I_5: \quad S \rightarrow aC \bullet d, \$$$

$$\begin{aligned}I_6: \quad & B \rightarrow e \bullet, c \\& C \rightarrow e \bullet, d\end{aligned}$$

$$I_7: \quad S \rightarrow bC \bullet c, \$$$

Reduce to B when next token is d  
Reduce to C when next token is c

$$I_8: \quad S \rightarrow bB \bullet d, \$$$

$$\begin{aligned}I_9: \quad & B \rightarrow e \bullet, d \\& C \rightarrow e \bullet, c\end{aligned}$$

$$I_{10}: \quad S \rightarrow aBc \bullet, \$$$

$$I_{11}: \quad S \rightarrow aCd \bullet, \$$$

$$I_{12}: \quad S \rightarrow bCc \bullet, \$$$

$$I_{13}: \quad S \rightarrow bBd \bullet, \$$$

Reduce to B when next token is c

Reduce to C when next token is d

# Example: Error Delay

---

- (0)  $S' \rightarrow S$
- (1)  $S \rightarrow XX$       Input: **aab\$**
- (2)  $X \rightarrow aX$
- (3)  $X \rightarrow b$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

# Example: Error Delay

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

# Example: Error Delay

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_3$

symbol  $\rightarrow \$ a$

ab\$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

# Example: Error Delay

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_3$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_3S_3$

symbol  $\rightarrow \$ a a$

b\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

# Example: Error Delay

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_3$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_3S_3$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_3S_3S_4$

symbol  $\rightarrow \$ a a b$

\$

# Example: Error Delay

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_3$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_3S_3$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_3S_3S_4$

symbol  $\rightarrow \$ a a b$

\$

# Example: Error Delay (cont.)

- (0)  $S' \rightarrow S$
- (1)  $S \rightarrow XX$       Input: **aab\$**
- (2)  $X \rightarrow aX$
- (3)  $X \rightarrow b$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

state  $\rightarrow S_0$

(1)  $S \rightarrow XX$

Input: aab\$

symbol  $\rightarrow \$$

(2)  $X \rightarrow aX$

aab\$

(3)  $X \rightarrow b$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

State	ACTION			GOTO	
	a	b	\$	S	X
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_{36}S_{36}S_{47}$

symbol  $\rightarrow \$ a a b$

\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_{36}S_{36}S_{47}$

symbol  $\rightarrow \$ a a b$

\$

state  $\rightarrow S_0S_{36}S_{36}S_{89}$

symbol  $\rightarrow \$ a a X$

\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_{36}S_{36}S_{47}$

symbol  $\rightarrow \$ a a b$

\$

state  $\rightarrow S_0S_{36}S_{36}S_{89}$

symbol  $\rightarrow \$ a a X$

\$

state  $\rightarrow S_0S_{36}S_{89}$

symbol  $\rightarrow \$ a X$

\$

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_{36}S_{36}S_{47}$

symbol  $\rightarrow \$ a a b$

\$

state  $\rightarrow S_0S_{36}S_{36}S_{89}$

symbol  $\rightarrow \$ a a X$

\$

state  $\rightarrow S_0S_{36}S_{89}$

symbol  $\rightarrow \$ a X$

\$

state  $\rightarrow S_0S_2$

symbol  $\rightarrow \$ X$

\$

# Example: Error Delay (cont.)

(0)  $S' \rightarrow S$

(1)  $S \rightarrow XX$

(2)  $X \rightarrow aX$

(3)  $X \rightarrow b$

Input: aab\$

State	ACTION			GOTO	
	a	b	\$	s	x
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47			89
47	r3	r3	r3		
5			r1		
89	r2	r2	r2		

state  $\rightarrow S_0$

symbol  $\rightarrow \$$

aab\$

state  $\rightarrow S_0S_{36}$

symbol  $\rightarrow \$ a$

ab\$

state  $\rightarrow S_0S_{36}S_{36}$

symbol  $\rightarrow \$ a a$

b\$

state  $\rightarrow S_0S_{36}S_{36}S_{47}$

symbol  $\rightarrow \$ a a b$

\$

state  $\rightarrow S_0S_{36}S_{36}S_{89}$

symbol  $\rightarrow \$ a a X$

\$

state  $\rightarrow S_0S_{36}S_{89}$

symbol  $\rightarrow \$ a X$

\$

state  $\rightarrow S_0S_2$

symbol  $\rightarrow \$ X$

\$

# LALR Table Construction[解析表构建]

---

- LALR(1) parsing table is built from the configuration sets in the same way as LR(1)[同样方法构建的项目集]
  - The lookaheads determine where to place reduce actions
  - If there are no mergable states, the LALR(1) table will be identical to the LR(1) table and we gain nothing[退化为LR(1)]
  - Usually, there will be states that can be merged and the LALR table will thus have **fewer rows** than LR
- LALR(1) table have the same #states (rows) with SLR(1) and LR(0), but have fewer reduce actions[同等数目的状态,但更少的归约动作]
  - Some reductions are not valid if we are more precise about the lookahead
  - Some conflicts in SLR(1) and LR(0) are avoided by LALR(1)
  - For C language: SLR/LALR - 100s states, LR - 1000s states

# LALR Table Construction (cont.)

---

- Brute force[暴力方式]
  - Construct LR(1) states, then merge states with same core
  - If no conflicts, you have a LALR parser
  - **Inefficient**: building LR(1) items are expensive in time and space
    - We need a better solution
- Efficient way[高效方式]
  - Avoid initial construction of LR(1) states
  - Merge states on-the-fly (step-by-step merging)
    - States are created as in LR(1)
    - On state creation, immediately merge if there is an opportunity

# LALR(1) Grammars

---

- For a grammar, if the LALR(1) parse table has no conflicts, then we say the grammar is LALR(1)
  - No formal definition of a set of rules
- LALR(1) is a subset of LR(1) and a superset of SLR(1)
  - A SLR(1) grammar is definitely LALR(1)[LALR归约更精细了]
  - A LR(1) grammar may or may not be LALR(1)[LALR合并了状态]
    - Depends on whether merging introduces conflicts
  - A non-SLR(1) grammar may be LALR(1)[LALR能解决SLR冲突]
    - Depends on whether the more precise lookaheads resolve the SLR(1) conflicts
- LALR(1) reaches a good balance between the **lookahead power** and the **table size**
  - Most used variant of the LR family

# LALR Summary[小结]

---

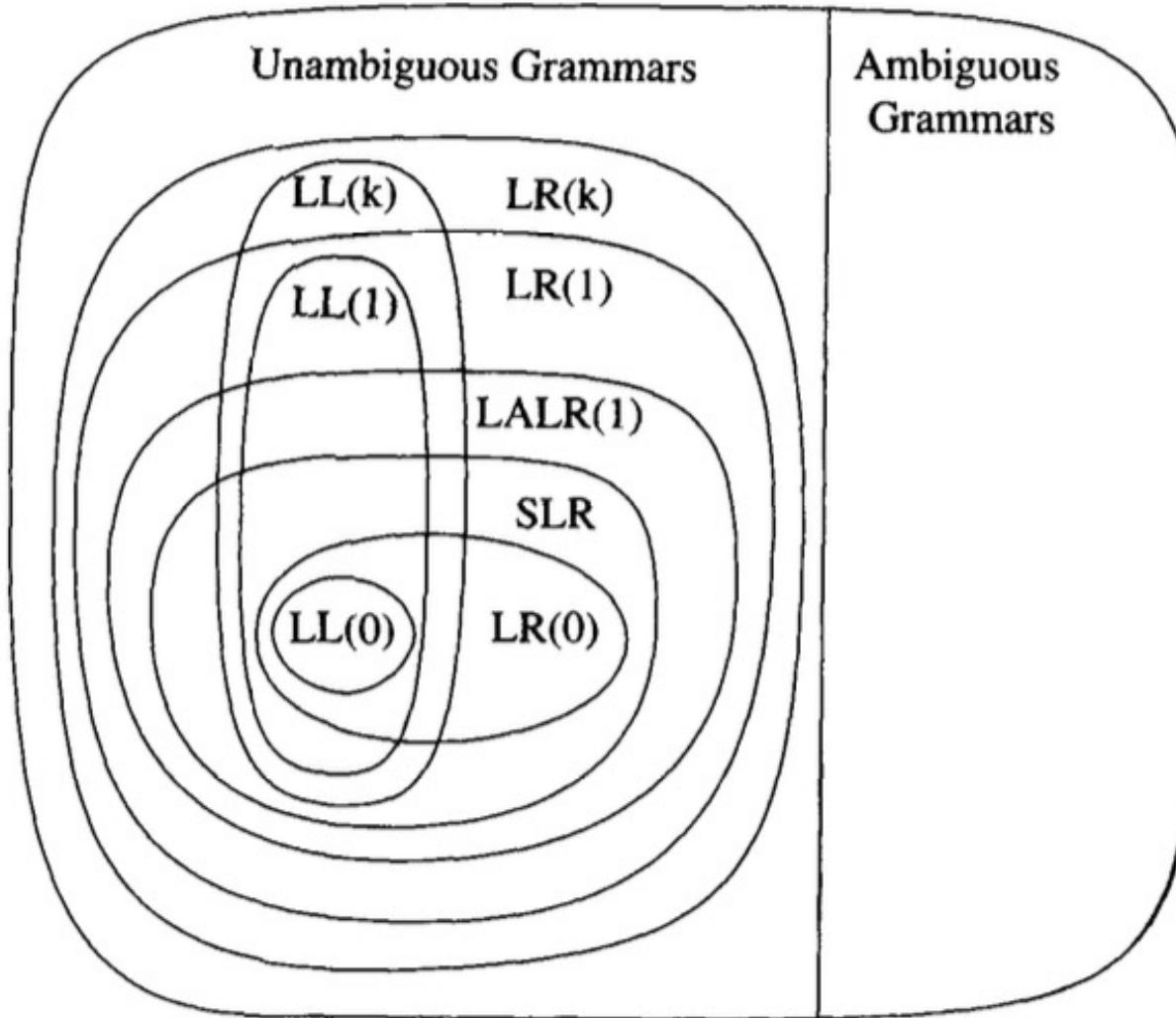
- LALR(1)是LR(1)和SLR(1)的平衡
  - 文法范围: LR > LALR > SLR
  - 状态数目: LR > LALR = SLR
- 假如一个文法G是LR而非SLR, 可能是LALR
  - 非SLR: SLR产生了冲突 (依靠FOLLOW集进行归约不够精确)
    - 是LR: 而LR通过精确的lookahead解决了冲突
  - 可能是LALR: LALR对LR进行相似状态合并
    - 若合并后出现了冲突 --> 不是LALR文法
    - 若合并后没有冲突 --> 是LALR文法
      - LALR可以解析文法G, 也即解决了SLR原有的冲突
      - 实际上LALR的状态数与SLR相同, 但归约动作减少了 (也即, 对SLR解析表而言, 多个移进/归约动作的单元格中的归约被消除了)
    - 如果没有相似状态, 则LALR=LR
- 假如一个文法G是SLR
  - 那么G一定也是LR和LALR文法
  - LR的FOLLOW集细分是不必要的, 因此LALR合并回了SLR

# LL vs. LR Parsing (LL < LR)

---

- LL( $k$ ) parser, each expansion  $A \rightarrow \alpha$  is decided based on
  - Current non-terminal at the top of the stack[依赖LHS]
    - Which LHS to produce
  - $k$  terminals of lookahead at beginning of RHS[RHS的一点展望]
    - Must **guess** which RHS by peeking at **first few terminals** of RHS
  - 选择依据： LHS + RHS的 $k$ 个符号（有限信息）
- LR( $k$ ) parser, each production  $A \rightarrow \alpha \cdot$  is decided based on
  - RHS at the top of the stack[依赖RHS]
    - Can **postpone** choice of RHS until **entire RHS** is seen
    - Common left factor is OK – waits until entire RHS is seen anyway
    - Left recursion is OK – does not impede forming RHS for reduction
  - $k$  terminals of lookahead beyond RHS[超越RHS]
    - Can decide on RHS after looking at entire RHS plus lookahead
  - 选择依据： 整个RHS + LHS后的 $k$ 个符号（充足信息）

# Hierarchy of Grammars[文法层级]



# 总结: 语法分析 (1)

---

- 语法分析(Syntax analysis)是编译的第二个阶段
  - 输入: 词法分析产生的token序列
  - 输出: 分析树(parse tree)或抽象语法树(AST)
- 语法指定(Syntax specification)
  - 词法分析使用的RE/FA表达能力不够(e.g., 嵌套结构)
  - 需要使用文法(grammar), 尤其是上下文无关文法(context-free grammar, CFG)
- 文法形式化定义:  $\{T, N, s, \sigma\}$ 
  - $T$ : terminal symbols[终结符] = 词法分析的token, 分析树的叶子节点
  - $N$ : non-terminal symbols[非终结符], 分析树的内部节点
  - $s$ : start symbol[开始符号]
  - $\sigma$ : set of productions[产生式], 形式: LHS  $\rightarrow$  RHS

# 总结: 语法分析 (2)

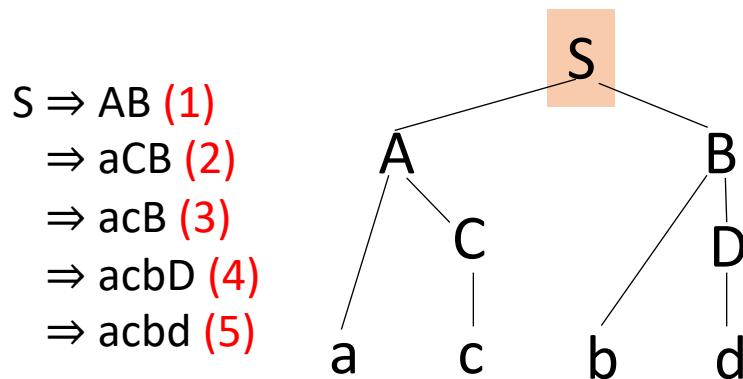
---

- **推导(Derivation)**
  - 对产生式的若干次使用 (从LHS到RHS)
    - 从文法开始符号到输入串(input string)
- **归约(Reduce)**
  - 推导的逆过程(从RHS到LHS)
    - 从输入串(input string)到开始符号
- **分析树(Parse tree)**
  - 是推导的图形化表示, 略去了推导中产生式的使用顺序
- **歧义文法(Ambiguous grammar)**
  - 某个句子对应多个(最左或最右)分析树
  - 通过指定优先级(precedence)和结合性(associativity)来改写文法以消除歧义

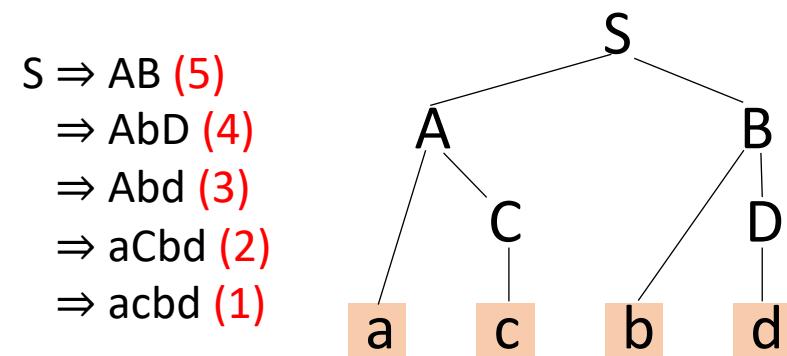
# 总结: 语法分析 (3)

- 语法分析(或解析)就是处理给定文法的输入句子，构建一个以分析树或抽象语法树表示的推导
  - 自顶向下(Top-down): 从根节点扩展到叶子节点，每步考虑
    - 替换哪个非终结符？
    - 使用哪个产生式来替换？
  - 自底向上(Bottom-up): 从叶子节点回到根节点
    - 消耗输入token还是归约？
    - 使用哪个产生式来归约？

Top-down (leftmost derivation)



Bottom-up (reverse of rightmost derivation)



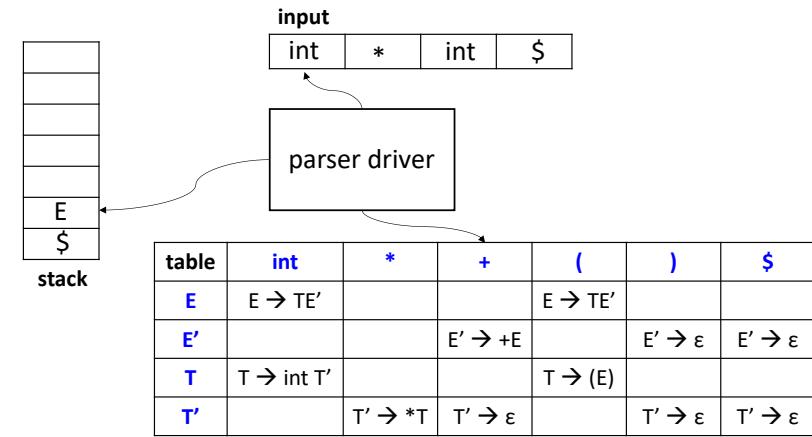
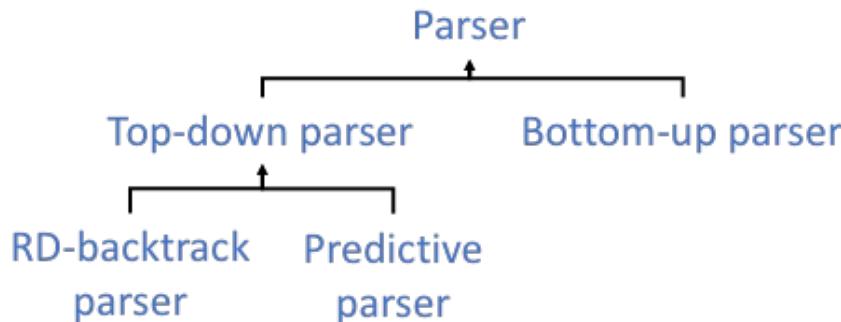
# 总结: 语法分析 (4)

## • Top-down 分析

- 递归下降分析(Recursive descent): 试错->回溯(backtracking)
  - 消除左递归(Left recursion)
- 预测分析(Predictive): 预测, 无需回溯
  - 消除左递归, 提取左共因子(Left factoring)

## • 表驱动的LL(1)分析器

- 四部分: input buffer, stack, parse table, parser driver
- 基于<stack top, current token>来采取操作(expand or match)
- 解析表行为文法的非终结符、列为文法的终结符号及\$
  - 单元格存放一个产生式或空
  - 表格是借助FIRST和FOLLOW集来构建



# 总结: 语法分析 (5)

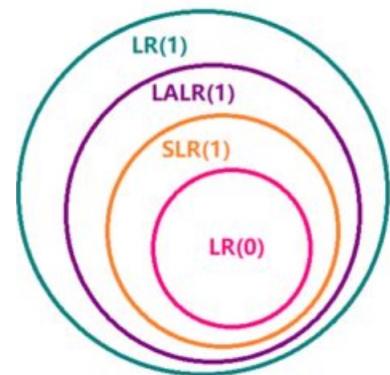
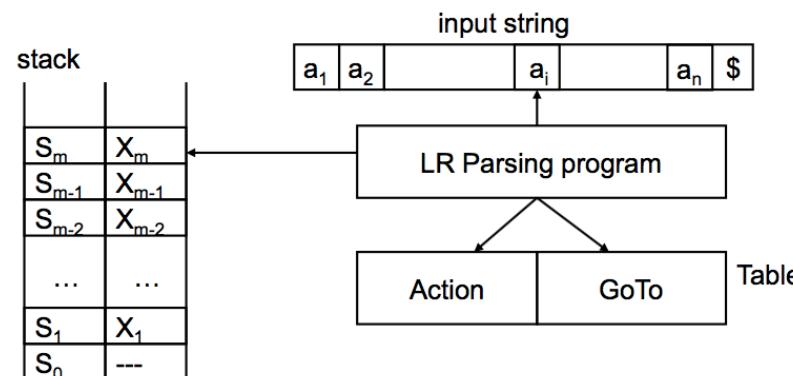
- Bottom-up分析

- 主要有移进(Shift)和归约(Reduce)两个动作
- 实现上主要是LR类型分析器
  - 表格驱动，高效

- 表驱动的LR分析器

- 四部分: input buffer, stack, parse table, parser driver
- 基于栈顶来采取操作(shift or reduce)
  - 栈保存状态序列和每个状态关联的文法符号
- 解析表包含Action和Goto两个子表
  - 表格是通过识别文法的可能项目集及转换(i.e., DFA)
  - $\text{LR}(0) \rightarrow \text{SLR}(1) \rightarrow \text{LR}(1) \rightarrow \text{LALR}(1)$

State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	s3	s4			5
3	s3	s4			6
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		





# Compilation Principle 编译原理

---

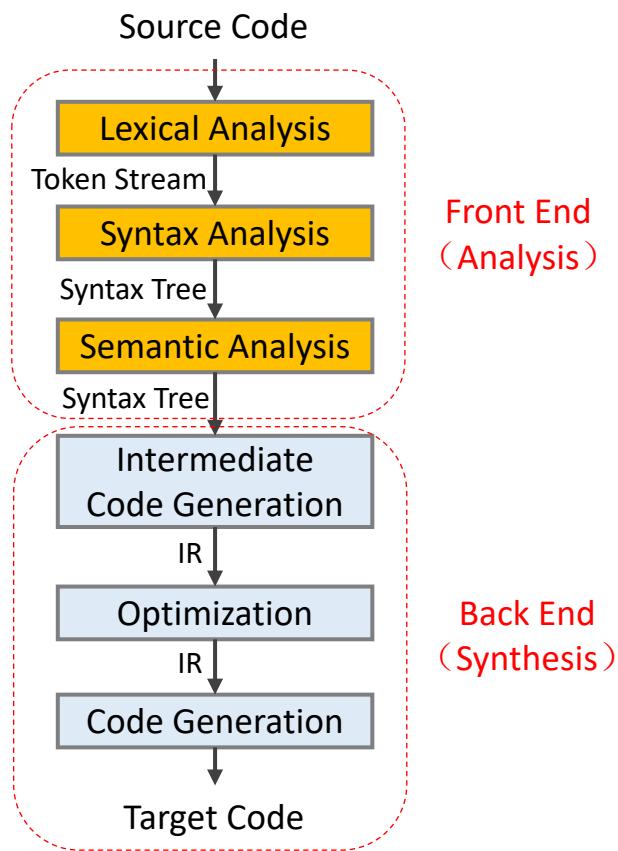
## 第14讲：语义分析(1)

张献伟

[xianweiz.github.io](https://xianweiz.github.io)

DCS290, 4/11/2023

# Compilation Phases[编译阶段]



# Compilation Phases (cont.)

---

- Lexical analysis[词法分析]
  - Source code → tokens
  - Detects inputs with illegal tokens
  - Is the input program **lexically** well-formed?
- Syntax analysis[语法分析]
  - Tokens → parse tree or abstract syntax tree (AST)
  - Detects inputs with incorrect structure
  - Is the input program **syntactically** well-formed?
- Semantic analysis[语义分析]
  - AST → (modified) AST + symbol table
  - Detects semantic errors (errors in meaning)
  - Does the input program has a well-defined **meaning**?

# Compilation Phases (cont.)

---

- Lexical analysis[词法分析]
  - Source code → tokens
  - Detects inputs with illegal tokens
  - Is the input program **lexically** well-formed?
- Syntax analysis[语法分析]
  - Tokens → parse tree or abstract syntax tree (AST)
  - Detects inputs with incorrect structure
  - Is the input program **syntactically** well-formed?
- Semantic analysis[语义分析]
  - AST → (modified) AST + symbol table
  - Detects semantic errors (errors in meaning)
  - Does the input program has a well-defined **meaning**?