



中山大學
SUN YAT-SEN UNIVERSITY

计算机学院 (软件学院)

SCHOOL OF COMPUTER SCIENCE AND ENGINEERING

Compilation Principle 编译原理

第20讲：中间代码(2)

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Review Questions

- Input and output of code generation?

Input: AST + symbol table; output: IR

- What is IR?

Intermediate Representation. A machine- and language-independent version of the original source code.

- Why do we use IR?

Clean separation of front-/back-end; easy to optimize and extend

- What is three-address code (TAC)?

A type of IR, with at most three operands. (High-level assembly)

- TAC of $x + y * z + 5$?

$t_1 = y * z; t_2 = x + t_1; t_3 = t_2 + 5;$

Three-Address Code[三地址码]

- High-level assembly where each operation has **at most three** operands. Generic form is $X = Y \text{ op } Z$ [最多3个操作数]
 - where X, Y, Z can be variables, constants, or compiler-generated temporaries holding intermediate values
- Characteristics[特性]
 - Assembly code for an 'abstract machine'
 - Long expressions are converted to multiple instructions
 - Control flow statements are converted to jumps[控制流->跳转]
 - Machine independent
 - Operations are generic (not tailored to any specific machine)
 - Function calls represented as generic call nodes
 - Uses symbolic names rather than register names (actual locations of symbols are yet to be determined)
- Design goal: for easier machine-independent optimization

Three-Address Statements

- Assignment statement[二元赋值]

$x = y \text{ op } z$

where op is an arithmetic or logical operation (binary operation)

- Assignment statement[一元赋值]

$x = \text{op } y$

where op is an unary operation such as -, not, shift

- Copy statement[拷贝]

$x = y$

- Unconditional jump statement[无条件跳转]

`goto L`

where L is label

Three-Address Statements (cont.)

- Conditional jump statement[条件跳转]

if (x relop y) goto L

where relop is a relational operator such as =, ≠, >, <

- Procedural call statement[过程调用]: may have too many addr

param $x_1, \dots, \text{param } x_n, \text{ call } F_y, n$

As an example, $\text{foo}(x_1, x_2, x_3)$ is translated to

param x_1

param x_2

param x_3

call foo, 3

- Procedural call return statement[过程调用返回]

return y

where y is the return value (if applicable)

Three-Address Statements (cont.)

- Indexed assignment statement[索引]

$x = y[i]$

or

$y[i] = x$

where x is a scalar variable and y is an array variable

- Address and pointer operation statement[地址和指针]

$x = \& y$; a pointer x is set to address of y

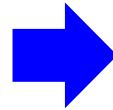
$y = * x$; y is set to the value of location
; pointed to by pointer x

$*y = x$; location pointed to by y is assigned x

Example: TAC

```
i = 1
do {
  a[i] = x * 5;
  i ++;
} while (i <= 10);
```

Source program



```
i = 1
L: t1 = x * 5
  t2 = &a
  t3 = sizeof(int)
  t4 = t3 * i
  t5 = t2 + t4
  *t5 = t1
  i = i + 1
  if i <= 10 goto L
```

a[i]

Three-address code

Example: TAC (cont.)

```
i = 1
do {
    a[i] = x * 5;
    i++;
} while (i <= 10);
```

```
@i = dso_local global i32 1, align 4
@x = dso_local global i32 2, align 4
@a = dso_local global [10 x i32] zeroinitializer, align 4
```

```
; Function Attrs: noinline nounwind optnone
define dso_local i32 @main() #0 {
    %1 = alloca i32, align 4
    store i32 0, i32* %1, align 4
    br label %2
```

```
2:                                     ; preds = %7, %0
    %3 = load i32, i32* @x, align 4     // %3 = x
    %4 = mul nsw i32 %3, 5              // %4 = %3 x 5
    store i32 %4, i32* @telementptr inbounds ([10 x i32], [10 x i32]* @a, i64 0, i64 1), align 4
    %5 = load i32, i32* @i, align 4    // %5 = i
    %6 = add nsw i32 %5, 1              // %6 = %5 + 1
    store i32 %6, i32* @i, align 4     // i = %6
    br label %7
```

```
7:                                     ; preds = %2
    %8 = load i32, i32* @i, align 4    // %8 = i
    %9 = icmp sle i32 %8, 10           // %9 = (i <= 10)
    br i1 %9, label %2, label %10     // T: %2, F: %10
```

```
10:                                    ; preds = %7
    ret i32 0
}
```

```
1 int i = 1, x = 2;
2 int a[10];
3
4 int main(){
5
6     do {
7         a[1] = x * 5;
8         i++;
9     } while (i <= 10);
10
11 return 0;
12 }
```

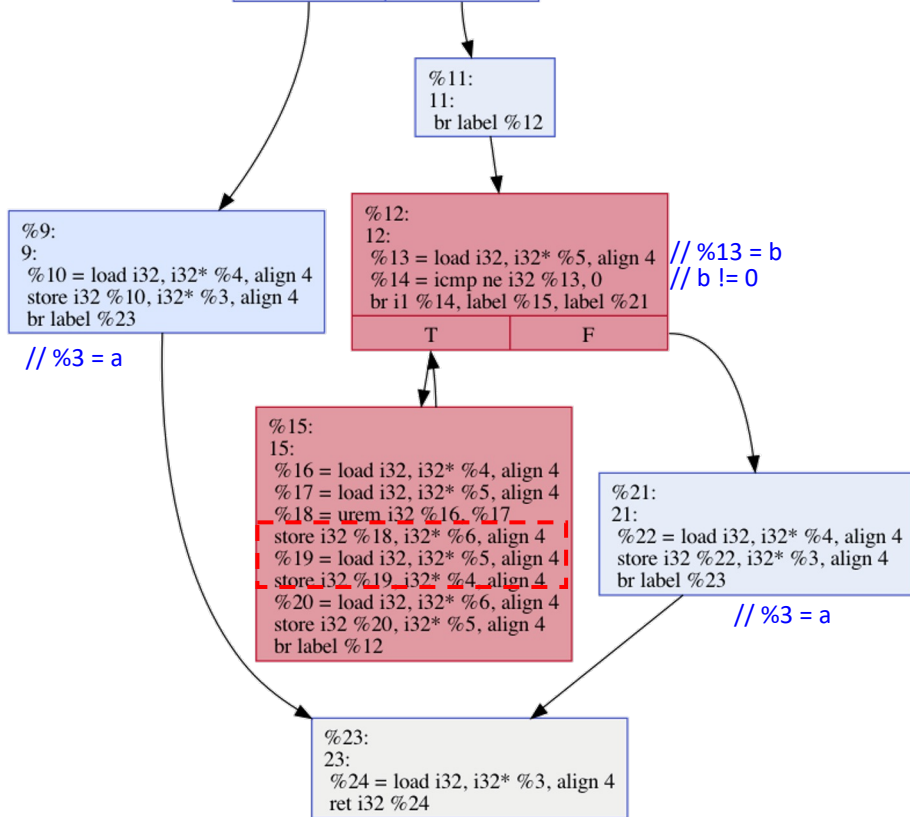


Example: IR and SSA

\$clang -emit-llvm -S gcd.c

```

%2:
%3 = alloca i32, align 4 // a
%4 = alloca i32, align 4 // b
%5 = alloca i32, align 4
%6 = alloca i32, align 4 // %4 = a
store i32 %0, i32* %4, align 4 // %5 = b
store i32 %1, i32* %5, align 4 // %7 = b
%7 = load i32, i32* %5, align 4 // b == 0?
%8 = icmp eq i32 %7, 0 // Y: %9; N: %11
br i1 %8, label %9, label %11
    
```



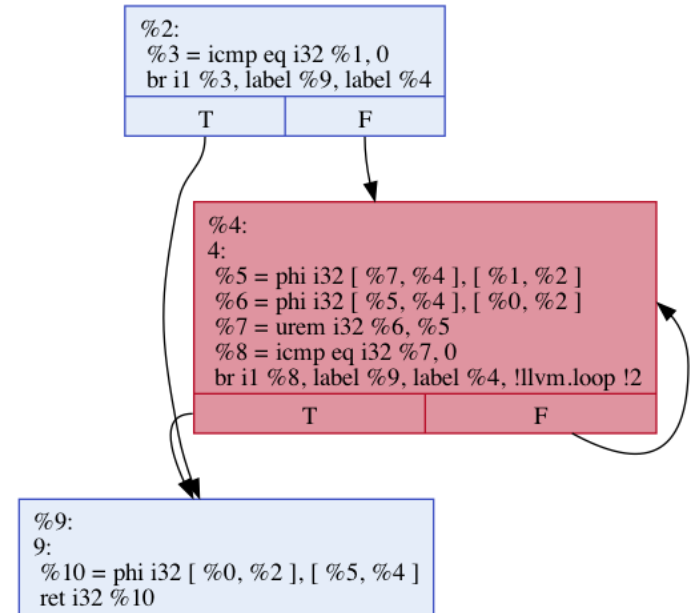
CFG for 'gcd' function

Load-and-store approach (not SSA)

```

1 unsigned gcd(unsigned a, unsigned b) {
2   if (b == 0)
3     return a;
4   while (b != 0) {
5     unsigned t = a % b;
6     a = b;
7     b = t;
8   }
9   return a;
10 }
    
```

\$clang -emit-llvm -S -O1 gcd.c

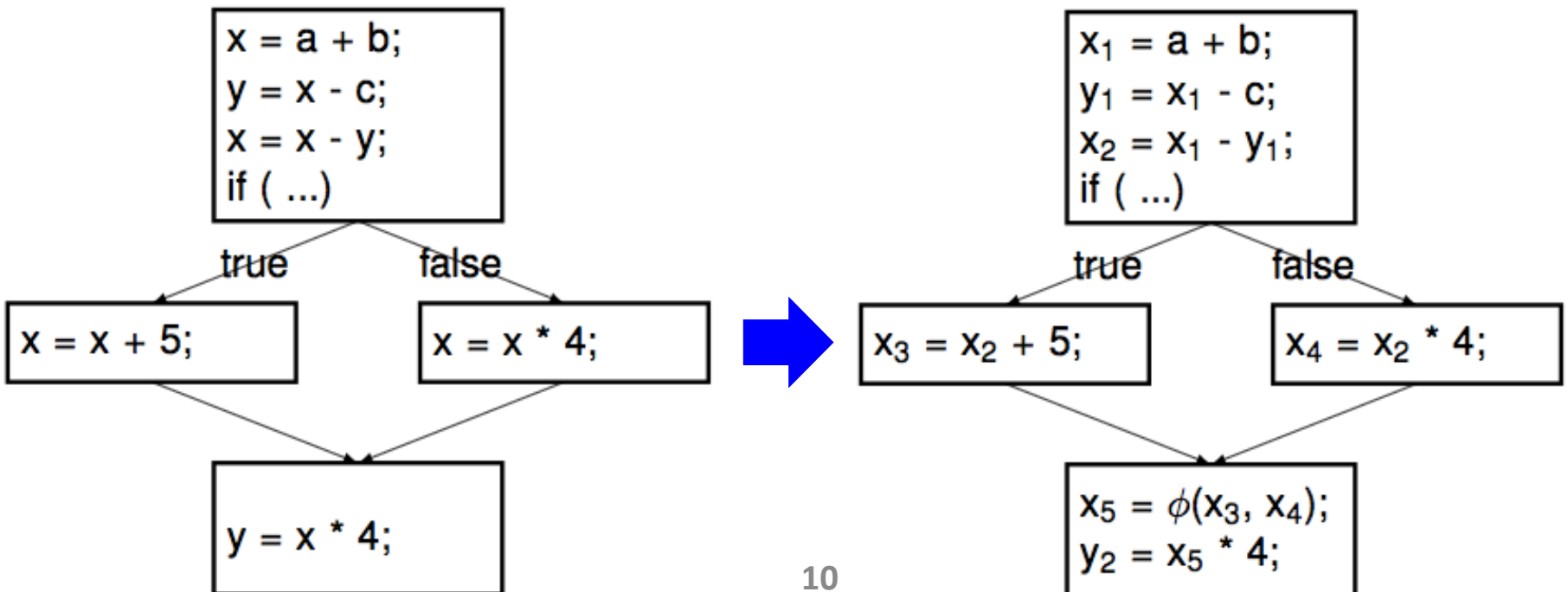


CFG for 'gcd' function

Phi approach (SSA)

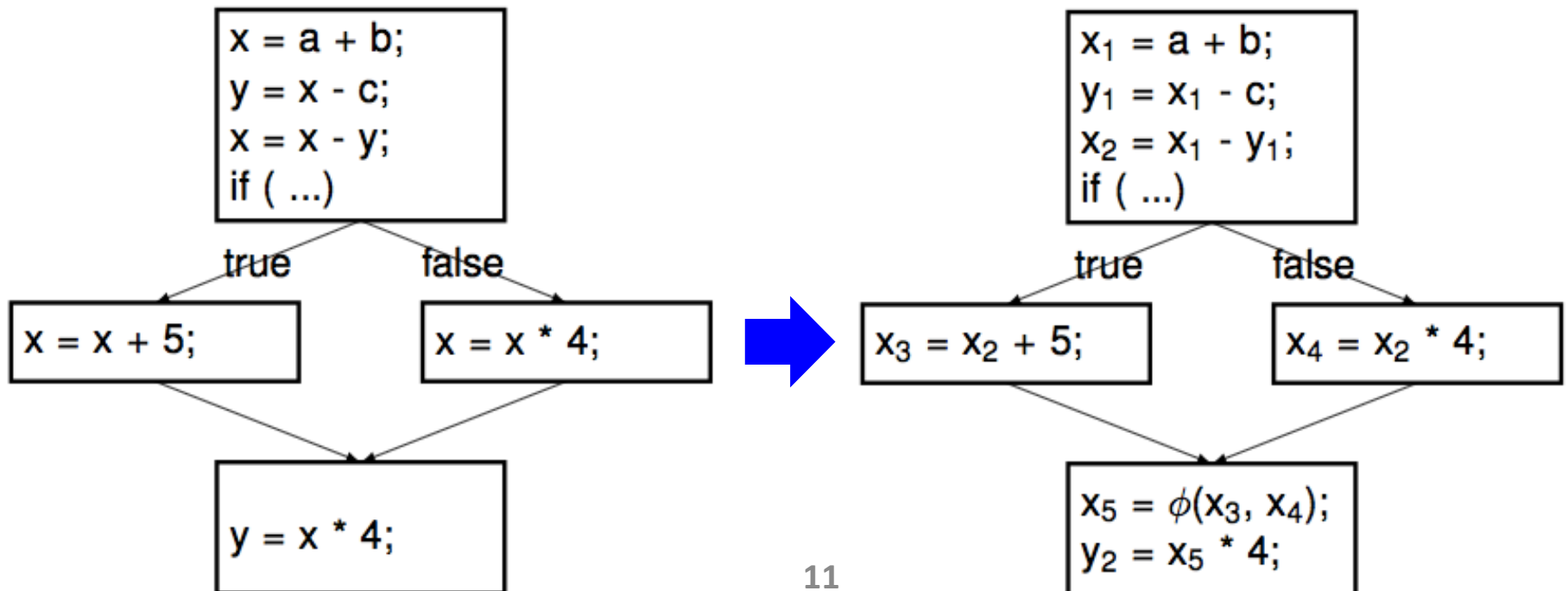
Single Static Assignment[静态单赋值]

- Every variable is assigned to exactly once statically[仅一次]
 - Give variable a different version name on every assignment
 - e.g. $x \rightarrow x_1, x_2, \dots, x_5$ for each static assignment of x
 - Now value of each variable guaranteed not to change
 - On a control flow merge, ϕ -function combines two versions
 - e.g. $x_5 = \phi(x_3, x_4)$: means x_5 is either x_3 or x_4



Benefits of SSA

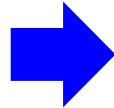
- SSA is an IR that facilitates certain code optimizations
 - SSA tells you when an optimization **shouldn't** happen
 - Suppose compiler performs CSE on previous example:
 - Without SSA, (incorrectly) tempted to eliminate second $x * 4$
 - $x = x * 4; y = x * 4; \rightarrow x = x * 4; y = x;$
 - With SSA, $x_2 * 4$ and $x_5 * 4$ are clearly different values



Benefits of SSA (cont.)

- SSA is an IR that facilitates certain code optimizations
 - SSA tells you when an optimization **should** happen
 - Suppose compiler performs dead code elimination (DCE): (DCE removes code that computes dead values)

```
x = a + b;  
x = c - d;  
y = x * b;
```



```
x1 = a + b;  
x2 = c - d;  
y1 = x2 * b;
```

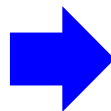
- Without SSA, not very clear whether there are dead values
- With SSA, x_1 is never used and clearly a dead value
- Why does SSA work so well with compiler optimizations?
 - SSA makes flow of values explicit in the IR[数据流显现]
 - Without SSA, need a separate dataflow graph
 - Will discuss more in **Compiler Optimization** section

LLVM: SSA and Phi



- All LLVM instructions are represented in the Static Single Assignment (SSA) form
 - Affordable to the design of simpler algorithms for existing optimizations and has facilitated the development of new ones
- The ‘phi’ instruction is used to implement the ϕ node in the SSA graph representing the function
 - `<result> = phi [fast-math-flags] <ty> [<val0>, <label0>], ...`
 - At runtime, the ‘phi’ instruction logically takes on the value specified by the pair corresponding to the predecessor basic block that executed just prior to the current block

```
a = 1;  
if (v < 10)  
    a = 2;  
b = a;
```

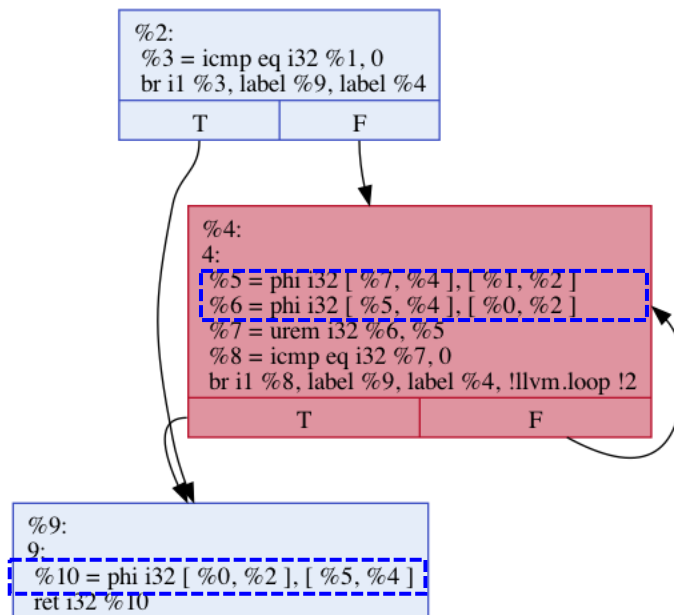


```
a1 = 1;  
if (v < 10)  
    a2 = 2;  
b = PHI(a1, a2);
```

Example

- Registers
 - Unlimited #virtual registers
 - Each is written only once
 - %0: *a*, %1: *b*
- Phi instructions
 - %5 = phi i32 [%7, %4], [%1, %2]
 - *b* is from before-while or while
 - %6 = phi i32 [%5, %4], [%0, %2]
 - *a* is either before-while or while
 - %10 = phi i32 [%0, %2], [%5, %4]
 - *a* is either before-while or while
- Phi restrictions
 - Must be the 1st insts of a BB
 - The 1st BB cannot begin with phi
 - Has no previously executed block

\$clang -emit-llvm -S -O1 gcd.c

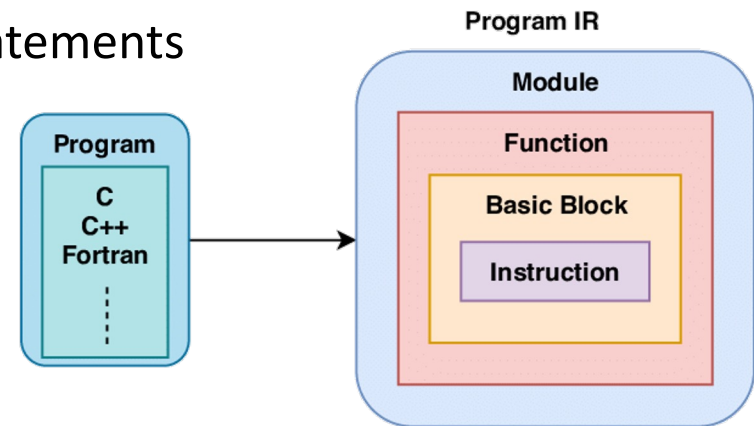


CFG for 'gcd' function
Phi approach (SSA)

```
1 unsigned gcd(unsigned a, unsigned b) {
2   if (b == 0)
3     return a;
4   while (b != 0) {
5     unsigned t = a % b;
6     a = b;
7     b = t;
8   }
9   return a;
10 }
```

IR Generation Overview[代码生成]

- Program code is a collection of functions
 - By now, all functions are listed in symbol table
- Goal is to generate code for each function in that list
- Generating code for a function involves two steps:
 - Processing variable definitions[变量定义]
 - Involves laying out variables in memory
 - Processing statements[语句]
 - Involves generating instructions for statements
 - Assignment[赋值]
 - Array references[数组引用]
 - Boolean expressions[布尔表达式]
 - Control-flow statements[控制流语句]
 - ...



- We will start with processing variable definitions

Processing Variable Definitions[变量定义]

- To lay out a variable, both **location** and **width** are needed
 - Location: where variable is located in memory
 - Width: how much space variable takes up in memory
- Attributes for variable definition:
 - **T V** e.g. `int x;`
 - **T**: non-terminal for type name
 - **T.type**: type (int, float, ...)
 - **T.width**: width of type in bytes (e.g. 4 for int)
 - **V**: non-terminal for variable name
 - **V.type**: type (int, float, ...)
 - **V.width**: width of variable according to type
 - **V.offset**: offset of variable in memory
 - But offset from what...?

Example: LLVM

```
1 double x;  
2  
3 void foo() {  
4     char a;  
5     int b = 0;  
6     long long c;  
7     int d;  
8 }
```

```
@x = dso_local global double 0.000000e+00, align 8
```

```
; Function Attrs: noinline nounwind optnone  
define dso_local void @foo() #0 {  
    %1 = alloca i8, align 1  
    %2 = alloca i32, align 4  
    %3 = alloca i64, align 8  
    %4 = alloca i32, align 4  
    store i32 0, i32* %2, align 4  
    ret void  
}
```



```
auto addr = Builder.CreateAlloca(...);  
Builder.CreateStore(..., addr);
```

Calculate Variable Location from Offset

- Naive method: reserve a big memory section for all data
 - Size data section to be large enough to contain all variables
 - Location = var offset + base of data section
- Naive method wastes a lot of memory
 - Vars with limited scope need to live only briefly in memory
 - E.g. function variables need to last only for duration of call
- **Solution:** allocate memory briefly for each scope[域内]
 - Allocate when entering scope, free when exiting scope
 - Variables in the same scope are allocated / freed together
 - Location = var offset + base of scope memory section
 - Will discuss more later in **Runtime Management**

Storage Layout of Variables in a Function

- When there are multiple variables defined in a function,
 - Compiler lays out variables in memory sequentially
 - Current offset used to place variable x in memory

- $\text{address}(x) \leftarrow \text{offset}$
- $\text{offset} += \text{sizeof}(x.\text{type})$

```
define dso_local void @foo() #0 {  
    %1 = alloca i32, align 4  
    %2 = alloca i32, align 4  
    %3 = alloca i64, align 8  
    %4 = alloca i32, align 4  
    ret void  
}
```

```
void foo() {  
    int a;  
    int b;  
    long long c;  
    int d;  
}
```

Address

0x0000

a

Offset = 0

Addr(a) \leftarrow 0

0x0004

b

Offset = 4

Addr(b) \leftarrow 4

0x0008

c

Offset = 8

Addr(c) \leftarrow 8

0x000c

c

0x0010

d

Offset = 16

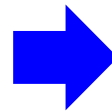
Addr(d) \leftarrow 16

Offset = 20

More about Storage Layout

- Allocation alignment[对齐]
 - Enforce $\text{addr}(x) \% \text{sizeof}(x.\text{type}) == 0$
 - Most machine architectures are designed such that computation is most efficient at sizeof(x.type) boundaries
 - E.g. most machines are designed to load integer values at integer word boundaries
 - If not on word boundary, need to load two words and shift & concatenate → inefficient

```
void foo() {  
    char a;      // addr(a) = 0  
    int b;       // addr(b) = 1  
    int c;       // addr(c) = 5  
    long long d; // addr(d) = 9  
}
```



```
void foo() {  
    char a;      // addr(a) = 0  
    int b;       // addr(b) = 4  
    int c;       // addr(c) = 8  
    long long d; // addr(d) = 16  
}
```

Type Expressions[类型表达式]

- A **type expression** is either a basic type or is formed by applying an operator called a type constructor[类型构造符] to a type expression
 - Basic type: *integer, float, char, boolean, void*
 - Array: *array(l, T)* is a type expression, if *T* is
 - $\text{int}[3] \leftrightarrow \text{array}(3, \text{int})$
 - $\text{int}[2][3] \leftrightarrow \text{array}(2, \text{array}(3, \text{int}))$
 - Pointer: *pointer(T)* is a type expression, if *T* is
 - $\text{int} * \text{val} \leftrightarrow \text{pointer}(\text{int})$

```
P -> D
D -> T id; D1 | ε
T -> B C | *T1
B -> int | real
C -> [num]C1 | ε
```

CodeGen: Variable Definitions

- Translating variable definitions

- *enter(name, type, offset)*

- Save the type and relative address in the symbol-table entry for the name

① $P \rightarrow \{ \text{offset} = 0 \} D$

② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset});$
 $\text{offset} = \text{offset} + T.\text{width}; \} D_1$

③ $D \rightarrow \epsilon$

④ $T \rightarrow B \{ t = B.\text{type}; w = B.\text{width}; \}$

$C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width}; \}$

⑤ $T \rightarrow *T_1 \{ T.\text{type} = \text{pointer}(T_1.\text{type}); T.\text{width} = 4; \}$

⑥ $B \rightarrow \text{int} \{ B.\text{type} = \text{int}; B.\text{width} = 4; \}$

⑦ $B \rightarrow \text{real} \{ B.\text{type} = \text{real}; B.\text{width} = 8; \}$

⑧ $C \rightarrow \epsilon \{ C.\text{type} = t; C.\text{width} = w; \}$

⑨ $C \rightarrow [\text{num}]C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type});$
 $C.\text{width} = \text{num.val} * C_1.\text{width}; \}$

- Examples:

- *real x; int i;*

- *int[2][3];*

- *type, width*

- Syn attributes

- *t, w*

- Vars to pass type and width from B node to the node for $C \rightarrow \epsilon$

- *offset*

- The next relative address

Example

- Input: `real x; int i;`

- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset});$
 $\text{offset} = \text{offset} + T.\text{width}; \} D_1$
- ③ $D \rightarrow \epsilon$
- ④ $T \rightarrow B \{ t = B.\text{type}; w = B.\text{width}; \}$
 $C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width}; \}$
- ⑤ $T \rightarrow *T_1 \{ T.\text{type} = \text{pointer}(T_1.\text{type}); T.\text{width} = 4; \}$
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 $C.\text{width} = \text{num.val} * C_1.\text{width}; \}$

Example

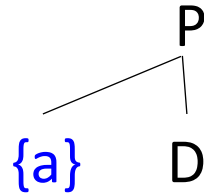
- Input: `real x; int i;`



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
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Example

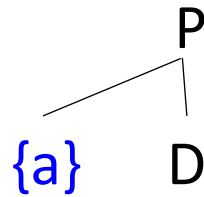
- Input: **real x; int i;**



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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Example

- Input: real x; int i;



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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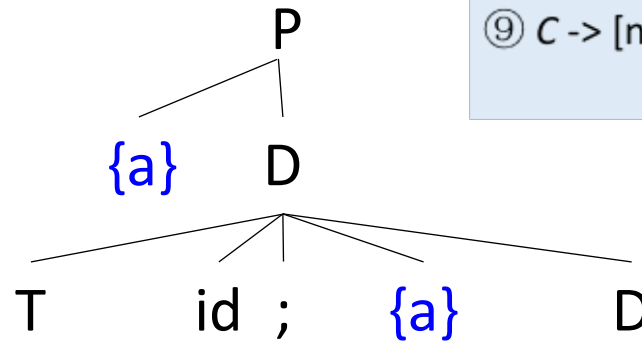
offset = 0

Example

- Input: real x; int i;



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
- ③ $D \rightarrow \epsilon$
- ④ $T \rightarrow B \{ t = B.\text{type}; w = B.\text{width}; \} C \{ T.\text{type} = C.\text{type}; T.\text{width} = C.\text{width}; \}$
- ⑤ $T \rightarrow *T_1 \{ T.\text{type} = \text{pointer}(T_1.\text{type}); T.\text{width} = 4; \}$
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- ⑦ $B \rightarrow \text{real} \{ B.\text{type} = \text{real}; B.\text{width} = 8; \}$
- ⑧ $C \rightarrow \epsilon \{ C.\text{type} = t; C.\text{width} = w; \}$
- ⑨ $C \rightarrow [\text{num}]C_1 \{ C.\text{type} = \text{array}(\text{num.val}, C_1.\text{type}); C.\text{width} = \text{num.val} * C_1.\text{width}; \}$



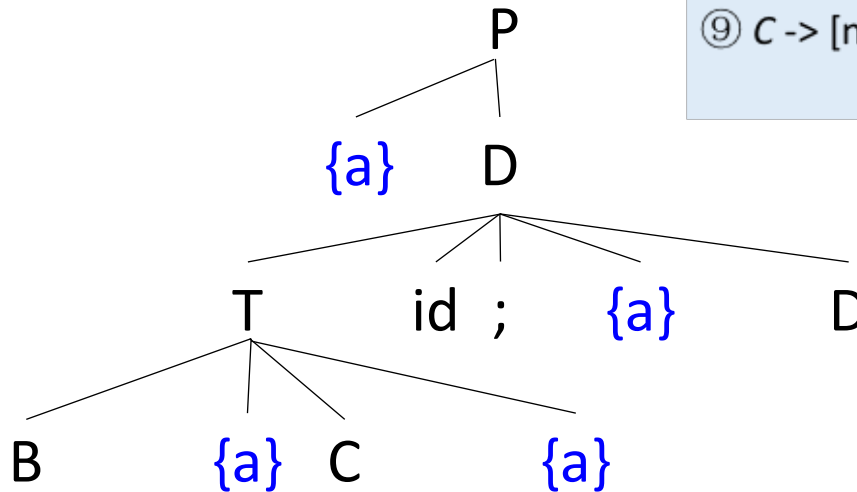
offset = 0

Example

- Input: real x; int i;



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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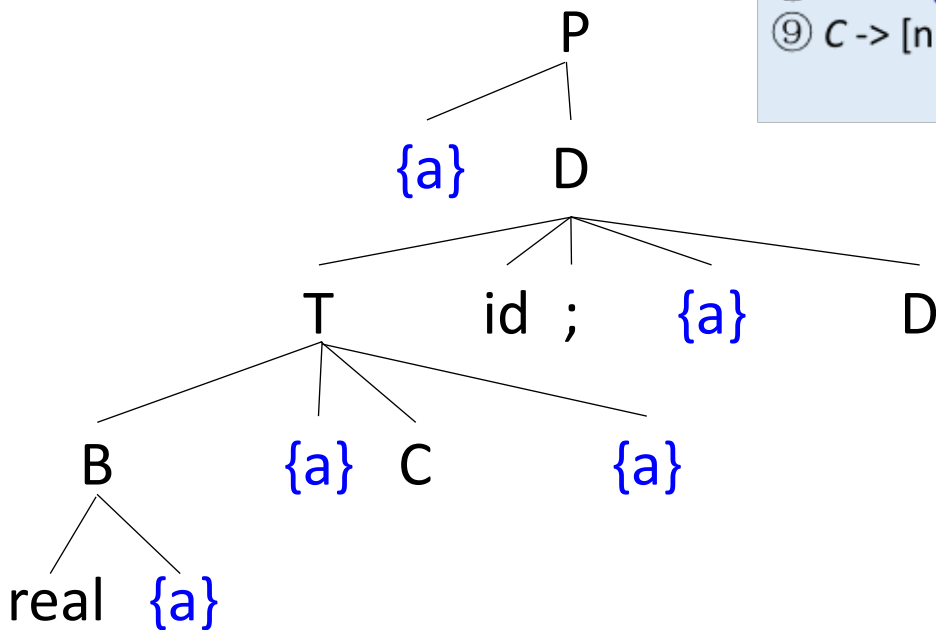
offset = 0

Example

- Input: real x; int i;



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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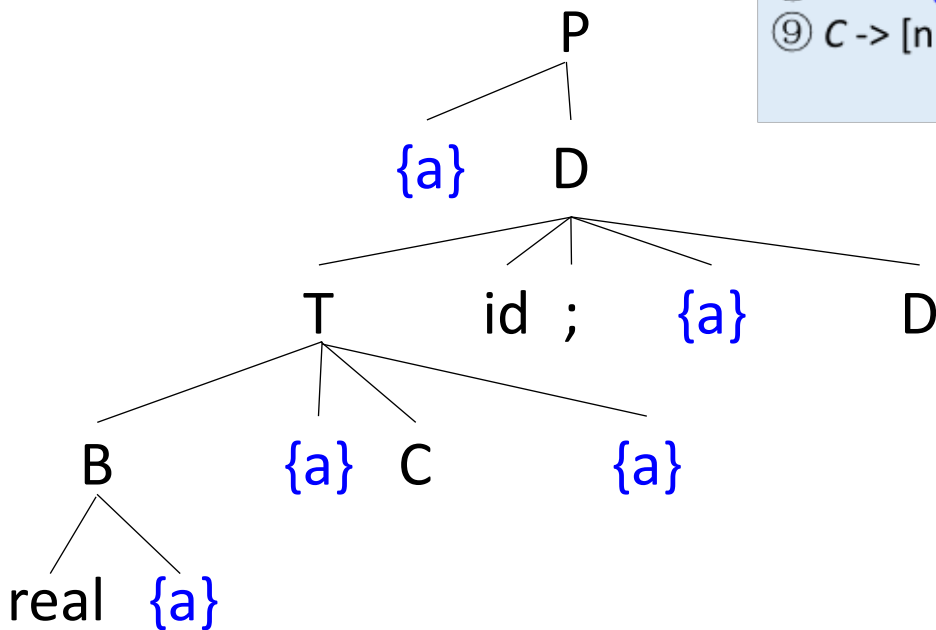


offset = 0

Example

- Input: **real x; int i;**
 ↑ ↑

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- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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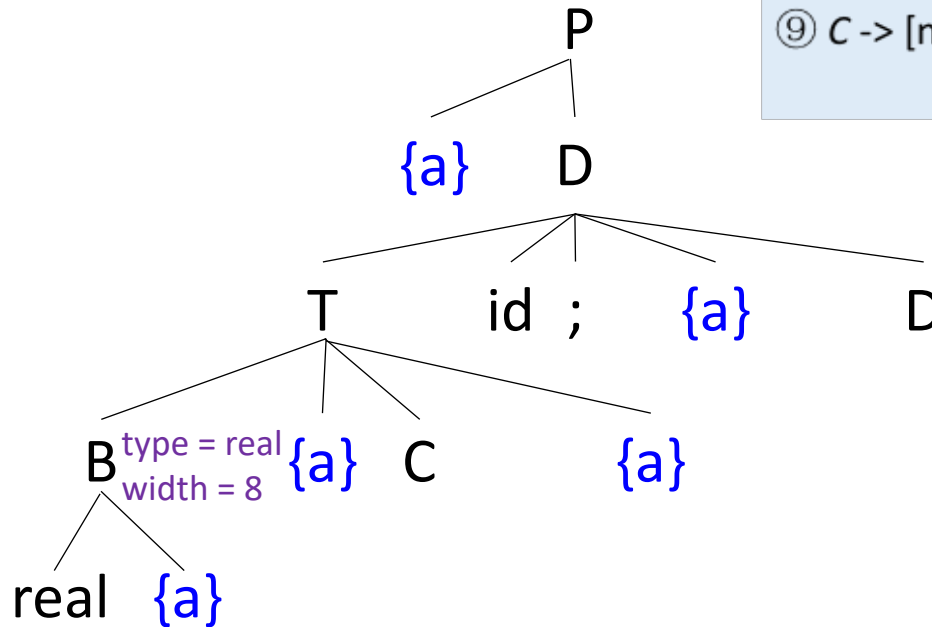


offset = 0

Example

- Input: **real x; int i;**
↑ ↑

- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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offset = 0

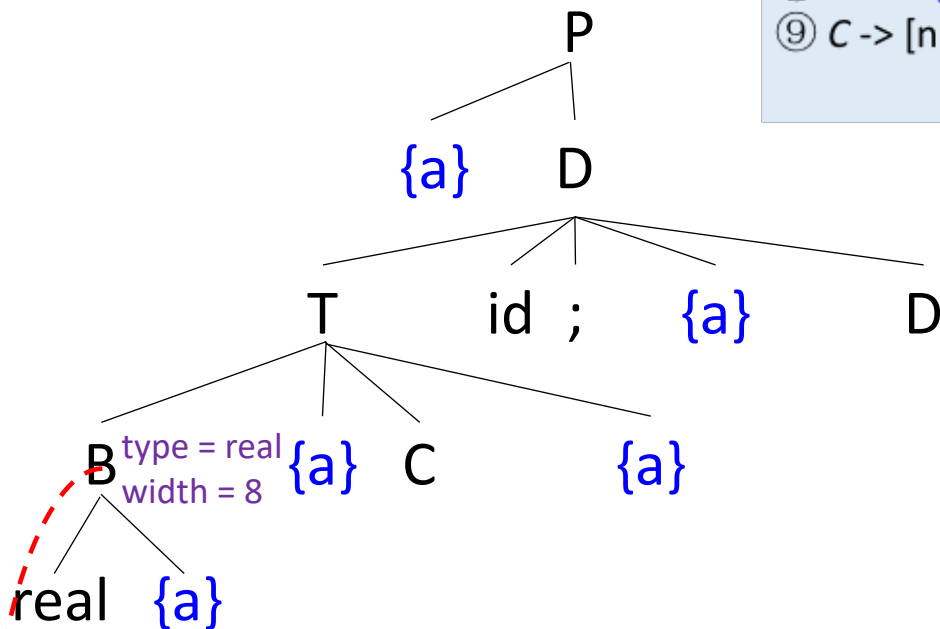
t = real
w = 8

Example

- Input: **real x; int i;**



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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offset = 0

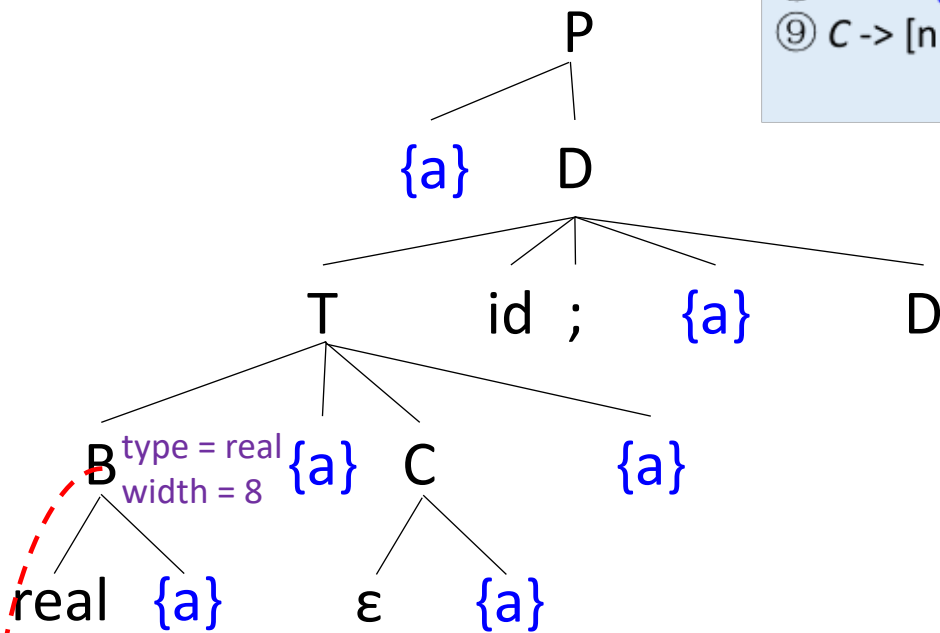
t = real
w = 8

Example

- Input: **real x; int i;**



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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offset = 0

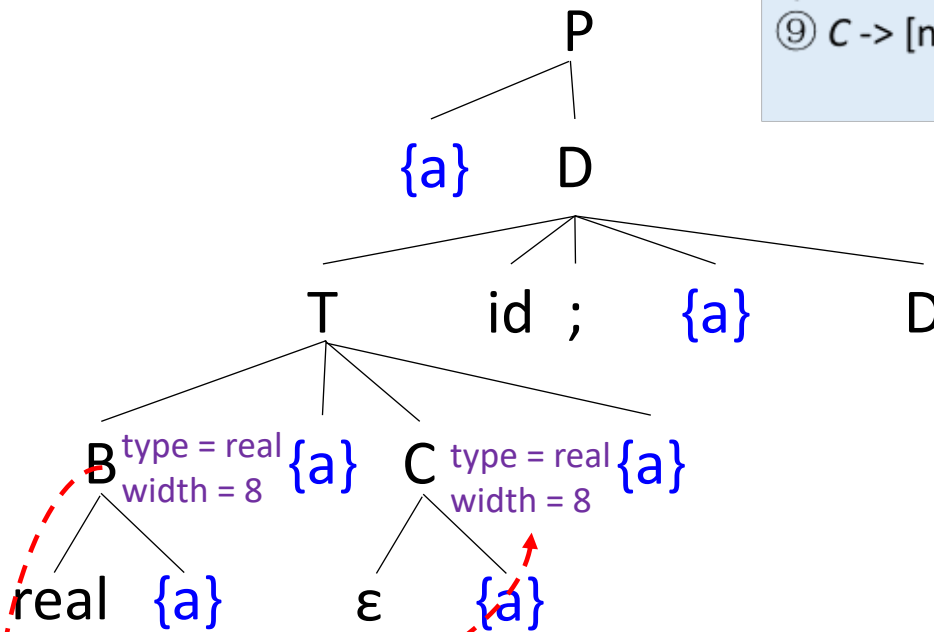
t = real
w = 8

Example

- Input: **real x; int i;**



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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offset = 0

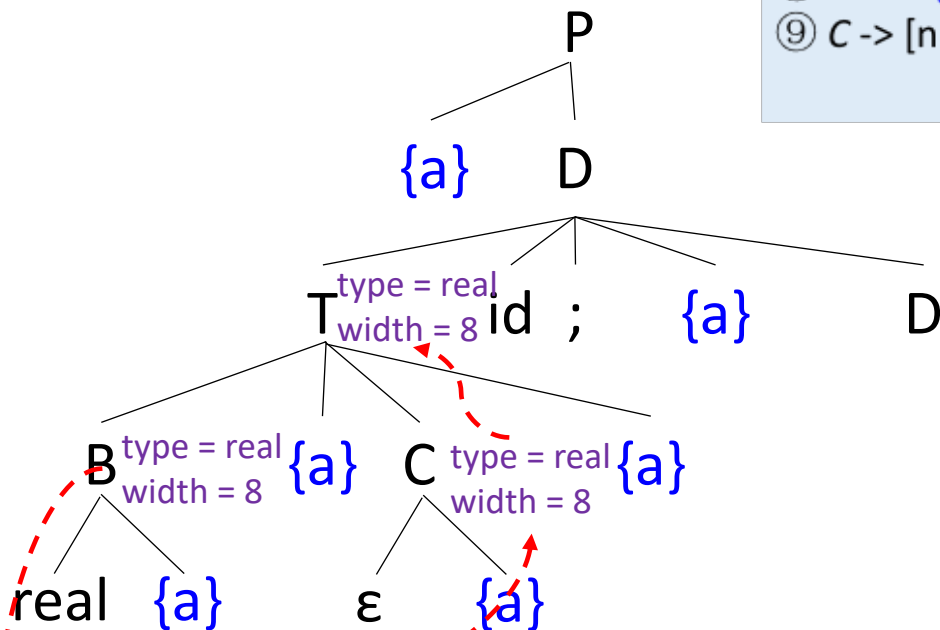
t = real
w = 8

Example

- Input: **real x; int i;**



- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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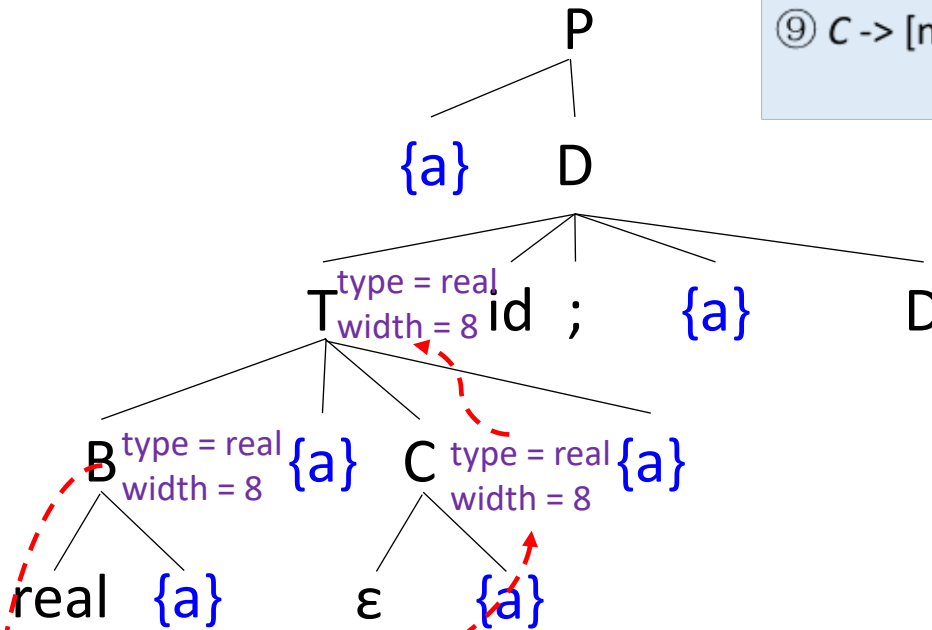
offset = 0

t = real
w = 8

Example

- Input: **real x; int i;**
↑ ↑↑ ↑↑

- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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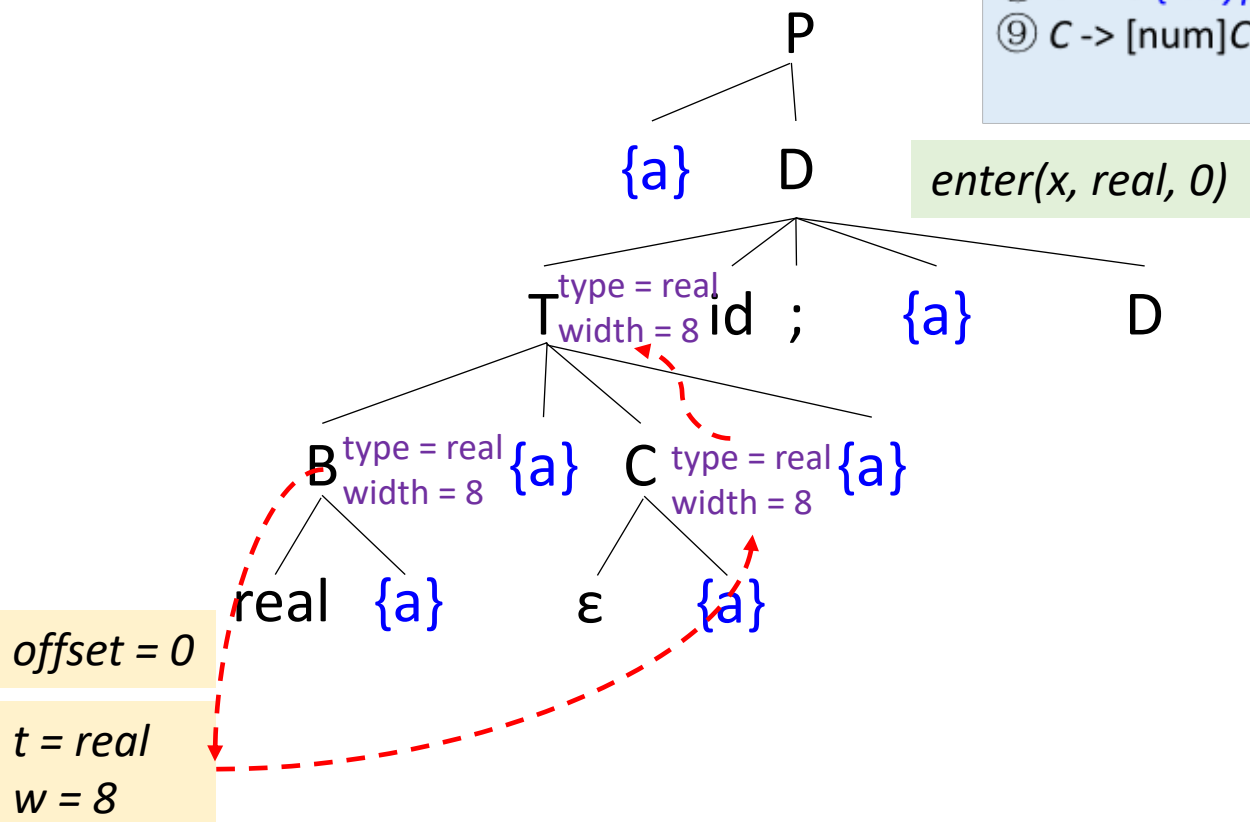


offset = 0
 t = real
 w = 8

Example

- Input: **real x; int i;**
↑ ↑↑ ↑

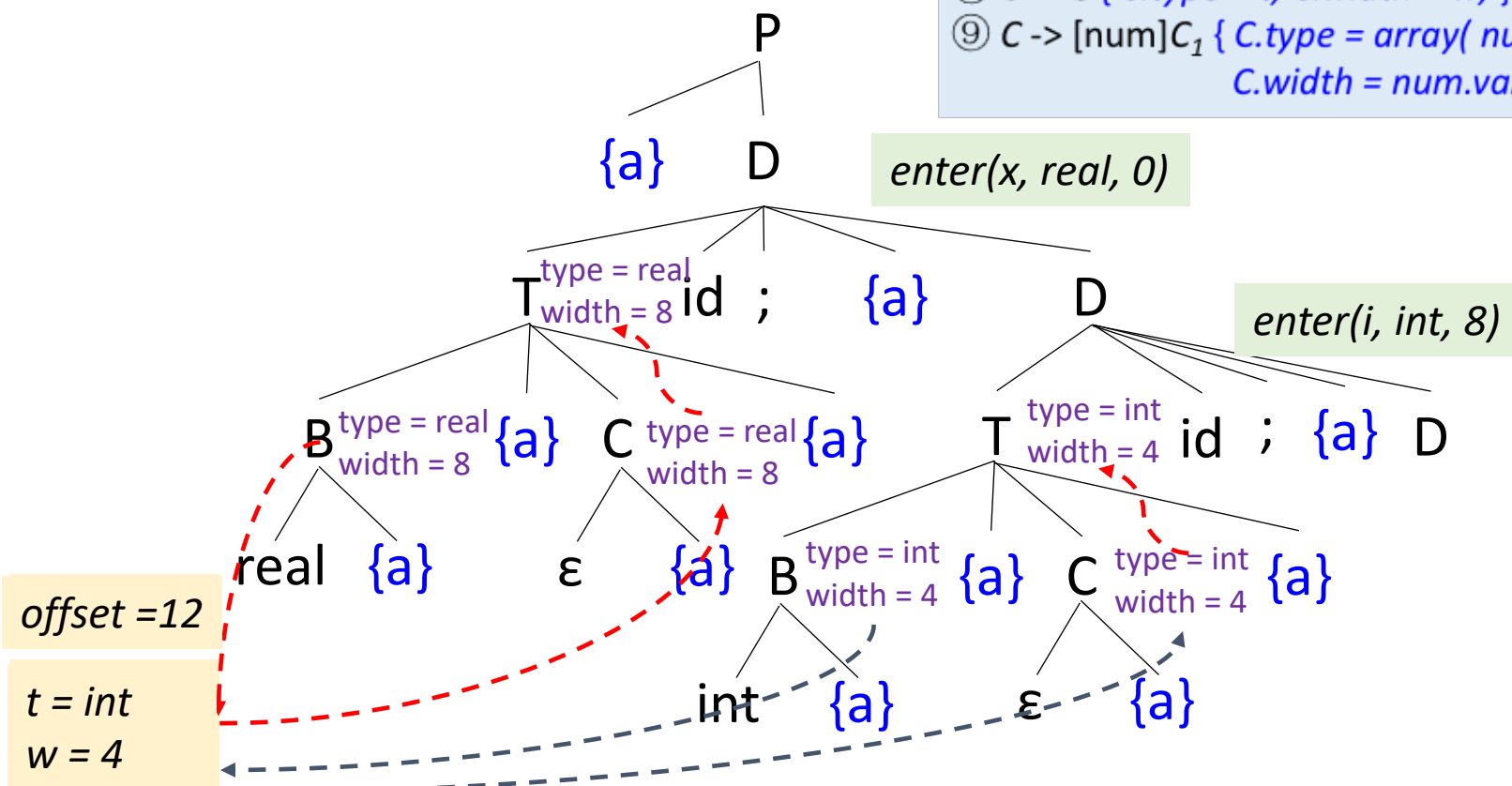
- ① $P \rightarrow \{ \text{offset} = 0 \} D$
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Example

- Input: `real x; int i;`

- ① $P \rightarrow \{ \text{offset} = 0 \} D$
- ② $D \rightarrow T \text{ id}; \{ \text{enter}(\text{id.lexeme}, T.\text{type}, \text{offset}); \text{offset} = \text{offset} + T.\text{width}; \} D_1$
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Code Generation[代码生成]

- Translations
 - Variable definitions[变量定义]
 - Assignment[赋值]
 - Array references[数组引用]
 - Boolean expressions[布尔表达式]
 - Control-flow statements[控制流语句]
- To generate three-address codes (TACs)
 - Lay out variables in memory
 - Generate TAC for any subexpressions or substatements
 - Using the result, generate TAC for the overall expression
- We can also use the syntax-directed formalisms to specify translations

CodeGen: Assignment Statement

- Translate into three-address code[赋值语句]
 - An expression with more than one operator will be translated into instructions with at most one operator per instruction
- Helper functions in translation
 - *lookup(id)*: search *id* in symbol table, return null if none
 - *emit()/gen()*: generate three-address IR
 - *newtemp()*: get a new temporary location

- ① $S \rightarrow id = E;$
- ② $E \rightarrow E_1 + E_2;$
- ③ $E \rightarrow - E_1$
- ④ $E \rightarrow (E_1)$
- ⑤ $E \rightarrow id$

Assignment statement:

$a = b + (-c)$

Three-address code:

$t_1 = \text{minus } c$

$t_2 = b + t_1$

$a = t_2$

Example: LLVM

```
1 double x;  
2  
3 void foo() {  
4     char a;  
5     int b = 0;  
6     long long c;  
7     int d;  
8  
9     int x = b + (-d);  
10 }
```

```
@x = dso_local global double 0.000000e+00, align 8
```

```
; Function Attrs: noinline nounwind optnone  
define dso_local void @foo() #0 {  
    %1 = alloca i8, align 1  
    %2 = alloca i32, align 4  
    %3 = alloca i64, align 8  
    %4 = alloca i32, align 4  
    %5 = alloca i32, align 4           // int x  
    store i32 0, i32* %2, align 4  
    %6 = load i32, i32* %2, align 4   // %6 = b  
    %7 = load i32, i32* %4, align 4   // %7 = d  
    %8 = sub nsw i32 0, %7           // %8 = -d  
    %9 = add nsw i32 %6, %8           // %9 = b + (-d)  
    store i32 %9, i32* %5, align 4   // x = %9 = b + (-d)  
    ret void  
}
```



```
auto left = myBuildExp(...);  
auto right = myBuildExp(...);  
Builder.CreateAdd(left, right, "add");
```

SDT Translation of Assignment

- Attributes ***code*** and ***addr***

- *S.code* and *E.code* denote the TAC for *S* and *E*, respectively
- *E.addr* denotes the address that will hold the value of *E* (can be a name, constant, or a compiler-generated temporary)

- ① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{if } !p \text{ then error};$
 $S.code = E.code \parallel$
 $gen(p '=' E.addr); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel E_2.code \parallel$
 $gen(E.addr '=' E_1.addr '+' E_2.addr); \}$
- ③ $E \rightarrow - E_1 \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel$
 $gen(E.addr '=' 'minus' E_1.addr); \}$
- ④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$
 $E.code = E_1.code; \}$
- ⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{if } !E.addr \text{ then error};$
 $E.code = ''; \}$

Incremental Translation[增量翻译]

- Generate only the new three-address instructions
 - *gen()* not only constructs a three-address inst, it appends the inst to the sequence of insts generated so far

- ① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{if } !p \text{ then error};$
 $S.code = E.code \parallel$
 $gen(p \text{ '=' } E.addr); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel E_2.code \parallel$
 $gen(E.addr \text{ '=' } E_1.addr \text{ '+' } E_2.addr); \}$
- ③ $E \rightarrow - E_1 \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel$
 $gen(E.addr \text{ '=' 'minus' } E_1.addr); \}$
- ④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$
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- ⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{if } !E.addr \text{ then error};$
 $E.code = \text{' '}; \}$

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- ① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{if } !p \text{ then error};$
 $S.code = E.code \parallel$
 $gen(p \text{ '=' } E.addr); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel E_2.code \parallel$
 $gen(E.addr \text{ '=' } E_1.addr \text{ '+' } E_2.addr); \}$
- ③ $E \rightarrow - E_1 \{ E.addr = newtemp();$
 $E.code = E_1.code \parallel$
 $gen(E.addr \text{ '=' } \text{'minus'} E_1.addr); \}$
- ④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$
 $E.code = E_1.code; \}$
- ⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{if } !E.addr \text{ then error};$
 $E.code = \text{' '}; \}$

Code attributes can
be long strings

Incremental Translation[增量翻译]

- Generate only the new three-address instructions
 - *gen()* not only constructs a three-address inst, it appends the inst to the sequence of insts generated so far

① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{if } !p \text{ then error};$

$gen(p := E.addr); \}$

② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp();$

$gen(E.addr := E_1.addr + E_2.addr); \}$

③ $E \rightarrow - E_1 \{ E.addr = newtemp();$

$gen(E.addr := 'minus' E_1.addr); \}$

④ $E \rightarrow (E_1) \{ E.addr = E_1.addr;$

$\}$

⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{if } !E.addr \text{ then error};$

$\}$

Code attributes can
be long strings

Example

- ① $S \rightarrow id = E; \{ p = \text{lookup}(id.\text{lexeme}); \text{if } !p \text{ then error; } \text{gen}(p = 'E.\text{addr}'); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.\text{addr} = \text{newtemp}(); \text{gen}(E.\text{addr} = 'E_1.\text{addr} + ' E_2.\text{addr}); \}$
- ③ $E \rightarrow - E_1 \{ E.\text{addr} = \text{newtemp}(); \text{gen}(E.\text{addr} = 'minus' E_1.\text{addr}); \}$
- ④ $E \rightarrow (E_1) \{ E.\text{addr} = E_1.\text{addr}; \}$
- ⑤ $E \rightarrow id \{ E.\text{addr} = \text{lookup}(id.\text{lexeme}); \text{if } !E.\text{addr} \text{ then error; } \}$

id	=	(id
x			a

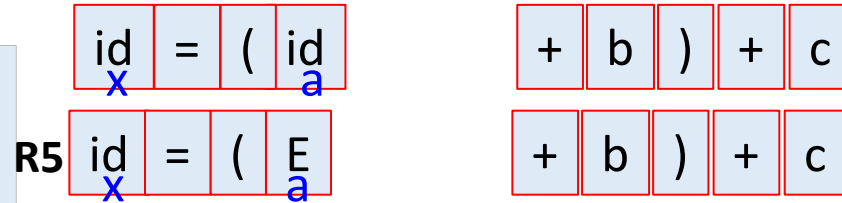
+	b)	+	c
---	---	---	---	---

- Input

$$x = (a + b) + c$$

Example

- ① $S \rightarrow id = E; \{ p = lookup(id.lexeme); \text{if } !p \text{ then error; } gen(p \text{ '=' } E.addr); \}$
- ② $E \rightarrow E_1 + E_2; \{ E.addr = newtemp(); gen(E.addr \text{ '=' } E_1.addr \text{ '+' } E_2.addr); \}$
- ③ $E \rightarrow - E_1 \{ E.addr = newtemp(); gen(E.addr \text{ '=' 'minus' } E_1.addr); \}$
- ④ $E \rightarrow (E_1) \{ E.addr = E_1.addr; \}$
- ⑤ $E \rightarrow id \{ E.addr = lookup(id.lexeme); \text{if } !E.addr \text{ then error; } \}$

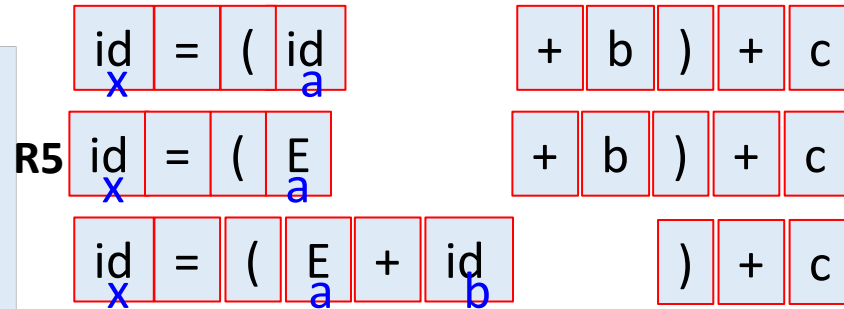


- Input

$$x = (a + b) + c$$

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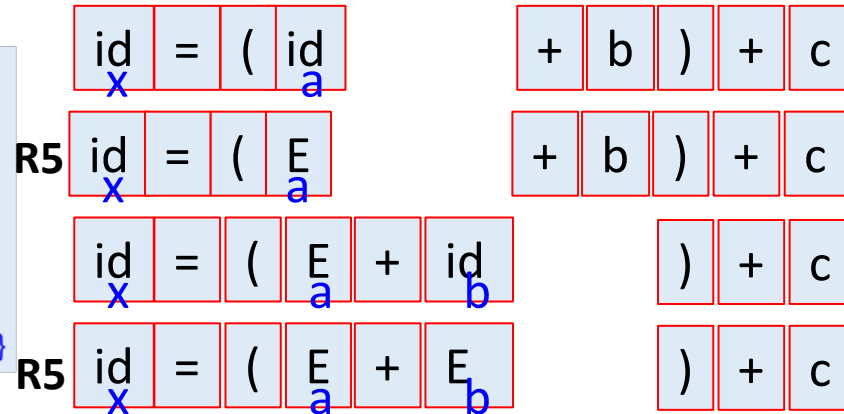


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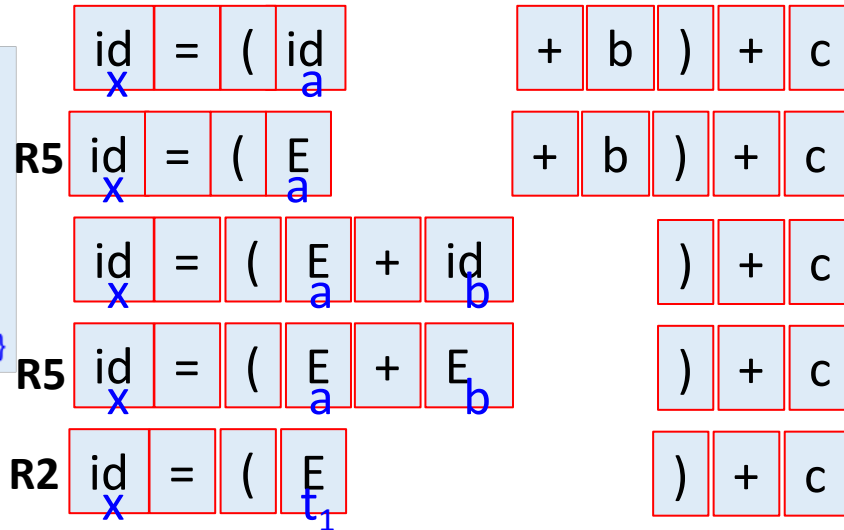


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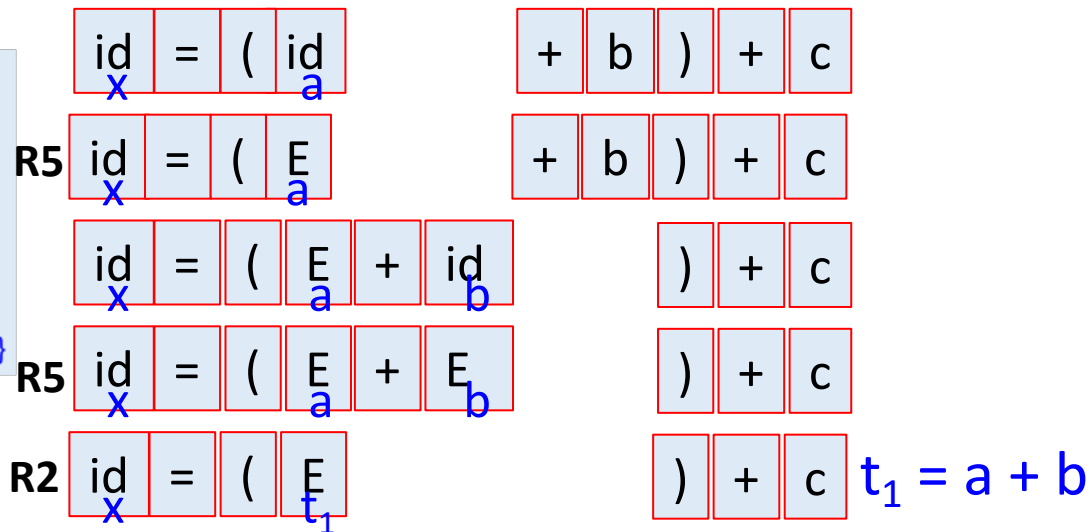


- Input

$$x = (a + b) + c$$

Example

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- Input

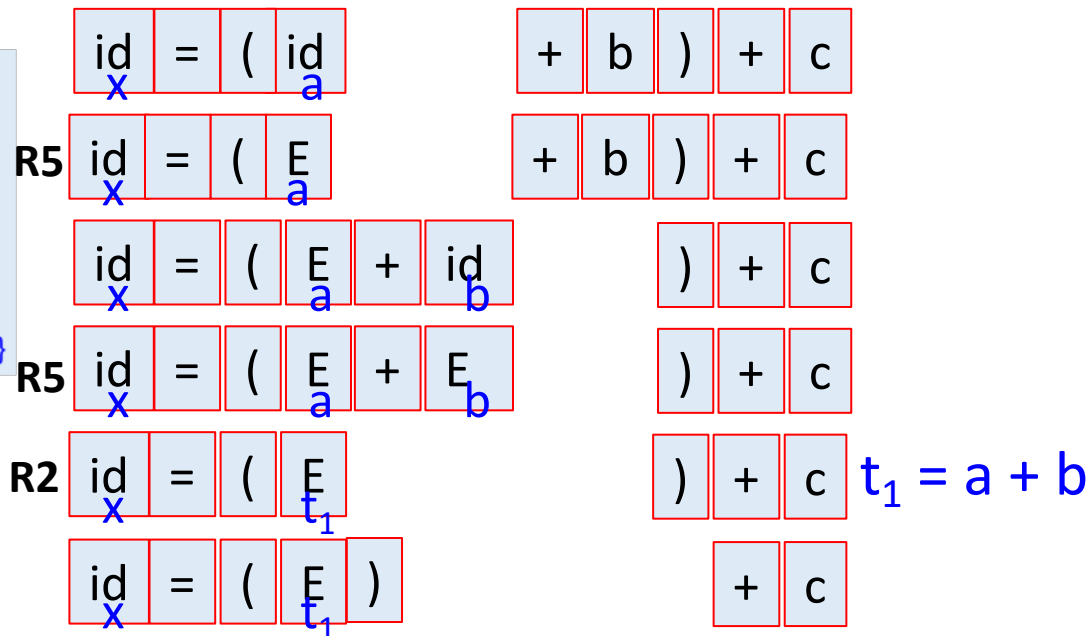
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Example

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- Input

$$x = (a + b) + c$$



CodeGen: Array Reference [数组引用]

- Primary problem in generating code for array references is to determine the address of element

- 1D array

```
int A[N];
```

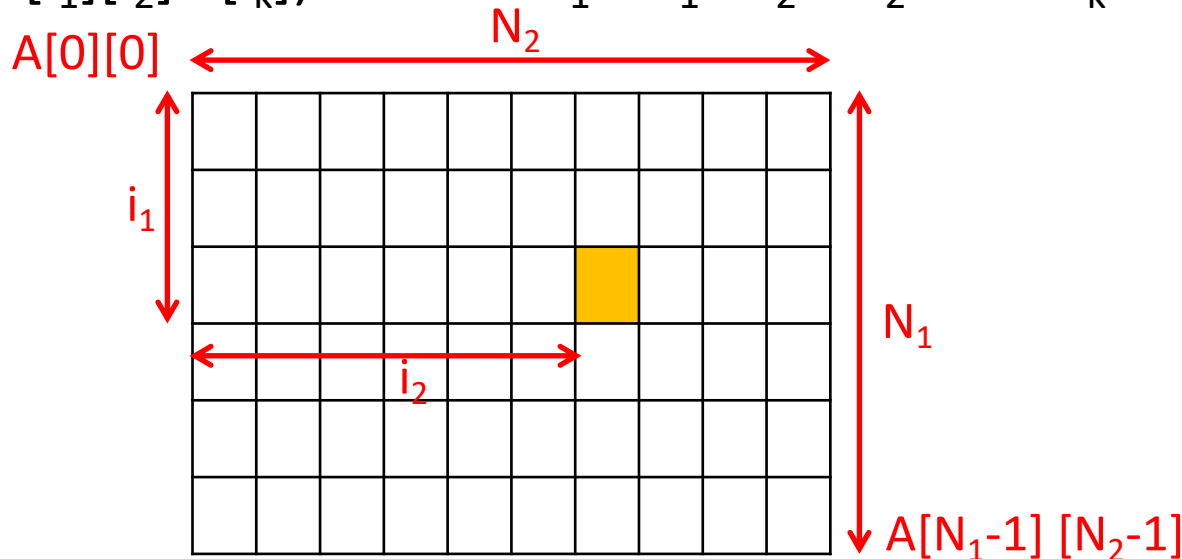
```
A[i] ++;
```



- *base*: address of the first element
 - *width*: width of each element
 - $i \times \text{width}$ is the offset
- Addressing an array element
 - $\text{addr}(A[i]) = \text{base} + i \times \text{width}$

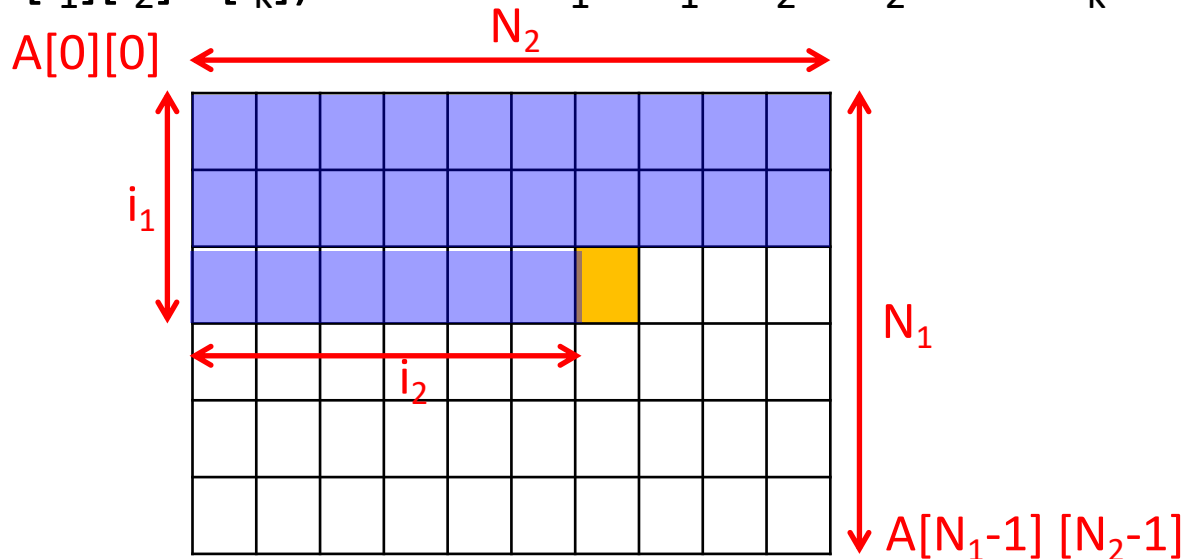
N-dimensional Array

- Laying out 2D array in 1D memory
 - `int A[N1][N2]; /* int A[0..N1][0..N2] */`
 - `A[i1][i2] ++;`
- The organization can be row-major or column-major
 - C language uses row major (i.e., stored row by row)
 - Row-major: $\text{addr}(A[i_1, i_2]) = \text{base} + (i_1 \times \underbrace{N_2}_{W_1} \times \text{width} + i_2 \times \underbrace{\text{width}}_{W_2})$
- *k*-dimensional array
 - $\text{addr}(A[i_1][i_2] \dots [i_k]) = \text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$



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- *k*-dimensional array
 - $\text{addr}(A[i_1][i_2] \dots [i_k]) = \text{base} + i_1 \times w_1 + i_2 \times w_2 + \dots + i_k \times w_k$



Example: LLVM

```
1 double x;  
2 int arr[3][5][8];  
3  
4 void foo() {  
5     char a;  
6     int b = 0;  
7     long long c;  
8     int d;  
9  
10    int x = arr[2][3][4];  
11 }
```

```
@arr = dso_local global [3 x [5 x [8 x i32]]] zeroinitializer, align 4  
@x = dso_local global double 0.000000e+00, align 8
```

```
; Function Attrs: noline nounwind optnone  
define dso_local void @foo() #0 {  
    %1 = alloca i8, align 1  
    %2 = alloca i32, align 4  
    %3 = alloca i64, align 8  
    %4 = alloca i32, align 4  
    %5 = alloca i32, align 4  
    store i32 0, i32* %2, align 4 // addr(@arr + 4x(0 + 2*3*4 + 3*4 + 4))  
    %6 = load i32, i32* getelementptr inbounds ([3 x [5 x [8 x i32]]], [3  
x [5 x [8 x i32]]]* @arr, i64 0, i64 2, i64 3, i64 4), align 4  
    store i32 %6, i32* %5, align 4  
    ret void  
}
```



`Builder.CreateInBoundsGEP(addr, ...);`