



中山大學
SUN YAT-SEN UNIVERSITY

计算机学院（软件学院）

SCHOOL OF COMPUTER SCIENCE AND ENGINEERING

Compilation Principle

编译原理

第13讲：语法分析(9)

张献伟

xianweiz.github.io

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中山大學
SUN YAT-SEN UNIVERSITY



Quiz

Handwritten, or email to
chenhq79@mail2.sysu.edu.cn



- Q1: explain action table entries si or rj .
 si : shift the input symbol and move to state i
 rj : reduce by production numbered j

State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	r2	r2	r2		5

- Q2: augment the grammar G .

G :

$S \rightarrow ABC$

$B \rightarrow b|c$

Add one extra rule $S' \rightarrow S$ to guarantee only one 'acc' in the table

- Q3: what is the initial state (S_0) of G' ?

G' :

$S' \rightarrow S$

$S \rightarrow ABC$

$B \rightarrow b|c$

$\text{Closure}(S' \rightarrow \bullet S) = \{ S' \rightarrow \bullet S, S \rightarrow \bullet ABC \}$

- Q4: what does $S \rightarrow ABC\bullet$ mean?

We have seen the body ABC and it is time to reduce ABC to S

- Q5: what is the closure of $S \rightarrow A\bullet BC$?

$\{ S \rightarrow A\bullet BC, B \rightarrow \bullet b, B \rightarrow \bullet c \}$

Deadline[截止时间]

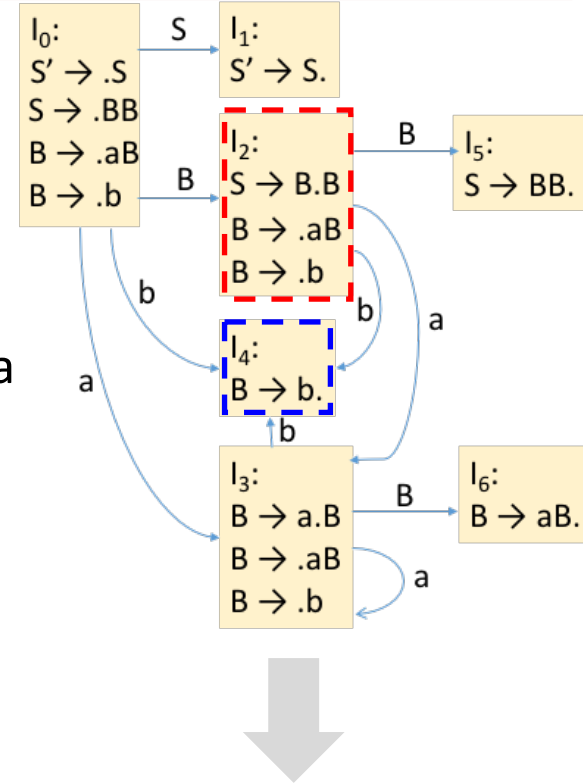
- 宽限期(Slip Days): proj2/3/4共10天
 - 可用于延期提交, 宽限期内不扣分
 - 每人共分配10天, 可拆分使用, 不可转借
 - 每个slip day为自然日, 使用单位为整数日
 - 如使用, 截止时间前需填写问卷申请
 - 迟交扣分规则
 - 不填写问卷或宽限期无剩余, 视为迟交
 - 迟交每一天扣除得分10%

proj1昨晚已经截止, 我们会尽快完成批改! 未提交的同学: 如果截止前填写了问卷, 自动宽限5天, 请于4.2/周二 23:59:59前提交 (宽限期内扣除得分的5%), 宽限期外每延一天再扣除得分的10%; 没有填写问卷的同学, 从今天开始每天扣除10%。proj2/3/4将类似执行, 具体有所调整。

- 理论
 - 随机点名
 - 缺席优先
 - 随机提问
 - 后排优先
 - 随机测试
 - 不定时间
- 实验
 - 个人完成
 - 杜绝抄袭
 - 按时提交
 - 硬性截止
 - 侧重代码实现
 - 简略报告

Build Parse Table from DFA

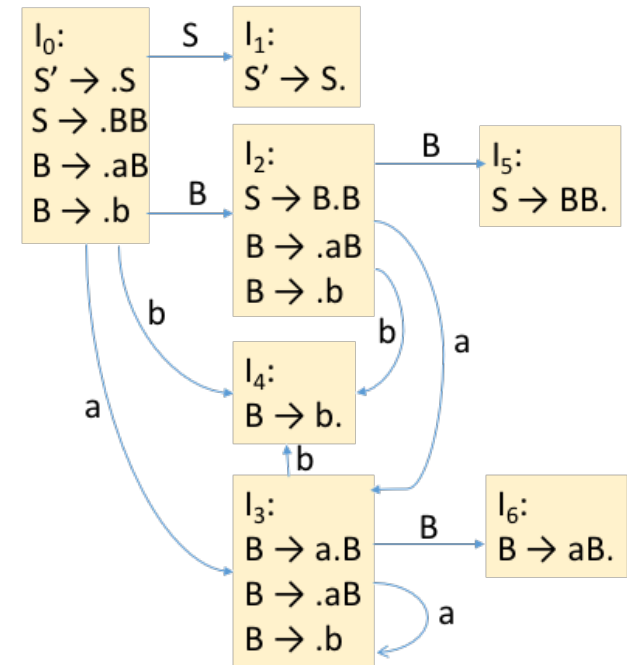
- ACTION: [*state*, *terminal symbol*]
- GOTO: [*state*, *non-terminal symbol*]
- ACTION[动作]
 - If $[A \rightarrow \alpha \cdot a \beta]$ is in S_i and $\text{goto}(S_i, a) = S_j$, where "a" is a terminal, then $\text{ACTION}[S_i, a] = \text{shift } j$ (*sj*)
 - If $[A \rightarrow \alpha \cdot]$ is in S_i and $A \rightarrow \alpha$ is rule numbered j , then $\text{ACTION}[S_i, a] = \text{reduce } j$ (*rj*)
 - If $[S' \rightarrow S \cdot]$ is in S_i then $\text{ACTION}[S_i, \$] = \text{accept}$
 - If no conflicts among 'shift' and 'reduce' (the first two 'if's), then this parser is able to parse the given grammar
- GOTO[跳转]
 - if $\text{goto}(S_i, A) = S_j$ then $\text{GOTO}[S_i, A] = j$
- All entries not filled are rejects




State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	s3	s4			5
3	s3	s4			6
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		

LR(0) Parsing

- Construct LR(0) automaton from the Grammar[由文法构建自动机]
- Idea: assume
 - Input buffer contains α [但buffer不止有 α]
 - Next input is t [α 后是 t]
 - DFA on input α terminates in state s
 - α 处理完毕后处于状态 s
- Next: **reduce** by $X \rightarrow \beta$ if[归约]
 - s contains item $X \rightarrow \beta \cdot$
- Or, **shift** if[移进]
 - s contains item $X \rightarrow \beta \cdot t w$
 - Equivalent to saying s has a transition labeled t



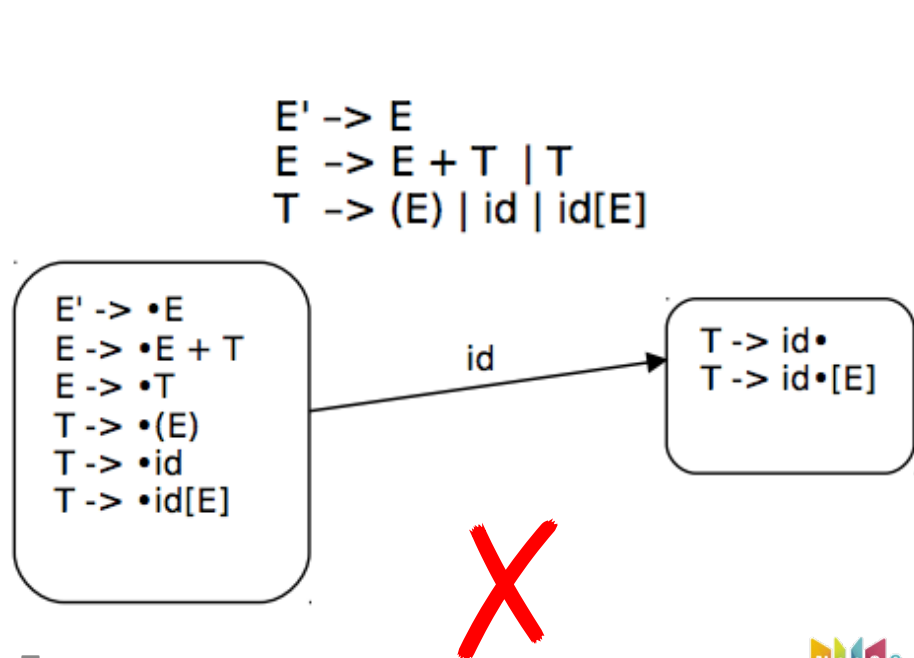
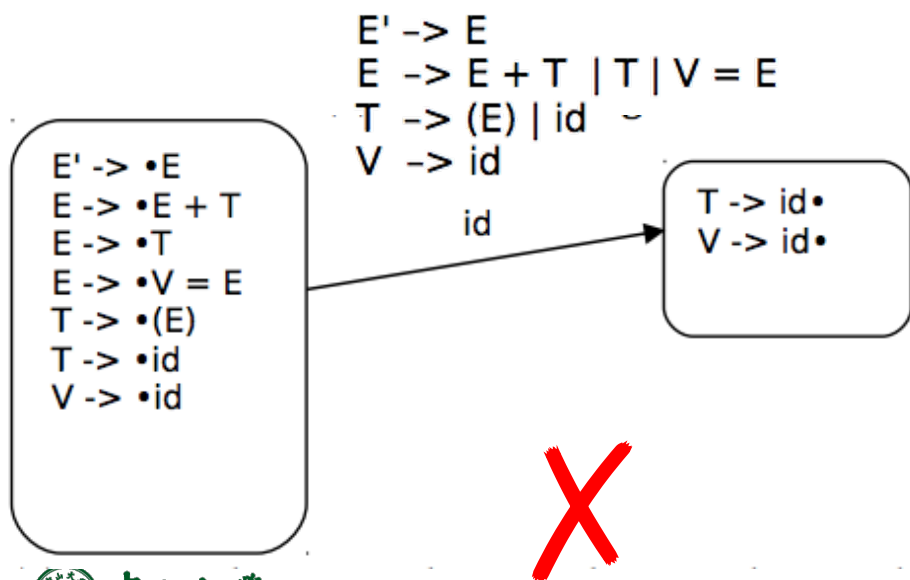
LR(0) Parsing (cont.)

- The parser must be able to determine what action to take in each state without looking at any further input symbols [没有展望就可以决定动作]
 - i.e. by only considering what the parsing stack contains so far
 -  This is the '0' in the parser name
- In a LR(0) table, each state must only shift or reduce [确定性移进或归约]
 - Thus an LR(0) configuring set can only have exactly one reduce item [每个归约item自成一个状态]
 - cannot have both shift and reduce items; otherwise, conflicts

State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	s3	s4			5
3	s3	s4			6
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		

LR(0) Conflicts[冲突]

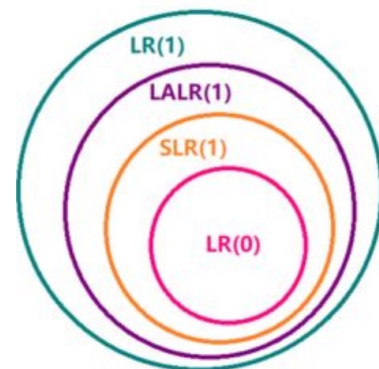
- LR(0) has a **reduce/reduce** conflict[归约-归约冲突] if:
 - Any state has two reduce items:
 - $X \rightarrow \beta \cdot$ and $Y \rightarrow \omega \cdot$
- LR(0) has a **shift/reduce** conflict[移进-归约冲突] if:
 - Any state has a reduce item and a shift item:
 - $X \rightarrow \beta \cdot$ and $Y \rightarrow \omega \cdot t \sigma$



LR(0) Summary[小结]

- LR(0) is the simplest LR parsing[最简单]
 - Table-driven shift-reduce parser[表驱动]
 - ACTION table[s, a] + GOTO table[s, X]
 - Weakest LR, not used much in practice[实际不常使用]
 - Parses without using any lookahead[没有任何展望]

- Adding just one token of lookahead vastly increases the parsing power[考虑展望]
 - SLR(1): simple LR(1), use FOLLOW[归约用FOLLOW]
 - LR(1): use dedicated symbols[比FOLLOW更精细]
 - LALR(1): balance SLR(1) and LR(1)[折衷]



SLR(1) Parsing

- LR(0) conflicts are generally caused by **reduce** actions

- If the item is complete ($A \rightarrow \alpha \cdot$), the parser must choose to reduce [项目形式完整就归约]

- Is this always appropriate?

- The next upcoming token may tell us something different

- What tokens may tell the reduction is not appropriate?

- Perhaps **FOLLOW(A)** could be useful here

- If the sequence on top of the stack could be reduced to the nonterminal A , what tokens do we expect to find as the next input?

State	ACTION			GOTO	
	a	b	\$	S	B
0	s3	s4		1	2
1			acc		
2	s3	s4			5
3	s3	s4			6
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		

- **SLR** = Simple LR

- Use the same LR(0) configuring sets and have the same table structure and parser operation [表结构一致]

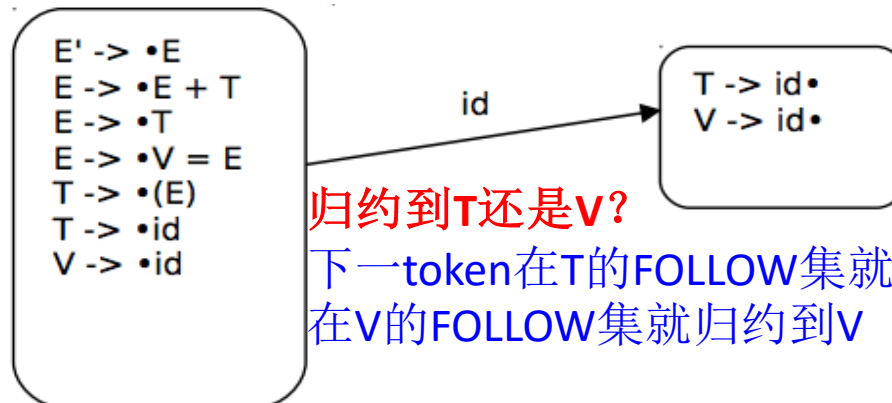
- The difference comes in assigning table actions [动作填充不同]

- Use one token of lookahead to help arbitrate among the conflicts

- Reduce only if the next input token is a member of the FOLLOW set of the non-terminal being reduced to [下一token在FOLLOW集才归约]

SLR(1) Parsing (cont.)

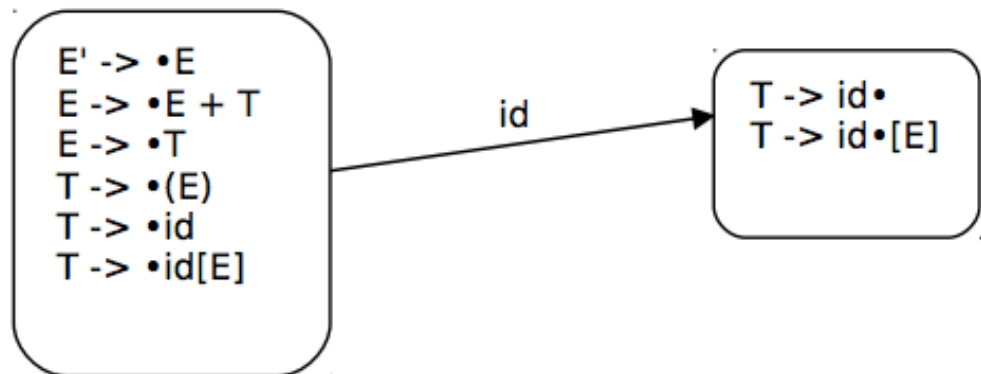
- In the SLR(1) parser, it is allowable for there to be both shift and reduce items in the same state as well as multiple reduce items
 - The SLR(1) parser will be able to determine which action to take as long as the FOLLOW sets are **disjoint**[可区分即可]



Example

- The first two LR(0) configurating sets entered if *id* is the first token of the input[用于识别id所处的前两个状态]
 - LR(0) parser: the set on the right side has a **shift-reduce conflict**
 - SLR(1) parser:
 - Compute FOLLOW(T) = { +,),], \$ }, i.e., only reduce on those tokens
 - FOLLOW(T) = FOLLOW(E) = {+,),], \$}
 - **id[id]**: next input is **[**, not in FOLLOW(T), **shift**
 - **id + id**: next input is **+**, in FOLLOW(T), **reduce**

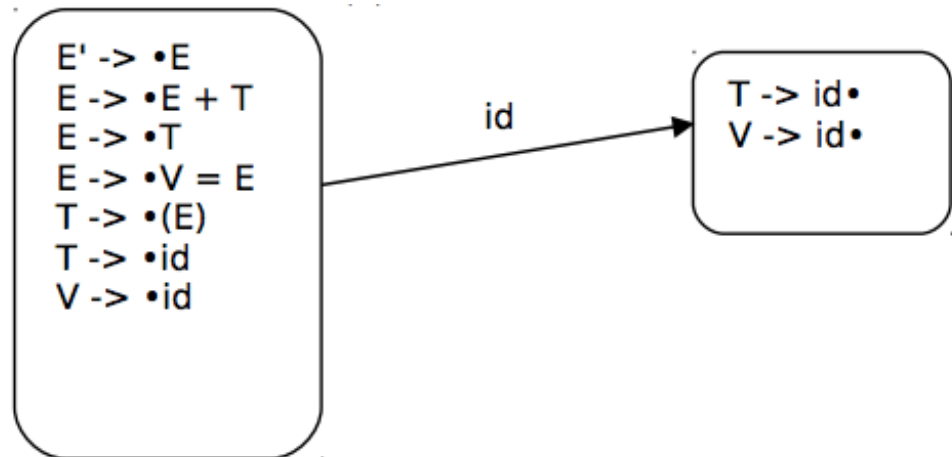
$E' \rightarrow E$
 $E \rightarrow E + T \mid T$
 $T \rightarrow (E) \mid id \mid id[E]$



Example (cont.)

- The first two LR(0) configurating sets entered if *id* is the first token of the input [用于识别id所处的前两个状态]
 - LR(0) parser: the right set has a **reduce-reduce conflict**
 - SLR(1) parser:
 - Capable to distinguish which reduction to apply depending on the next input token, **no conflict**
 - Compute FOLLOW(T) = { +,), \$ } and FOLLOW(V) = { = }
id + id => T -> id
id = id => V -> id

$E' \rightarrow E$
 $E \rightarrow E + T \mid T \mid V = E$
 $T \rightarrow (E) \mid id$
 $V \rightarrow id$



SLR(1) Grammars[文法]

- A grammar is SLR(1) if the following two conditions hold for each configurating set[可区分]
 - (1) For any item $A \rightarrow u \cdot x v$ in the set, with terminal x , there is no complete item $B \rightarrow w \cdot$ in that set with x in FOLLOW(B)[无移入-归约冲突]
 - In the table, this translates no shift-reduce conflict on any state
 - (2) For any two complete items $A \rightarrow u \cdot$ and $B \rightarrow v \cdot$ in the set, the follow sets must be disjoint, i.e. FOLLOW(A) \cap FOLLOW(B) is empty[无归约-归约冲突]
 - This translates to no reduce-reduce conflict on any state
 - If more than one nonterminal could be reduced from this set, it must be possible to uniquely determine which using only one token of lookahead

SLR(1) Limitations[限制]

- SLR(1) vs. LR(0)
 - Adding just one token of lookahead and using the FOLLOW set greatly expands the class of grammars that can be parsed without conflict
- When we have a completed configuration (i.e., dot at the end) such as $X \rightarrow u \cdot$, we know that it is reducible[可归约]
 - We allow such a reduction whenever the next symbol is in FOLLOW(X)[使用 FOLLOW集]
 - However, it may be that we should not reduce for every symbol in FOLLOW(X), because the symbols below u on the stack preclude u being a handle for reduction in this case[FOLLOW集不足够]
 - In other words, SLR(1) states only tell us about the sequence on top of the stack, not what is below it on the stack[状态是怎么转移过来的?]
 - We may need to divide an SLR(1) state into separate states to differentiate the possible means by which that sequence has appeared on the stack[额外使用栈信息, FOLLOW是input buffer信息]

Example

- For input string: $id = id$, at I_2 after having reduced id_{Left} to L
 - Initially, at S_0
 - Move to S_5 , after shifting id to stack (S_5 is also pushed to stack)
 - Reduce, and back to S_0 , and further GOTO S_2
 - S_5 has a completed item, and next '=' is in FOLLOW(L)
 - S_5 and id are popped from stack, and L is pushed onto stack
 - $GOTO(S_0, L) = S_2$

$S' \rightarrow S$
 $S \rightarrow L = R$
 $S \rightarrow R$
 $L \rightarrow *R$
 $L \rightarrow id$
 $R \rightarrow L$

$I_0:$

$S' \rightarrow \bullet S$
$S \rightarrow \bullet L = R$
$S \rightarrow \bullet R$
$L \rightarrow \bullet *R$
$L \rightarrow \bullet id$
$R \rightarrow \bullet L$

$I_5:$

$L \rightarrow id \bullet$

$I_6:$

$S \rightarrow L = \bullet R$
$R \rightarrow \bullet L$
$L \rightarrow \bullet *R$
$L \rightarrow \bullet id$

$I_1:$

$S' \rightarrow S \bullet$

$I_7:$

$L \rightarrow *R \bullet$

$I_2:$

$S \rightarrow L \bullet = R$
$R \rightarrow L \bullet$

$I_8:$

$R \rightarrow L \bullet$

$I_3:$

$S \rightarrow R \bullet$

$I_9:$

$S \rightarrow L = R \bullet$

$I_4:$

$L \rightarrow * \bullet R$
$R \rightarrow \bullet L$
$L \rightarrow \bullet *R$
$L \rightarrow \bullet id$

Example (cont.)

- Choices upon seeing = coming up in the input:

$S' \rightarrow S$
 $S \rightarrow L = R$
 $S \rightarrow R$
 $L \rightarrow *R$
 $L \rightarrow id$
 $R \rightarrow L$

- Action[2, =] = s6
 - Move on to find rest of assignment

▫ $S \Rightarrow L=R \Rightarrow L=L \Rightarrow \dots$

- Action[2, =] = r5

▫ $= \in FOLLOW(R): S \Rightarrow L=R \Rightarrow L=L \Rightarrow L=*R \Rightarrow L=*L \Rightarrow \dots$

- Shift-reduce conflict

- SLR parser fails to remember enough info
- Reduce using $R \rightarrow L$ only after seeing * or =

$I_0: S' \rightarrow \bullet S$
 $S \rightarrow \bullet L = R$
 $S \rightarrow \bullet R$
 $L \rightarrow \bullet *R$
 $L \rightarrow \bullet id$
 $R \rightarrow \bullet L$

$I_5: L \rightarrow id \bullet$
 $I_6: S \rightarrow L = \bullet R$
 $R \rightarrow \bullet L$
 $L \rightarrow \bullet *R$
 $L \rightarrow \bullet id$

$I_1: S' \rightarrow S \bullet$

$I_7: L \rightarrow *R \bullet$

$I_2: S \rightarrow L \bullet = R$
 $R \rightarrow L \bullet$

$I_8: R \rightarrow L \bullet$

$I_3: S \rightarrow R \bullet$

$I_9: S \rightarrow L = R \bullet$

$I_4: L \rightarrow * \bullet R$
 $R \rightarrow \bullet L$
 $L \rightarrow \bullet *R$
 $L \rightarrow \bullet id$

For any item $A \rightarrow u \cdot x v$ in the set, with terminal x , there is no complete item $B \rightarrow w \cdot$ in that set with x in $FOLLOW(B)$

SLR(1) Improvement[改进]

- We don't need to see additional symbols beyond the first token in the input, we have already seen the info that allows us to determine the correct choice[展望信息已足够]
- Retain a little more of the left **context** that brought us here[历史路径]
 - Divide an SLR(1) state into separate states to differentiate the possible means by which that sequence has appeared on the stack
- Just using the entire FOLLOW set is not discriminating enough as the guide for when to reduce[FOLLOW集不够]
 - For the example, the FOLLOW set contains symbols that can follow R in any position within a valid sentence
 - But it does not precisely indicate which symbols follow R at this particular point in a derivation

LR(1) Parsing

- LR parsing adds the required extra info into the state
 - By redefining items to include a **terminal symbol** as an added component[让项目中包含终结符]
- General form of **LR(1) items**[项目]
 - $A \rightarrow X_1 \dots X_i \bullet X_{i+1} \dots X_j, a$
 - We have states $X_1 \dots X_i$ on the stack and are looking to put states $X_{i+1} \dots X_j$ on the stack and then reduce
 - But **only if** the token following X_j is the terminal a
 - a is called the lookahead of the configuration
- The lookahead **only** works with completed items[完成项]
 - $A \rightarrow X_1 \dots X_j \bullet, a$
 - All states are now on the stack, but only reduce when next symbol is a (a is either a terminal or \$)
 - Multi lookahead symbols: $A \rightarrow u \bullet, a/b/c$

LR(1) Parsing (cont.)

- When to reduce?
 - LR(0): if the configuration set has a **completed item** (i.e., dot at the end)
 - SLR(1): only if the next input token is in the **FOLLOW** set
 - LR(1): only if the next input token is exactly a (terminal or \$)
 - Trend: **more and more precise**
- **LR(1) items**: LR(0) item + lookahead terminals
 - Many differ only in their lookahead components[仅展望不同]
 - The extra lookahead terminals allow to make parsing decisions beyond the SLR(1) capability, but with **a big price**[代价]
 - More distinguished items and thus more sets
 - Greatly increased GOTO and ACTION table sizes

$S' \rightarrow \cdot S$

LR(0)

$S' \rightarrow \cdot S, \$$

LR(1)

LR(1) Construction

- Configuration sets

- Sets construction are essentially the same with SLR, but differing on Closure() and Goto()
 - Because we must respect the lookahead

- Closure()

- For each item $[A \rightarrow u \cdot Bv, a]$ in I , for each production rule $B \rightarrow w$ in G' , add $[B \rightarrow \cdot w, b]$ to I , if
 - $b \in \text{FIRST}(va)$ and $[B \rightarrow \cdot w, b]$ is not already in I
- Lookahead symbols are the **FIRST(va)**, which are what can follow B
 - v can be nullable

(0) $S' \rightarrow S$

(1) $S \rightarrow BB$

(2) $B \rightarrow aB$

(3) $B \rightarrow b$

$S' \rightarrow \cdot S, \$$

I_0 :
 $S' \rightarrow \cdot S, \$$
 $S \rightarrow \cdot BB, \text{First}(\epsilon\$)$
 $B \rightarrow \cdot aB, \text{First}(B\$)$
 $B \rightarrow \cdot b, \text{First}(B\$)$

I_0 :
 $S' \rightarrow \cdot S, \$$
 $S \rightarrow \cdot BB, \$$
 $B \rightarrow \cdot aB, a/b$
 $B \rightarrow \cdot b, a/b$

LR(1) Construction (cont.)

- **Goto(I, X)**

- For item $[A \rightarrow u \cdot Xv, a]$ in I , $\text{Goto}(I, X) = \text{Closure}([A \rightarrow uX \cdot v, a])$
- Basically the same Goto function as defined for LR(0)
 - But have to **propagate the lookahead**[传递] when computing the transitions

- Overall steps

- Start from the initial set $\text{Closure}([S' \rightarrow \cdot S, \$])$
- Construct configuration sets following $\text{Goto}(I, X)$
- Repeat until no new sets can be added

I_0 :

$S' \rightarrow \cdot S, \$$

$S \rightarrow \cdot BB, \$$

$B \rightarrow \cdot aB, a/b$

$B \rightarrow \cdot b, a/b$

B

I_2 :

$S \rightarrow B \cdot B, \$$

$B \rightarrow \cdot aB, \text{First}(\epsilon \$)$

$B \rightarrow \cdot b, \text{First}(\epsilon \$)$

I_2 :

$S \rightarrow B \cdot B, \$$

$B \rightarrow \cdot aB, \$$

$B \rightarrow \cdot b, \$$