



中山大學
SUN YAT-SEN UNIVERSITY

计算机学院（软件学院）

SCHOOL OF COMPUTER SCIENCE AND ENGINEERING

Compilation Principle

编译原理

第7讲：语法分析(3)

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Review Questions

- Grammar G: $stmt \rightarrow \text{if} (expr) stmt \text{ else } stmt$
 $\quad \quad \quad | \text{ while} (expr) stmt \mid v$
 $expr \rightarrow \text{true} \mid \text{false}$

$N = \{ stmt \ expr \}$

- Is $\text{if} (\text{true}) stmt \text{ else } v$ an sentence of grammar G?

NO. It is a sentential form (句型), as $stmt$ is a non-terminal symbol.

- Is $\text{while} (\text{false}) \text{ else } v$ an sentence of G?

NO. It cannot be derived using the production rules.

- Grammar G: $E \rightarrow T/E \mid T$, result of $6 - 4 / 2$?
 $T \rightarrow T - T \mid \text{id}$

$(6 - 4) / 2 = 1$

- Regard $\text{id} - \text{id} - \text{id}$, is G ambiguous?

Yes. No associativity is specified for operator $-$.

Example

```
a, b = 1, c = 2;
a = b = c;
b = a - b - c;
b = ???
```

```
1 #include <stdio.h>
2
3 int main(int argc, char* argv[]) {
4     int a, b = 1, c = 2;
5     a = b = c;
6
7     b = a - b - c;
8
9     printf("\t\t\t a=%d, b=%d\n", a, b);
10
11    a = 0, b = 2, c = 3;
12    printf("\t\t\t (0==2-3) = %d, (0==2!=3) = %d\n", a == b - c, a == b != c);
13
14    return 0;
15 }
```

```
# vim ari.c
# clang -o ari ari.c
# ./ari
a=2, b=-2
(0==2-3) = 0, (0==2!=3) = 1
```

+	Binary plus(Addition)	Left to right
-	Binary minus(subtraction)	
==	Equal to	Left to right
!=	Not equal to	

Parser Implementation: Yacc + lex

parser.y

```
1 %{
2 #include <ctype.h>
3 #include <stdio.h>
4 #define YYSTYPE double /* double type for Yacc stack */
5 %}
6 %token NUMBER
7
8 %left '+' '-'
9 %left '*' '/'
10
11 %%
12
13 lines : lines expr '\n' { printf("= %g\n", $2); }
14       | lines '\n'
15       /* empty */
16       ;
17 expr  : expr '+' expr { $$ = $1 + $3; }
18       | expr '-' expr { $$ = $1 - $3; }
19       | expr '*' expr { $$ = $1 * $3; }
20       | expr '/' expr { $$ = $1 / $3; }
21       | '(' expr ')' { $$ = $2; }
22       | NUMBER
23       ;
24
25 E → E+E|E-E|E*E|E/E|(E)|num
26
27 /*
28 int yylex() {
29     int c;
30     while ((c = getchar()) == ' ');
31     if ((c == '.') || isdigit(c)) {
32         ungetc(c, stdin);
33         scanf("%lf", &yylval);
34         return NUMBER;
35     }
36     return c;
37 }
38 */
39
40 int main() {
41     if (yyparse() != 0)
42         fprintf(stderr, "Abnormal exit\n");
43     return 0;
44 }
45
46 int yyerror(char *s) {
47     fprintf(stderr, "Error: %s\n", s);
48 }
```

lexer.l

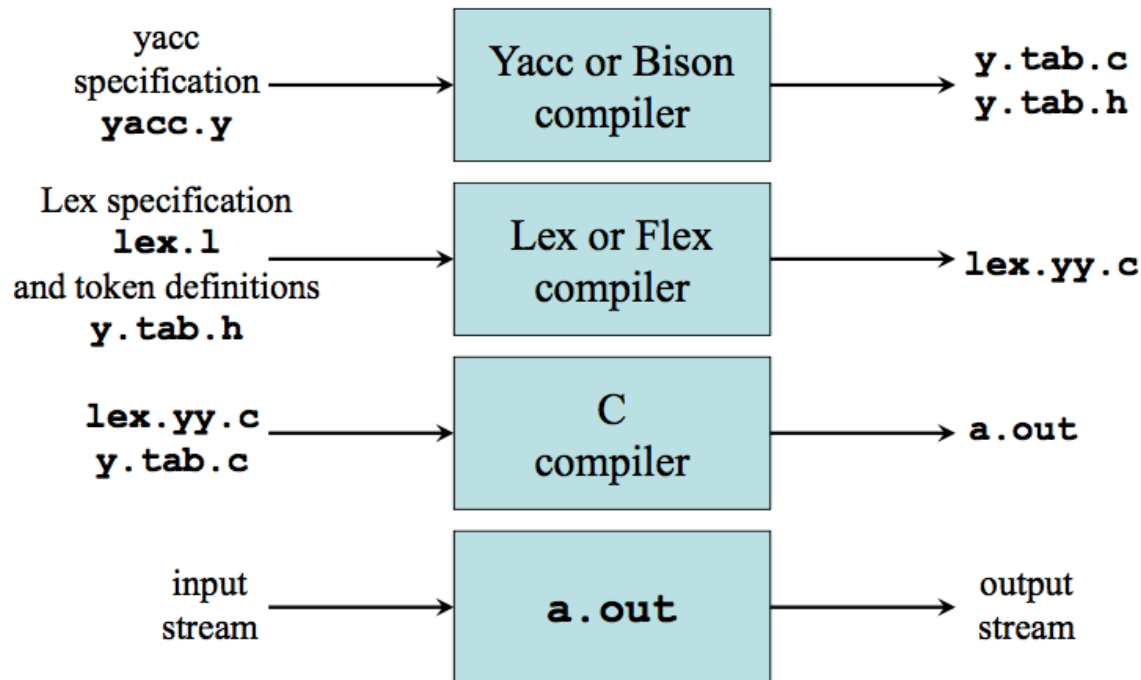
```
1 %{
2 #define YYSTYPE double
3 #include "y.tab.h"
4 extern double yyval;
5 %}
6 number [0-9]+\.[0-9]*|[0-9]*\.[0-9]+
7
8 %%
9
10 [ ]          { /* skip blanks */ }
11 {number}    { sscanf(yytext, "%lf", &yylval);
12              return NUMBER; }
13 \n|.        { return yytext[0]; }
14
15 %%
16
17 int yywrap(void) {
18     return 1;
19 }
```

Generated by Yacc

Defined in y.tab.c

Yacc + Lex

- Lex was designed to produce lexical analyzers that could be used with Yacc
- Yacc generates a parser in `y.tab.c` and a header `y.tab.h`
- Lex includes the header and utilizes token definitions
- Yacc calls `yylex()` to obtain tokens



Example: Yacc + Lex (cont.)

- Compile

- `$yacc -d parser.y`
- `$lex lexer.l`
- `$clang -o test y.tab.c lex.yy.c`

- Run

- `./test < exprs.txt`

```
1 1 + 5
2 1 * 2 + 10
3 10 - 2 -3
```

Detour

- **Lexer**

- **Lex**: initial release in 1975
- **Flex** (fast lexical analyzer generator): written around 1987

- **Parser**

- **Yacc**: full description was published in 1975
- GNU **Bison**: initial release in 1985
- **ANTLR** (ANother Tool for Language Recognition): initial release in 1992

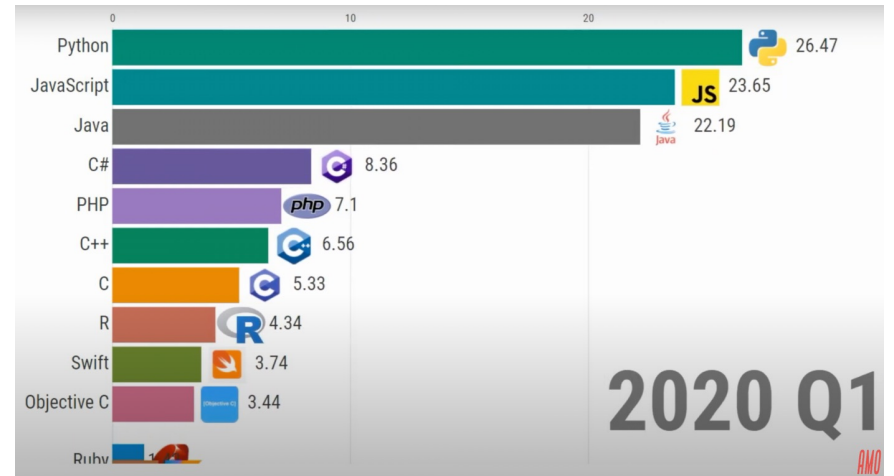
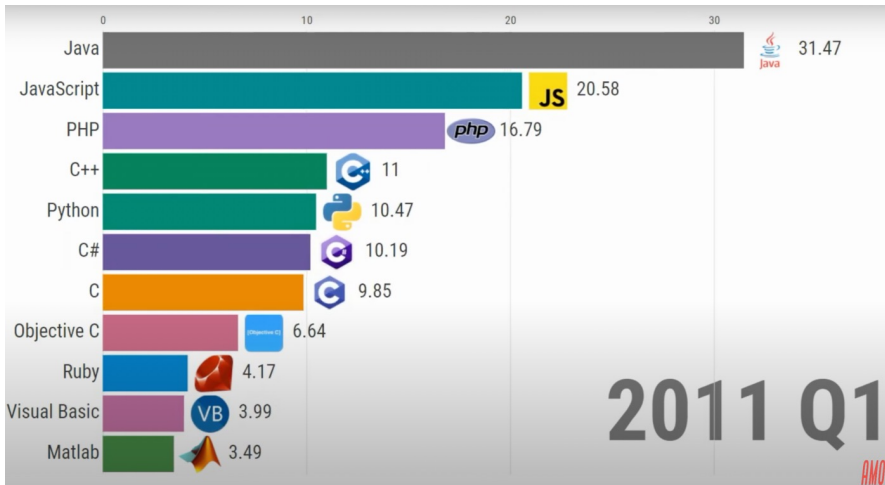
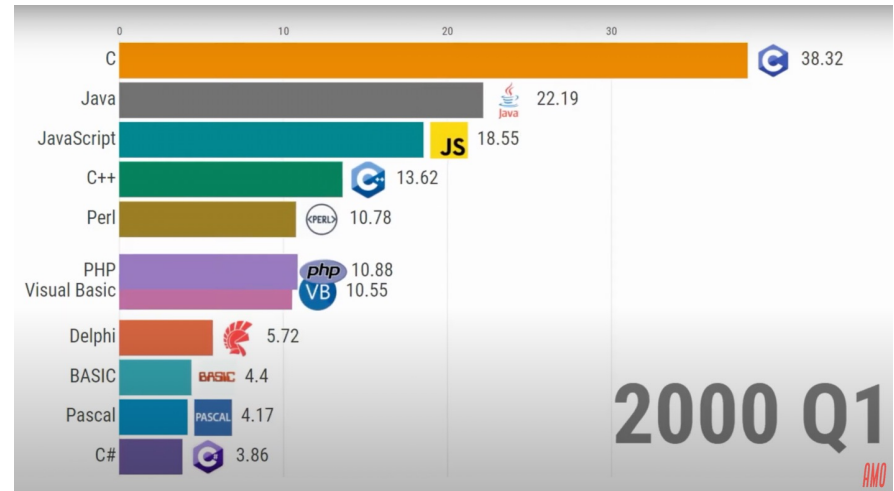
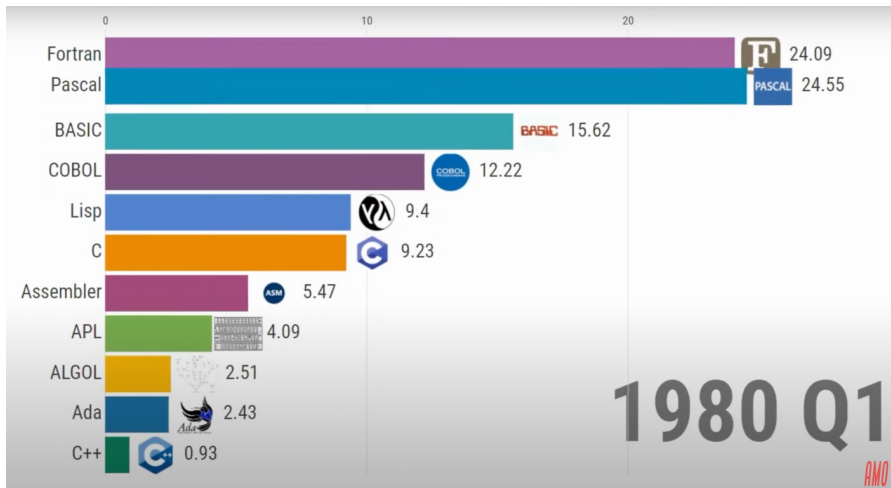
- **Compiler**

- **GCC** (GNU Compiler Collection): initial release in 1987
- **LLVM/Clang**: initial release in 2003/2007

- **Language**

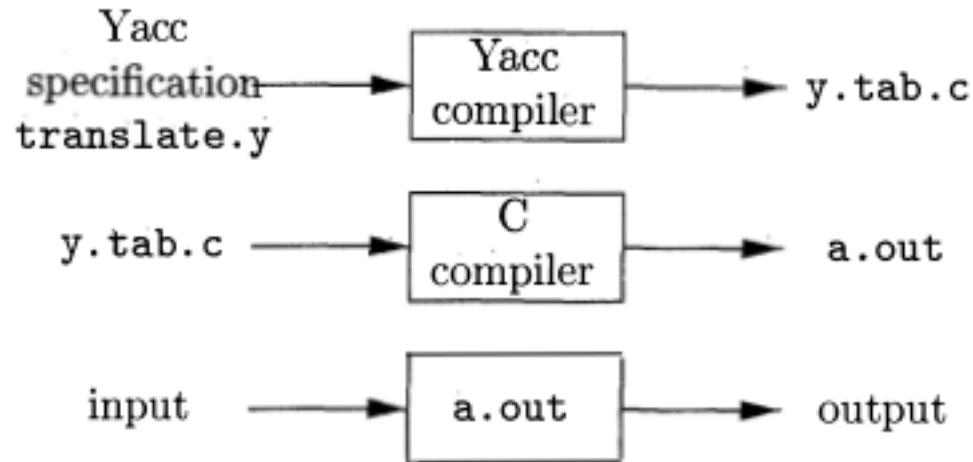
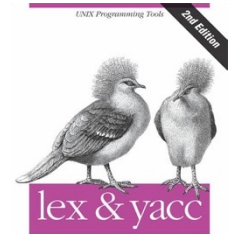
- **C/C++/Python/Java/Rust**: first appeared in 1972/1985/1991/1995/2015

Detour (cont.)



Yacc Overview

- Yacc is an LALR(1) parser generator
 - YACC: Yet Another Compiler-Compiler
 - Parse a language described by a context-free grammar (**CFG**)
 - Yacc constructs an **LALR(1)** table
- Available as a command on the UNIX system
 - Bison: free GNU project alternative to Yacc



Yacc Specification

- **Definitions** section[定义]:
 - C declarations within `{ %}`
 - Token declarations
- **Rules** section[规则]:
 - Each rule consists of a grammar production and the associated semantic action
- **Subroutines** section[辅助函数]:
 - User-defined auxiliary functions

```
{  
  #include ...  
}  
%token NUM VAR  
%%  
production { semantic action }  
...  
%%  
...
```

Write a Grammar in Yacc

- A set of productions $\langle \text{head} \rangle \rightarrow \langle \text{body} \rangle_1 \mid \dots \mid \langle \text{body} \rangle_n$ would be written in YACC as:

```
 $\langle \text{head} \rangle : \langle \text{body} \rangle_1 \{ \langle \text{semantic action} \rangle_1 \}$   
...  
:  $\langle \text{body} \rangle_n \{ \langle \text{semantic action} \rangle_n \}$   
;
```

- Usages

- Tokens that are single characters can be used directly within productions, e.g. '+'
- Named tokens must be declared first in the declaration part using `%token TokenName`

Write a Grammar in Yacc (cont.)

- Semantic actions may refer to values of the synthesized attributes of terminals and non-terminals in a production:

$X : Y_1 Y_2 Y_3 \dots Y_n \{ \text{action} \}$

- $\$\$$ refers to the value of the attribute of X (non-terminal)
- $\$i$ refers to the value of the attribute of Y_i (terminal or non-terminal)
- Normally the semantic action computes a value for $\$\$$ using $\$i$'s

- Example: $E \rightarrow E + T \mid T$

$\text{expr} : \text{expr} '+' \text{term} \{ \$\$ = \$1 + \$2 \}$

$\mid \text{term}$

;

default action: $\{\$\$ = \$1\}$

Example: $E \rightarrow E+E | E-E | E * E | E/E | (E) | \text{num}$

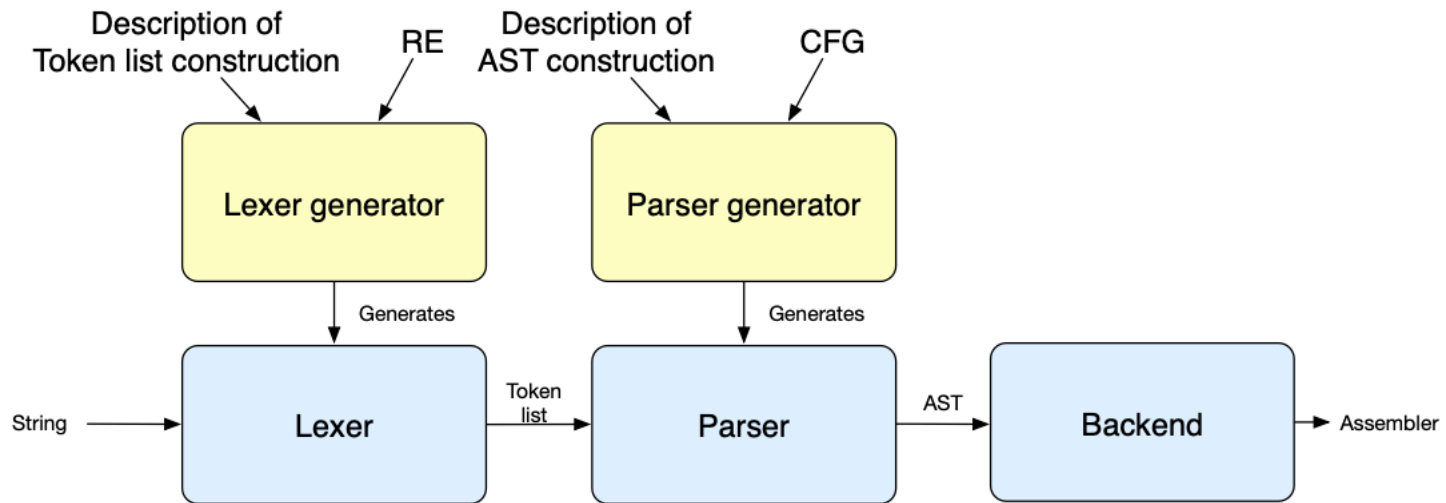
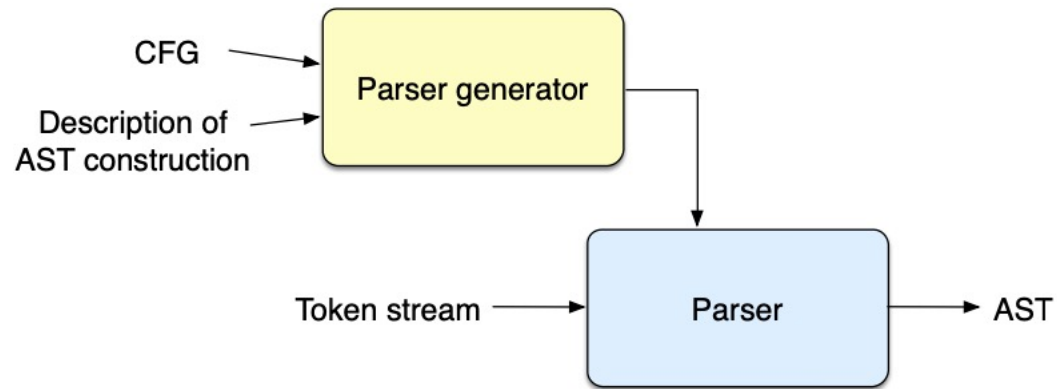
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18       | expr '-' expr { $$ = $1 - $3; }
19       | expr '*' expr { $$ = $1 * $3; }
20       | expr '/' expr { $$ = $1 / $3; }
21       | '(' expr ')' { $$ = $2; }
22       | NUMBER
23       ;
```

Can we remove those two lines?

Allow to evaluate a sequence of expressions, one to a line

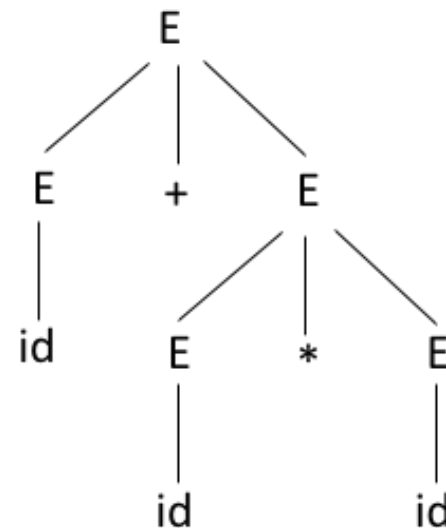
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Parser





Parser Types[分析器类型]

- **Grammar** is used to derive string or construct **parser**
- Most compilers use either **top-down** or **bottom-up** parsers
- **Top-down parsing**[自顶向下分析]
 - Starts from root and expands into leaves
 - Tries to **expand start symbol to input string**
 - Finds leftmost derivation[最左推导]
 - In each step
 - Which non-terminal to replace?[哪个符号?]
 - Which production of the non-terminal to use?[哪个规则?]
 - Parser code structure closely mimics grammar
 - Amenable to implementation by hand
 - Automated tools exist to convert to code (e.g. ANTLR)



ANTLR

Parser Types (cont.)

- Bottom-up parser[自底向上分析]
 - Starts at leaves and builds up to root
 - Tries to **reduce the input string to the start symbol**
 - Finds reverse order of the rightmost derivation[最右推导的逆 → 最左归约, 也称为规范归约]
 - Parser code structure nothing like grammar
 - Very difficult to implement by hand
 - Automated tools exist to convert to code (e.g. Yacc, Bison)
 - $LL \subset LR$ (Bottom-up works for a larger class of grammars)
- Top-down vs. bottom-up[对比]
 - Top-down: easier to understand and implement manually
 - E.g., ANTLR 
 - Bottom-up: more powerful, can be implemented automatically
 - E.g., YACC/Bison 

Example

- Consider a CFG grammar G

$$S \rightarrow AB$$

$$A \rightarrow aC$$

$$B \rightarrow bD$$

$$D \rightarrow d$$

$$C \rightarrow c$$

- This language has only one sentence: $L(G) = \{acbd\}$

Top-down (leftmost derivation)

$$\begin{aligned} S &\Rightarrow AB \quad (1) \\ &\Rightarrow aCB \quad (2) \\ &\Rightarrow acB \quad (3) \\ &\Rightarrow acbD \quad (4) \\ &\Rightarrow acbd \quad (5) \end{aligned}$$

Bottom-up (reverse of rightmost derivation)

$$\begin{aligned} S &\Rightarrow AB \quad (5) \\ &\Rightarrow AbD \quad (4) \\ &\Rightarrow Abd \quad (3) \\ &\Rightarrow aCbd \quad (2) \\ &\Rightarrow acbd \quad (1) \end{aligned}$$

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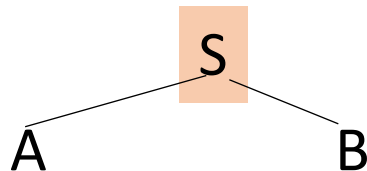
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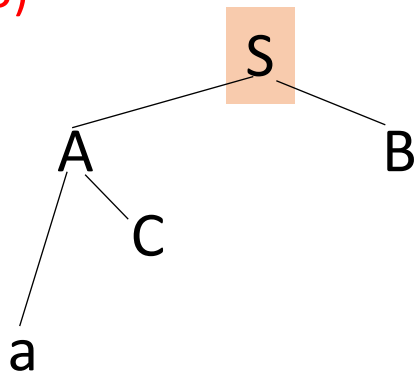
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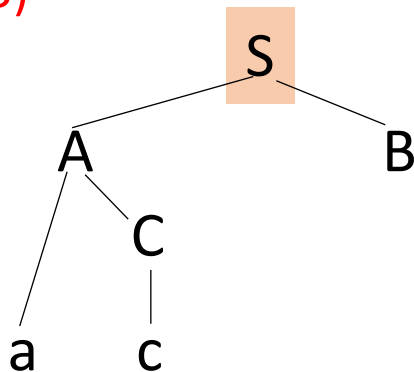
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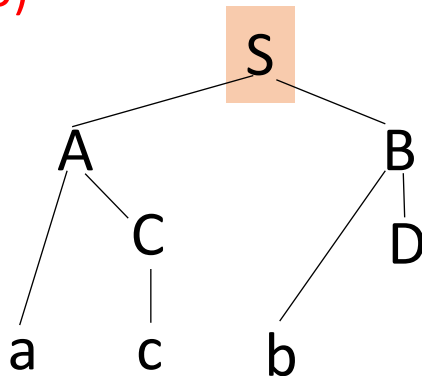
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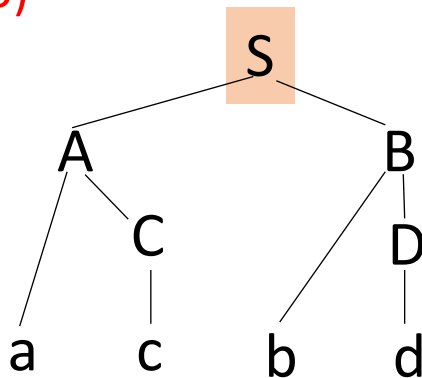
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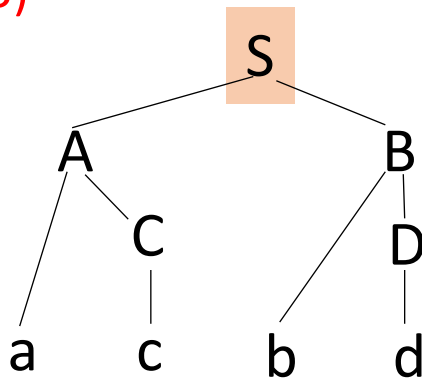
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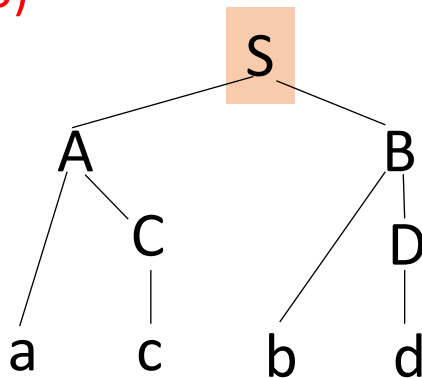
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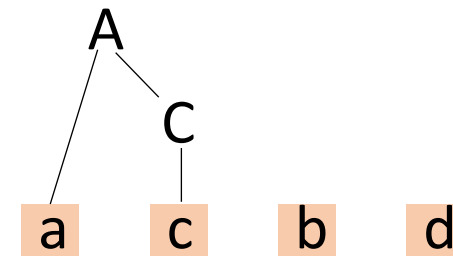
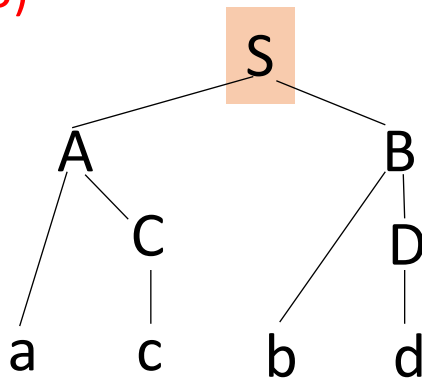
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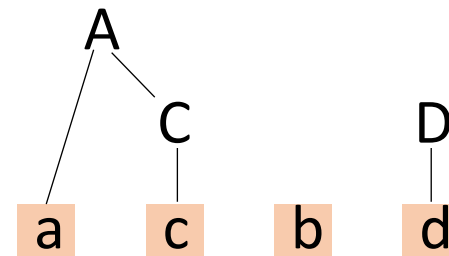
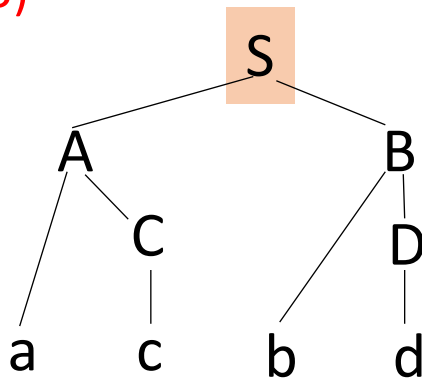
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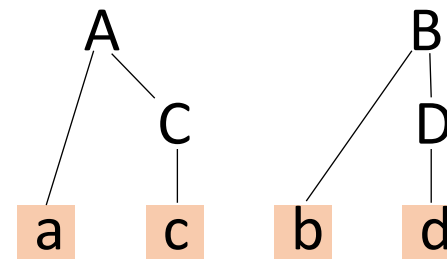
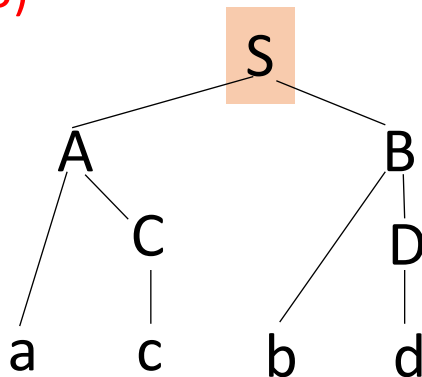
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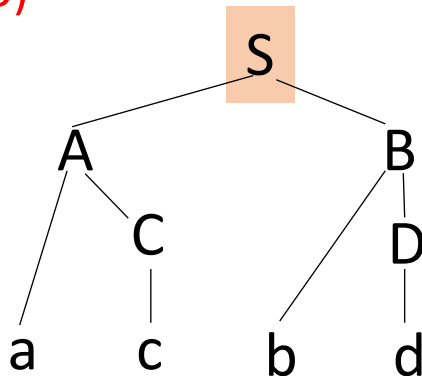
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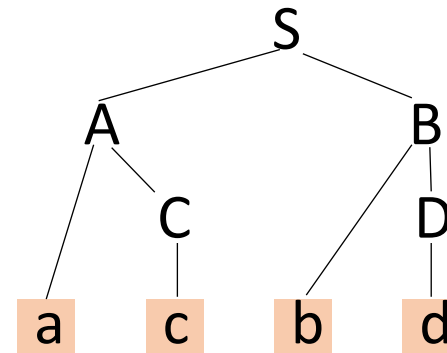
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Preview: Bottom-up Parsing[自底向上]

- Consider a CFG grammar G

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$C \rightarrow c$

Stack	Input	Action
\$	acbd\$	Shift
\$a	cbd\$	Shift
\$ac	bd\$	Reduce
\$aC	bd\$	Reduce
\$A	bd\$	Shift
\$Ab	d\$	Shift
\$Abd	\$	Reduce
\$AbD	\$	Reduce
\$AB	\$	Reduce
\$S	\$	<u>SUCCESS!</u>

Bottom-up (reverse of rightmost derivation)

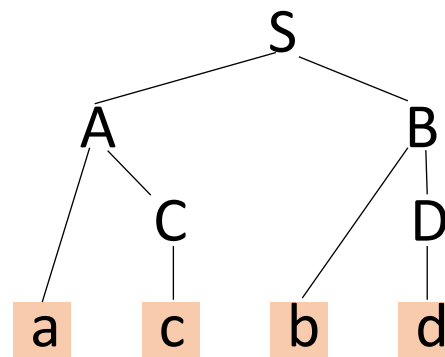
$S \Rightarrow AB$ (5)

$\Rightarrow AbD$ (4)

$\Rightarrow Abd$ (3)

$\Rightarrow aCbd$ (2)

$\Rightarrow acbd$ (1)



Top-down Parsers[自顶向下]

- **Recursive descent parser (RDP, 递归下降分析) with backtracking[回溯]**
 - Implemented using recursive calls to functions that implement the **expansion** of each non-terminal[非终结符-展开]
 - Goes through all possible expansions by **trial-and-error** until match with input; backtracks when mismatch detected[试错-回溯]
 - Simple to implement, but may take exponential time
- **Predictive parser[预测分析]**
 - Recursive descent parser with prediction (no backtracking)
 - Predict next rule by looking ahead k number of symbols
 - Restrictions on the grammar to avoid backtracking
 - Only works for a class of grammars called **LL(k)**

Classify rule: for a non-terminal, which production to use?

RDP with Backtracking[回溯]

- **Approach:** for a non-terminal in the derivation, productions are tried in some order until[N: 展开]
 - A production is found that generates a portion of the input, or[向前推进]
 - No production is found that generates a portion of the input, in which case backtrack to previous non-terminal[向后回溯]
- Terminals of the derivation are compared against input[T: 比较]
 - Match: advance input, continue parsing[能对上, 向前推]
 - Mismatch: backtrack, or fail[对不上, 向后退]
- Parsing fails if no derivation generates the entire input

Example

- Consider the grammar

$$S \rightarrow cAd \quad A \rightarrow ab \mid a$$

- To construct a parse tree top-down for input string $w=cad$
 - Begin with a tree consisting of a single node labeled S

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- To construct a parse tree top-down for input string $w=cad$
 - Begin with a tree consisting of a single node labeled S
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 - S has only one production, so we use it to expand S and obtain the tree

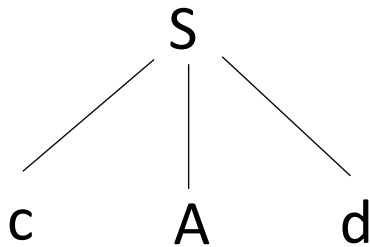
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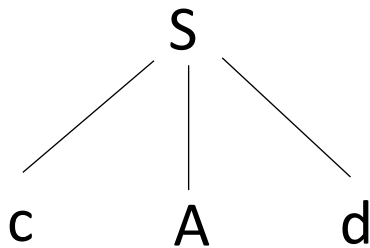
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- To construct a parse tree top-down for input string $w=cad$

–

- The leftmost leaf, labeled c , matches the first symbol of w

- So we advance the input pointer to a (i.e., the 2nd symbol of w) and consider the next leaf A

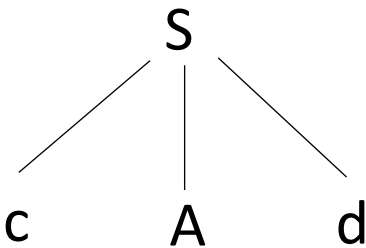


Example (cont.)

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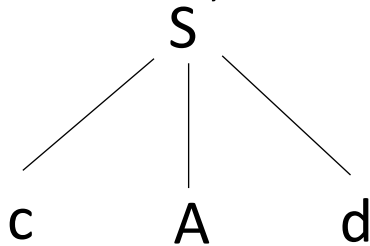
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- Next, expand A using $A \rightarrow ab$

- Have a match for the 2nd input symbol, a , so advance the input pointer to d , the 3rd input symbol



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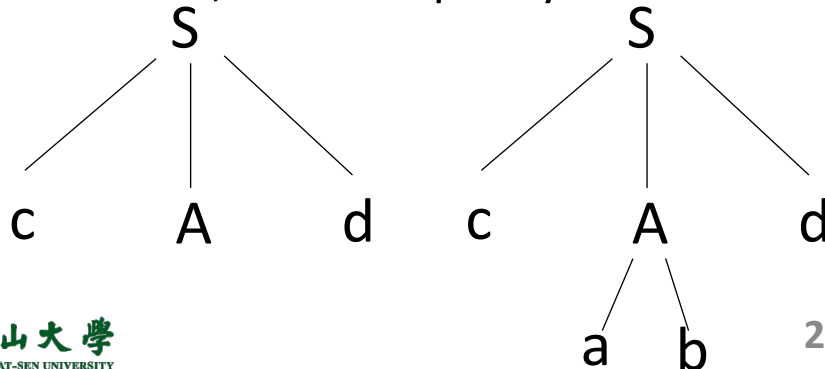
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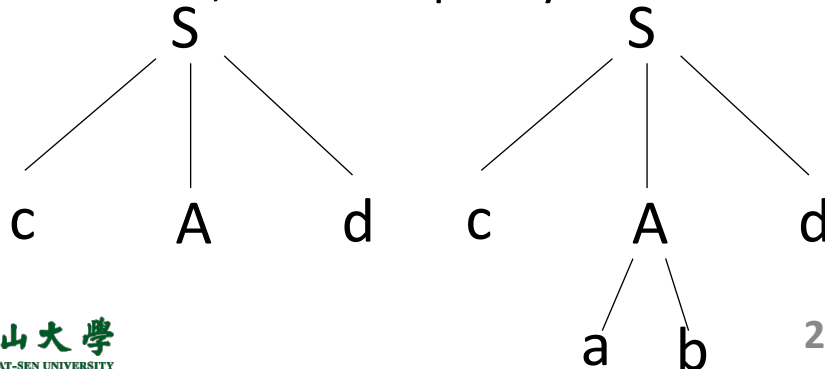
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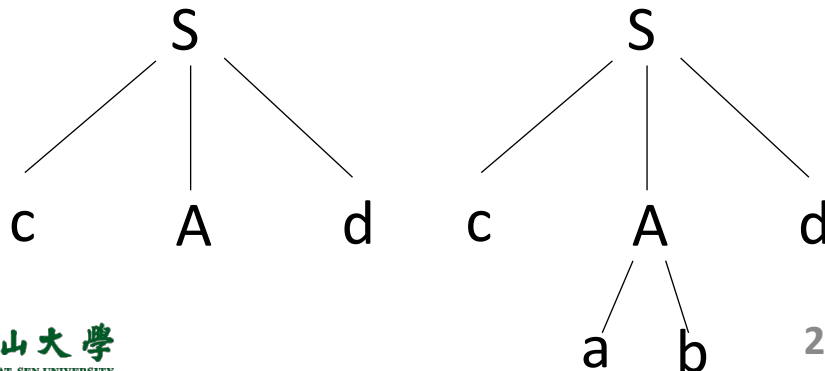
$S \rightarrow cAd$ $A \rightarrow ab \mid a$

- To construct a parse tree top-down for input string $w=cad$

-

- b does not match d , report failure and go back to A

- See whether there is another alternative for A that has not been tried
- In going back to A , we must reset the input pointer as well



Example (cont.)

- Consider the grammar

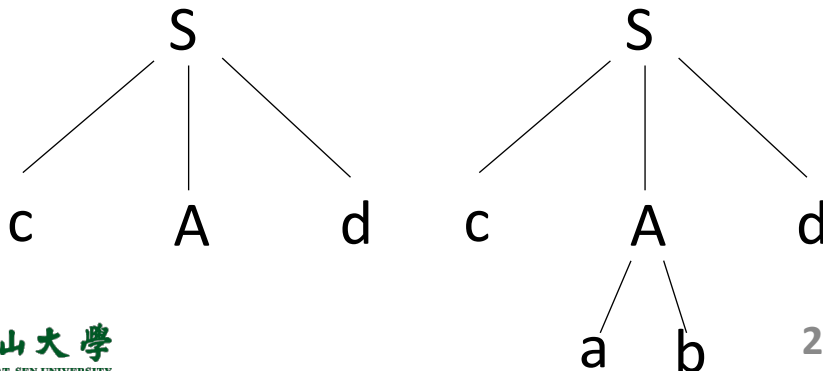
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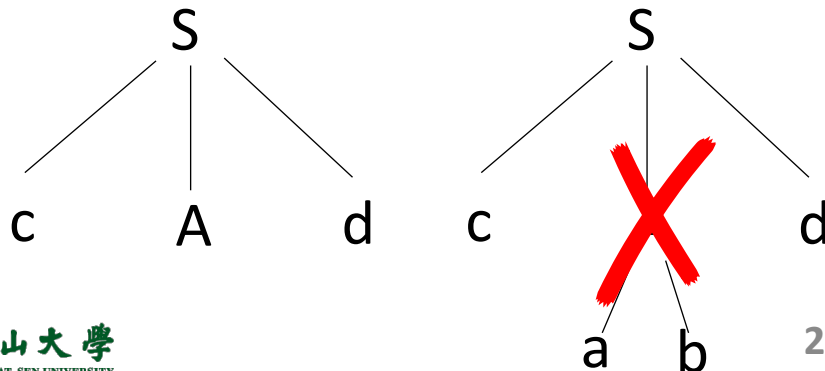
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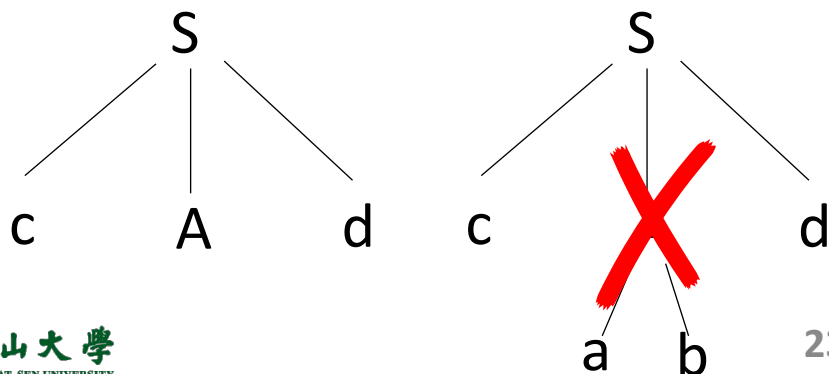
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▫ See whether there is another alternative for A that has not been tried

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– Leaf a matches the 2nd symbol of w , and leaf d matches the 3rd

– We have produced a parse tree for w , we halt and success



Example (cont.)

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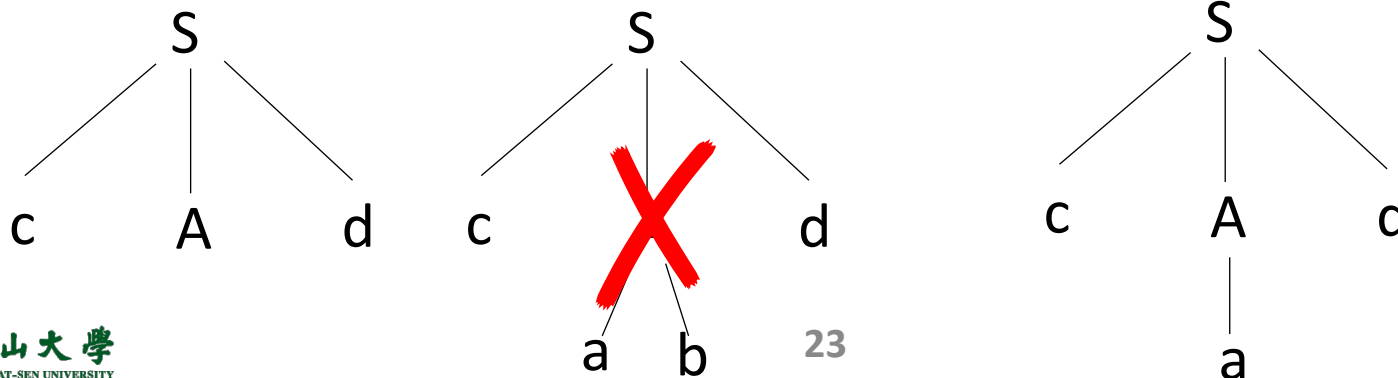
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Left Recursion Problem[左递归问题]

- Recursive descent **doesn't work with left recursion**
 - Right recursion is OK
- Why is left recursion[左递归] a problem?
 - For left recursive grammar
$$A \rightarrow Ab|c$$
 - We may repeatedly choose to apply $A b$
$$A \Rightarrow A b \Rightarrow A b b \dots$$
 - Sentential form can grow indefinitely w/o consuming input[句型无限增长而不消耗输入]
 - Non-terminal: expand, terminal: match
 - How do you know when to stop recursion and choose c ?
- Rewrite the grammar so that it is right recursive[改为右递归]
 - Which expresses the same language[等价]

Left Recursion[左递归]

- A grammar is left recursive if
 - It has a nonterminal A such that there is a derivation $A \Rightarrow^+ A\alpha$ for some string α
- Recursion types [直接和间接左递归]
 - **Immediate left recursion**, where there is a production $A \rightarrow A\alpha$
 - Non-immediate: left recursion involving derivation of 2+ steps
 - $S \rightarrow Aa \mid b$
 - $A \rightarrow Sd \mid \epsilon$
 - $S \Rightarrow Aa \Rightarrow Sda$
-  Algorithm to systematically eliminates left recursion from a grammar

Remove Left Recursion[消除左递归]

- Grammar: $A \rightarrow A\alpha \mid \beta$ ($\alpha \neq \beta$, β doesn't start with A)

$$A \Rightarrow A\alpha$$

$$\Rightarrow A\alpha\alpha$$

...

$$\Rightarrow A\alpha\dots\alpha\alpha$$

$$\Rightarrow \beta\alpha\dots\alpha\alpha$$

$$r = \beta\alpha^*$$

- Rewrite to:

$$A \rightarrow \beta A'$$

// begins with β (A' is a new non-terminal)

$$A' \rightarrow \alpha A' \mid \varepsilon$$

// A' is to produce a sequence of α

$$\Rightarrow \alpha\alpha A'$$

...

$$\Rightarrow \alpha\dots\alpha A' \Rightarrow \alpha\dots\alpha$$

Remove Left Recursion (cont.)

- Grammar:

$$A \rightarrow A\alpha \mid \beta$$

to

$$A \rightarrow \beta A'$$

$$A' \rightarrow \alpha A' \mid \varepsilon$$

- $E \rightarrow E \underline{+ T} \mid \underline{T}$
 $\alpha \quad \beta$



$$E \rightarrow TE'$$
$$E' \rightarrow +TE' \mid \varepsilon$$

- $T \rightarrow T \underline{* F} \mid \underline{F}$
 $\alpha \quad \beta$



$$T \rightarrow FT'$$
$$T' \rightarrow *FT' \mid \varepsilon$$

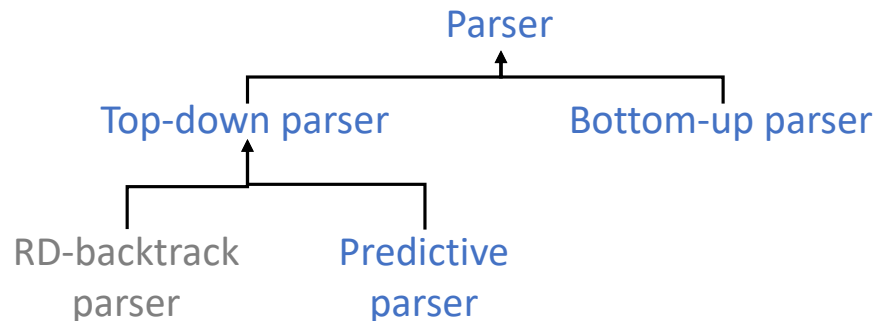
- $F \rightarrow (E) \mid \text{id}$



$$F \rightarrow (E) \mid \text{id}$$

Summary of RD-backtrack[小结]

- **RD-backtrack** is a simple and general parsing strategy
 - Left-recursion must be eliminated first
 - Can be eliminated automatically using some algorithm
 - $L(\text{Recursive_descent}) \equiv L(\text{CFG}) \equiv \text{CFL}$
- However it is **not popular** because of **backtracking**
 - Backtracking requires re-parsing the same string
 - Which is inefficient (can take exponential time)
 - Also undoing semantic actions may be difficult
 - E.g. removing already added nodes in parse tree



Predictive Parsers[预测分析]

- In recursive descent with backtracking[有回溯]:
 - At each step, many choices of production to use
 - Backtracking used to undo bad choices
- A parser with **no backtracking**[无回溯]: **predict** correct next production given next input terminal(s)?[以下面一些输入来预测]
 - If first terminal of every alternative production is **unique**, then parsing requires no backtracking[候选产生式首符号唯一]
 - If not unique, grammar cannot use predictive parsers[不唯一]

$A \rightarrow aBD \mid bBB$

$B \rightarrow c \mid bce$

$D \rightarrow d$

parsing input “**abcd**” requires no backtracking

?: 如果只往前看一个，那么next terminal其实就是current terminal，即要匹配的那个（注意backtrack是完全不看）